

SNS COLLEGE OF TECHNOLOGY

Coimbatore-641035 An Autonomous Institution



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DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

23ECT212 – LINEAR CONTROL SYSTEMS

II YEAR/ IV SEMESTER

UNIT I – CONTROL SYSTEM MODELING

TOPIC - SIGNAL FLOW GRAPH

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•REVIEW ABOUT PREVIOUS CLASS •TERMINOLOGY OF SIGNAL FLOW GRAPH •PATH, FORWARD PATH, FORWARD PATH GAIN •LOOP, LOOP GAIN, NON-TOUCHING LOOPS •ACTIVITY •MASON'S GAIN FORMULA •CALCULATION OF TRANSFER FUNCTION USING MASON'S GAIN FORMULA •EXAMPLE •SUMMARY



SIGNAL FLOW GRAPH- TERMINOLOGY



Consider the following signal flow graph in order to understand the basic terminology involved here.





SIGNAL FLOW GRAPH-TERMINOLOGY



Path

It is a traversal of branches from one node to any other node in the direction of branch arrows. It should not traverse any node more than once.

Examples – $y2 \rightarrow y3 \rightarrow y4 \rightarrow y5$ and $y5 \rightarrow y3 \rightarrow y2$

Forward Path

The path that exists from the input node to the output node is known as **forward path**. **Examples** $-y_1 \rightarrow y_2 \rightarrow y_3 \rightarrow y_4 \rightarrow y_5 \rightarrow y_6$ and $y_1 \rightarrow y_2 \rightarrow y_3 \rightarrow y_5 \rightarrow y_6$

Forward Path Gain

It is obtained by calculating the product of all branch gains of the forward path. **Examples** – **abcde** is the forward path gain of $y1 \rightarrow y2 \rightarrow y3 \rightarrow y4 \rightarrow y5 \rightarrow y6y1 \rightarrow y2 \rightarrow y3 \rightarrow y4 \rightarrow y5 \rightarrow y6$ and **abge** is the forward path gain of $y1 \rightarrow y2 \rightarrow y3 \rightarrow y5 \rightarrow y6y1 \rightarrow y2 \rightarrow y3 \rightarrow y5 \rightarrow y6$



SIGNAL FLOW GRAPH- TERMINOLOGY



Loop

The path that starts from one node and ends at the same node is known as **loop**. Hence, it is a closed path.

Examples – $y2 \rightarrow y3 \rightarrow y2$ and $y3 \rightarrow y5 \rightarrow y3$

Loop Gain

It is obtained by calculating the product of all branch gains of a loop.

Examples – b_j is the loop gain of $y2\rightarrow y3\rightarrow y2$ and gh is the loop gain of $y3\rightarrow y5\rightarrow y3$.

Non-touching Loops

These are the loops, which should not have any common node.

Examples – The loops, $y_2 \rightarrow y_3 \rightarrow y_2$ and $y_4 \rightarrow y_5 \rightarrow y_4$ are non-touching.



ACTIVITY -BLOOD RELATION TEST



- Pointing to a photograph of a boy Suresh said, "He is the son of the only son of my mother." How is Suresh related to that boy?
 - A. Brother
 - B. Uncle
 - C. Cousin
 - D. Father



CALCULATION OF TRANSFER FUNCTION USING MASON'S GAIN FORMULA



Let us consider the same signal flow graph for finding transfer function.



Answer: Option D Explanation:

The boy in the photograph is the only son of the son of Suresh's mother i.e., the son of Suresh. Hence, Suresh is the father of boy.





•Number of forward paths, N = 2.

•First forward path is - $y1 \rightarrow y2 \rightarrow y3 \rightarrow y4 \rightarrow y5 \rightarrow y6$.

•First forward path gain, p1=abcde

•Second forward path is - $y1 \rightarrow y2 \rightarrow y3 \rightarrow y5 \rightarrow y6$

•Second forward path gain, p2=abge

•Number of individual loops, L = 5.





^a Loops are - $y_2 o y_3 o y_2$, $y_3 o y_5 o y_3$, $y_3 o y_4 o y_5 o y_3$

 $y_4
ightarrow y_5
ightarrow y_4$ and $y_5
ightarrow y_5$.

- $^{
 all}$ Loop gains are $l_1=bj$, $l_2=gh$, $l_3=cdh$, $l_4=di$ and $l_5=f$.
- Number of two non-touching loops = 2.
- ${}^{=}$ First non-touching loops pair is $y_2 o y_3 o y_2$, $y_4 o y_5 o y_4$.
- $^{ imes}$ Gain product of first non-touching loops pair, $l_1l_4=bjdi$
- $^{\scriptscriptstyle \blacksquare}$ Second non-touching loops pair is $y_2 o y_3 o y_2$, $y_5 o y_5$.
- $^{ imes}$ Gain product of second non-touching loops pair is $~l_1l_5=bjf$





Higher number of (more than two) non-touching loops are not present in this signal flow graph.

We know,

 $\Delta = 1$ –(sum of all individual loop gains)

+(sum of gain products of all possible two non touching loops)

-(sum of gain products of all possible three non touching loops)+...





Substitute the values in the above equation, $\Delta = 1 - (bj+gh+cdh+di+f) + (bjdi+bjf) - (0)$

 $\Delta = 1 - (bj+gh+cdh+di+f) + (bjdi+bjf)$

 $\Rightarrow \Delta = 1 - (bj+gh+cdh+di+f)+bjdi+bjf$

There is no loop which is non-touching to the first forward path.

So, $\Delta_1=1$ Similarly, $\Delta_2=1$

Since, no loop which is non-touching to the second forward path.

Substitute,

N = 2 in Mason's gain formula



MASON'S GAIN FORMULA



 $T=rac{C(s)}{R(s)}=rac{\Sigma_{i=1}^NP_i\Delta_i}{\Delta}$

Where,

- C(s) is the output node
- R(s) is the input node

T is the transfer function or gain between R(s) and C(s)

P_i is the ith forward path gain

 $\Delta = 1 - (sum \, of \, all \, individual \, loop \, gains)$

+(sum of gain products of all possible two nontouching loops)

-(sum of gain products of all possible three nontouching loops)+...

 Δ_i is obtained from Δ by removing the loops which are touching the *i*th forward path. Consider the following signal flow graph in order to understand the basic terminology involved here.





Substitute, N = 2 in Mason's gain formula

$$T=rac{C(s)}{R(s)}=rac{\Sigma_{i=1}^2P_i\Delta_i}{\Delta}$$

$$T=rac{C(s)}{R(s)}=rac{P_1\Delta_1+P_2\Delta_2}{\Delta}$$

Substitute all the necessary values in the above equation.

$$T=rac{C(s)}{R(s)}=rac{(abcde)1+(abge)1}{1-(bj+gh+cdh+di+f)+bjdi+bjf}$$

$$\Rightarrow T = \frac{C(s)}{R(s)} = \frac{(abcde) + (abge)}{1 - (bj + gh + cdh + di + f) + bjdi + bjf}$$

Therefore, the transfer function is -

$$T = \frac{C(s)}{R(s)} = \frac{(abcde) + (abge)}{1 - (bj + gh + cdh + di + f) + bjdi + bjf}$$







