

SNS COLLEGE OF TECHNOLOGY



Coimbatore-641035 An Autonomous Institution

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DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

23ECT212 - LINEAR CONTROL SYSTEMS

II YEAR/ IV SEMESTER

UNIT I – CONTROL SYSTEM MODELING

TOPIC - SIGNAL FLOW GRAPH



OUTLINE



- •REVIEW ABOUT PREVIOUS CLASS
- INTRODUCTION
- •BASIC ELEMENTS OF SIGNAL FLOW GRAPH
- •6 -EXAMPLE-SFG
- •ACTIVITY
- •CONVERSION OF BLOCK DIAGRAMS INTO SIGNAL FLOW GRAPHS
- •EXAMPLE
- •MASON'S GAIN FORMULA
- •SUMMARY



INTRODUCTION



- Signal flow graph is a graphical representation of algebraic equations
- The block diagram reduction process takes more time for complicated system
- So, to overcome this drawback, use signal flow graphs (representation) is done where the calculation of transfer function is just by using a Mason's gain formula without doing any reduction process.



BASIC ELEMENTS OF SIGNAL FLOW GRAPH



Nodes and branches are the basic elements of signal flow graph.

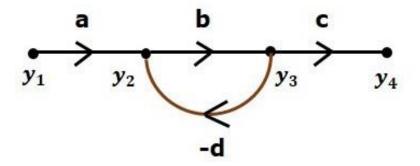
Node

Node is a point which represents either a variable or a signal. There are three types of nodes — input node, output node and mixed node.

Input Node – It is a node, which has only outgoing branches.

Output Node – It is a node, which has only incoming branches.

Mixed Node – It is a node, which has both incoming and outgoing branches.





BASIC ELEMENTS OF SIGNAL FLOW GRAPH...



- Forward path: It is a path from an input node to an output node that does not cross any node more than once.
- Individual loop: It is a closed path starting from one node and after passing through the graph arrives at the same node without crossing any node more than once.
- Non-touching loops: If a loop does not have a common node then they are said to be non-touching loops



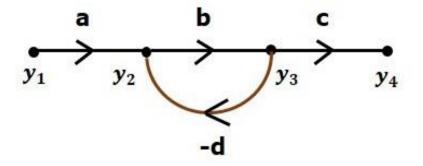
EXAMPLE



Let us consider the following signal flow graph to identify these nodes.

- The **nodes** present in this signal flow graph are y_1 , y_2 , y_3 and y_4 .
- $\bullet y_1$ and y_4 are the **input node** and **output node** respectively.
- • y_2 and y_3 are mixed nodes.

Branch is a line segment which joins two nodes. It has both **gain** and **direction**. For example, there are four branches in the above signal flow graph. These branches have **gains** of **a**, **b**, **c** and **-d**.



EXAMPLE



Let us construct a signal flow graph by considering the following algebraic eqns. –

$$egin{aligned} y_2 &= a_{12}y_1 + a_{42}y_4 \ & y_3 &= a_{23}y_2 + a_{53}y_5 \ & y_4 &= a_{34}y_3 \ & y_5 &= a_{45}y_4 + a_{35}y_3 \ & y_6 &= a_{56}y_5 \end{aligned}$$

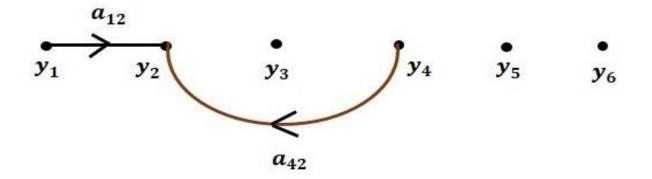
There will be six **nodes** $(y_1, y_2, y_3, y_4, y_5 \text{ and } y_6)$ and eight **branches** in this signal flow graph. The gains of the branches are a_{12} , a_{23} , a_{34} , a_{45} , a_{56} , a_{42} , a_{53} and a_{35} .

To get the overall signal flow graph, draw the signal flow graph for each equation, then combine all these signal flow graphs and then follow the steps given below –

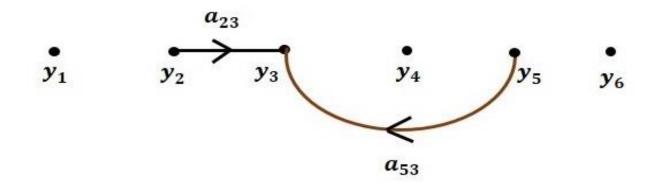


Step 1 – Signal flow graph for $y_2=a_{13}y_1+a_{42}y_4$ is shown in the following figure.

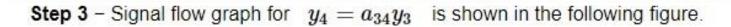




Step 2 – Signal flow graph for $y_3=a_{23}y_2+a_{53}y_5$ is shown in the following figure.

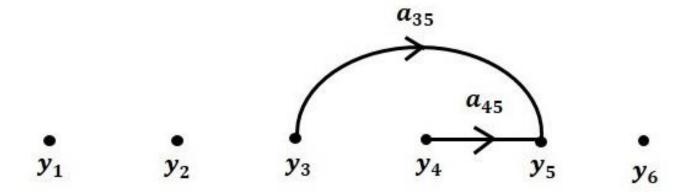




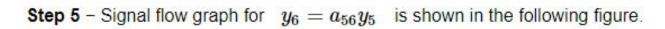




Step 4 – Signal flow graph for $y_5=a_{45}y_4+a_{35}y_3$ is shown in the following figure.



