



SNS COLLEGE OF TECHNOLOGY

Coimbatore – 35

An Autonomous Institution

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade

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DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING

19ECT311 / Wireless Communication

III ECE/ VI SEMESTER

Unit II - **MOBILE RADIO PROPAGATION**

Topic 3 : REFLECTION – TWO RAY MODEL

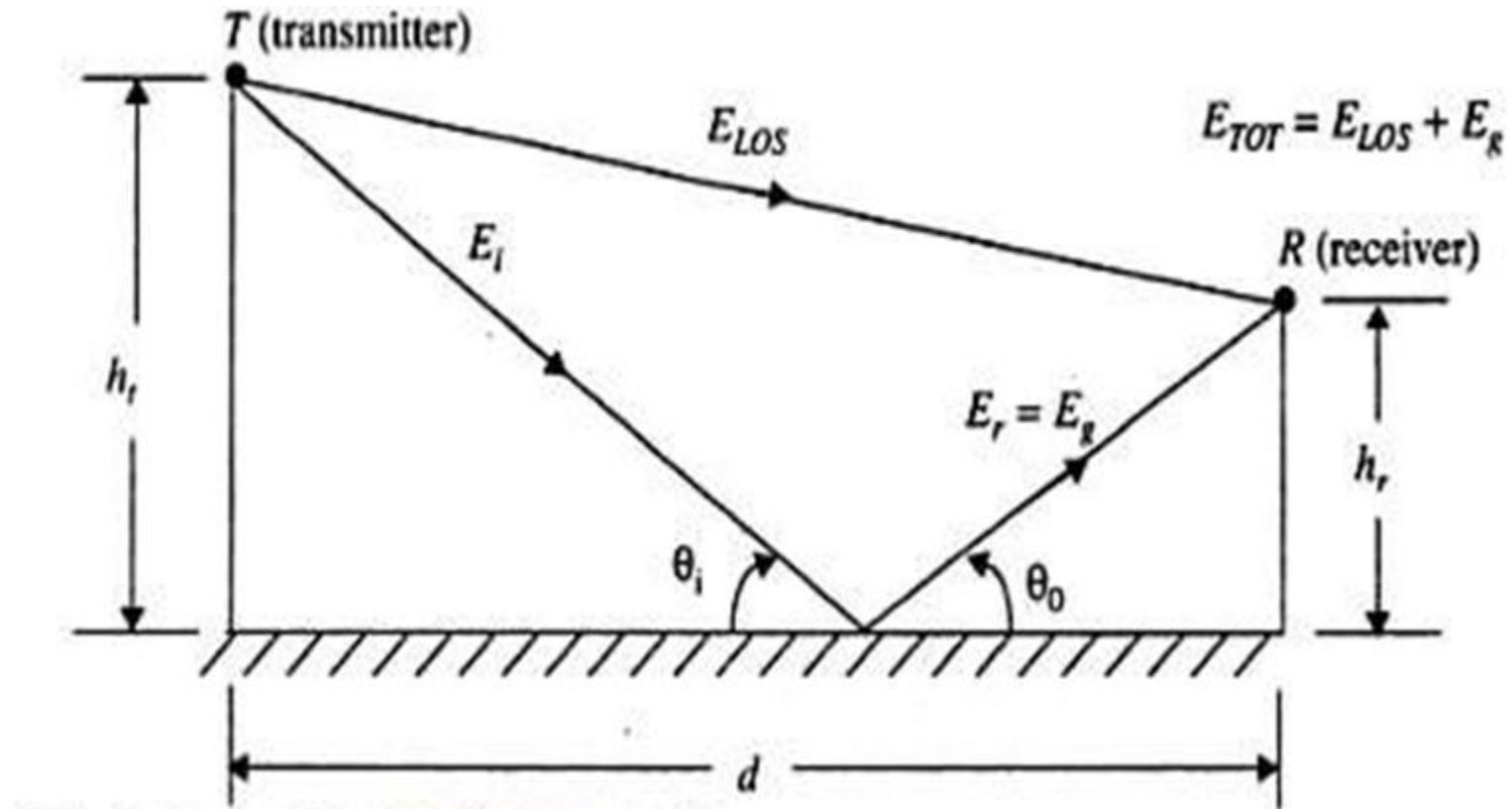


Introduction

- Free space propagation model is accurate in many cases when used alone
- Ground reflection model or Two ray model is designed for both LOS and Reflected rays
- This model is accurate for predicting the large scale signal strength over distance of several Kilometers
- The earth is assumed to be FLAT



