

SNS COLLEGE OF TECHNOLOGY (AN AUTONOMOUS INSTITUTION)

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Department of Biomedical Engineering

Course Name: Biocontrol System

II Year : IV Semester

Unit I – Introduction to physiological modeling

Topic : Modeling of control system

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Introduction

- control systems can be represented with a set of The mathematical equations known as mathematical model. These models are useful for analysis and design of control systems.
- The following mathematical models are mostly used.
 - Differential equation model
 - Transfer function model
 - State space model \checkmark







Mathematical Model

- A mathematical model is a set of equations (usually differential equations) that represents the dynamics of systems.
- In practice, the complexity of the system requires some assumptions in the determination model.
- How do we obtain the equations?
 - Physical law of the process
 - Examples: •
 - Mechanical system (Newton's laws) \checkmark
 - Electrical system (Kirchhoff's laws) \checkmark





Transfer Function

- Transfer function model is an s-domain mathematical model of control systems.
- The Transfer function of a Linear Time Invariant (LTI) system is defined as the ratio of Laplace transform of output and Laplace transform of input by assuming all the initial conditions are zero.

$$\frac{X(s)}{X(s)} \xrightarrow{Y(s)} Y(s)$$

$$\frac{Y(s)}{X(s)} \xrightarrow{Y(s)} Y(s)$$

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Figure 1: Scheme of an active vehicle suspension system







- Mechanical systems mainly consists of three main elements namely • mass, dashpot and spring.
- If a force is applied to a translational mechanical system, then it is • opposed by opposing forces due to mass, elasticity and friction of the system.
- Since the applied force and the opposing forces are in opposite • directions, the algebraic sum of the forces acting on the system is zero.







 $F_m \propto a$

 $F_m = M_a = M \frac{d^2 x}{dt^2}$

 $F = F_m = M \frac{d^2 x}{dt^2}$

Where,

- **F**_m is the opposing force due to mass
- **M** is mass
- **a** is acceleration
- **x** is displacement

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Mass:



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• **F** is the applied force



Spring:

Mechanical System





 $F_k = Kx$

$$F = F_k = Kx$$

Where,

- **F** is the applied force
- **F**_k is the opposing force due to elasticity of spring
- K is spring constant •
- **x** is displacement







 $F_h \propto v$

 $F_b = Bv = B\frac{dx}{dt}$

 $F = F_b = B$

dx

dt



Where,

- **F** is the applied force
- **F**_k is the opposing force due to friction of dashpot **B** is spring constant frictional coefficient ullet
- v is velocity
- x is displacement

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Transfer function of the mechanical translational system given in figure. \checkmark







0



Electrical System

Resistance



V-I in time domain

- $\nu_R(t) = i_R(t)R$
- V-I in s domain

 $V_R(s) = I_R(s)R$

Inductance



V-I in time domain

$$\nu_L(t) = L \frac{di_L(t)}{dt}$$

V-I in s domain

 $V_L(s) = sLI_L(s)$

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$$\nu_c(t) = \frac{1}{C} \int i_c(t) dt$$

V-I in s domain

$$V_c(s) = \frac{1}{Cs} I_c(s)$$



Electrical System

Transfer function $G(s) = E_o(s) / E_i(s)$ of the RLC network