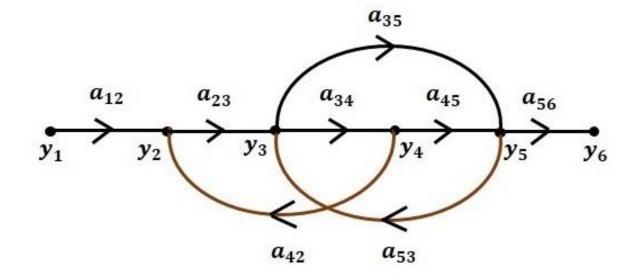








Step 6 - Signal flow graph of overall system is shown in the following figure.









ODD MAN OUT WITH REASON..?

108,120,132,144,156,164

Options:

A - 156

B - 164

C - 120

D - 108

Three of the following four are same in a certain way and hence form a group. Find out the one which does not belong to that group.

Options:

A - Violet

B - Black

C - Green

D - Red



CONVERSION OF BLOCK DIAGRAMS INTO SIGNAL FLOW GRAPHS



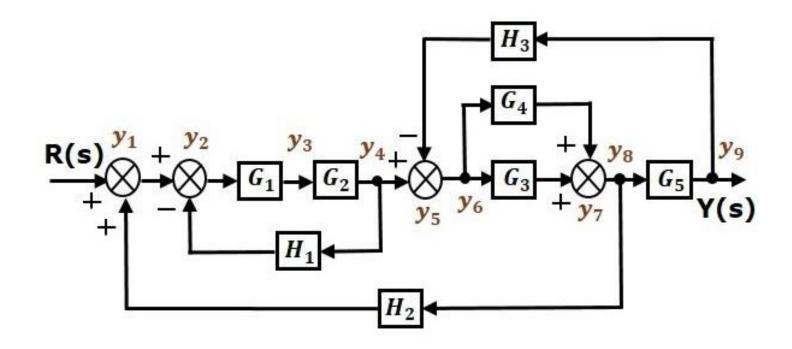
- Represent all the signals, variables, summing points and take-off points of block diagram as **nodes** in signal flow graph.
- Represent the blocks of block diagram as **branches** in signal flow graph.
- Represent the transfer functions inside the blocks of block diagram as **gains** of the branches in signal flow graph.
- Connect the nodes as per the block diagram.



EXAMPLE



Let us convert the following block diagram into its equivalent signal flow graph.





EXAMPLE ...



Represent the input signal R(s)R(s) and output signal C(s)C(s) of block diagram as input node R(s)R(s) and output node R(s)C(s) of signal flow graph.

Just for reference, the remaining nodes $(y_1 \text{ to } y_9)$ are labelled in the block diagram. There are nine nodes other than input and output nodes.

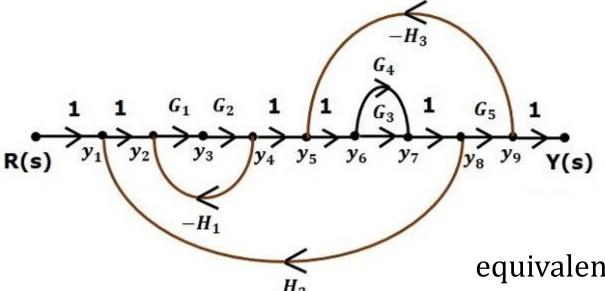
That is four nodes for four summing points, four nodes for four take-off points and one node for the variable between blocks G1G1 and G2G2.

The following figure shows the equivalent signal flow graph.



EXAMPLE ...





equivalent signal flow graph

With the help of **Mason's gain formula** you can calculate the transfer function of this signal flow graph.

This is the advantage of signal flow graphs.

To simplify (reduce) the signal flow graphs for calculating the transfer function.







Mason's gain formula statio that,

Overall gain,
$$T = \frac{1}{\Delta} \leq \frac{1}{K} = \frac{$$



MASON'S GAIN FORMULA



Let us now discuss the Mason's Gain Formula. Suppose there are 'N' forward paths in a signal flow graph.

The gain between the input and the output nodes of a signal flow graph is nothing but the **transfer function** of the system. It can be calculated by using Mason's gain formula.



MASON'S GAIN FORMULA



- Represent all the signals, variables, summing points and take-off points of block diagram as **nodes** in signal flow graph.
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- Connect the nodes as per the block diagram.



MASON'S GAIN FORMULA



$$T = rac{C(s)}{R(s)} = rac{\Sigma_{i=1}^N P_i \Delta_i}{\Delta}$$

Where,

- C(s) is the output node
- R(s) is the input node
- $^{ t B}$ **T** is the transfer function or gain between R(s) and C(s)
- P_i is the ith forward path gain

 $\Delta = 1 - (sum\ of\ all\ individual\ loop\ gains)$

 $+(sum\ of\ gain\ products\ of\ all\ possible\ two\ nontouching\ loops)$

 $-(sum\ of\ gain\ products\ of\ all\ possible\ three\ nontouching\ loops)+\dots$

 Δ_i is obtained from Δ by removing the loops which are touching the ith forward path.

Consider the following signal flow graph in order to understand the basic terminology involved here.





SUMMARY