Two ray model





E field – free Space

E Field in Free space Propagation is

$$E(d, t) = E_0 \frac{d_0}{d} \cos \left(2\pi f_c \left(t - \frac{d}{c} \right) \right)$$

Where,

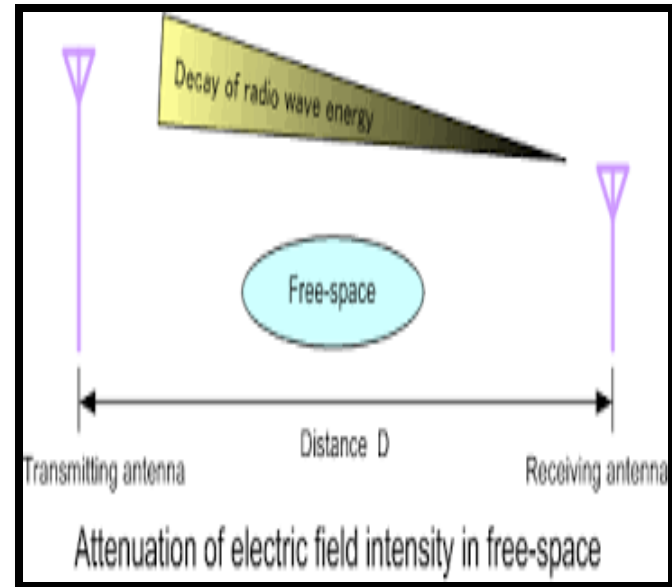
E_0 - Free Space E Field

d_0 - Reference Distance

Considering,

ht - Transmitting antenna height

hr - Receiving antenna height





E field- LOS path

E Field in Line of Sight path is

$$E_{LOS}(d', t) = \frac{E_0 d_0}{d'} \cos\left(\omega_c\left(t - \frac{d'}{c}\right)\right)$$

Where,

d' - Separation distance in the ground

C - Speed of light in vacuum

ω_c - Carrier frequency

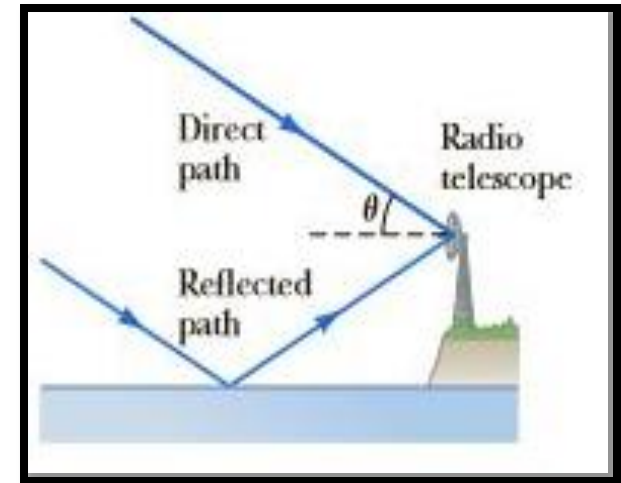




E field- reflected path

E Field in reflected path is

$$E_s(d'', t) = \Gamma \frac{E_0 d_0}{d''} \cos\left(\omega_c \left(t - \frac{d''}{c}\right)\right)$$

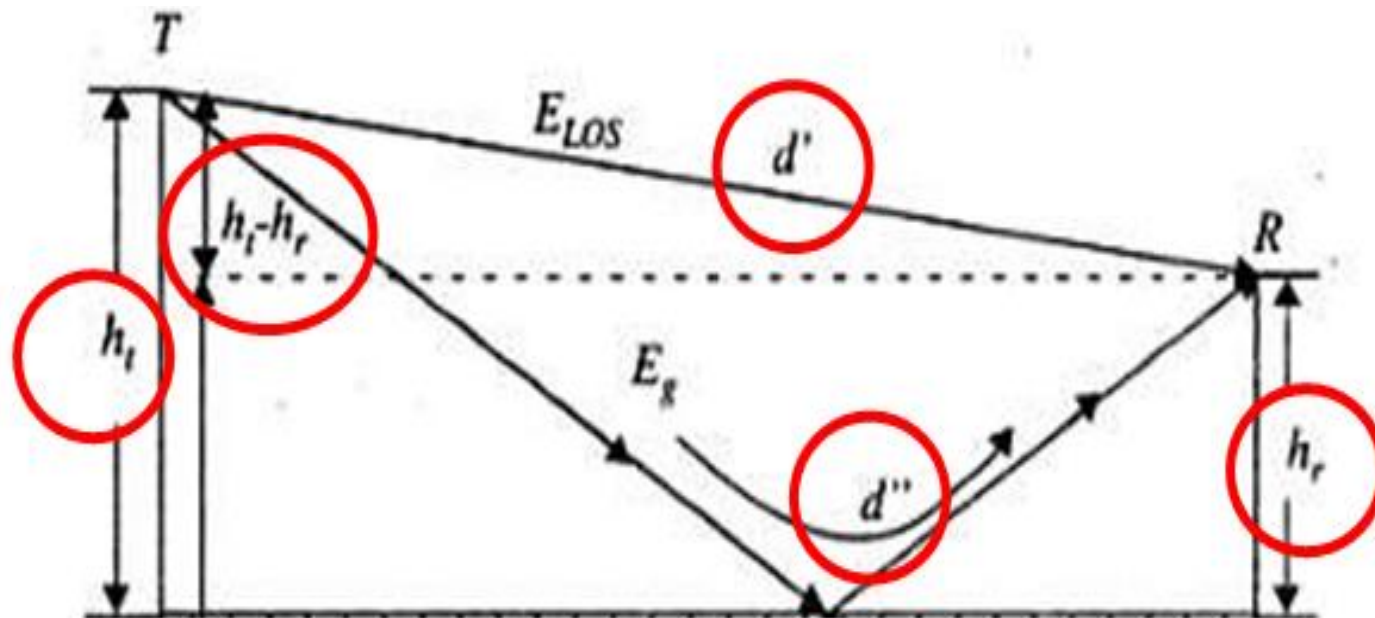


Where,

- d'' - Separation distance in the reflected path
- C - Speed of light in vacuum
- ω_c - Carrier frequency
- Γ - Reflection coefficient



Two paths





ACTIVITY



- Recall the incident happened during last birthday for those who wear red colour wardrobe.



Total Electric field

E Field in total by considering LOS and reflected path is

$$E_{TOT}(d, t) = \frac{E_0 d_0}{d'} \cos\left(\omega_c\left(t - \frac{d'}{c}\right)\right) + (-1) \frac{E_0 d_0}{d''} \cos\left(\omega_c\left(t - \frac{d''}{c}\right)\right)$$

$$\Gamma_{\perp} = -1$$

Where,

- d - Distance in the ground
- C - Speed of light in vacuum
- ω_c - Carrier frequency
- d_0 - reference point
- d' - Separation distance in the ground
- d'' - Separation distance in the reflected path



The diagram shows a cross-section of a two-layer medium. The top layer has a height of h_t and the bottom layer has a height of h_b . The total height is $h_t + h_r$. A laser beam is emitted from a source T at the top left and is received at a receiver R at the top right. The beam path is shown as a solid line with arrows, reflecting off the interface between the two layers. The distance from T to the reflection point is d' , and the distance from the reflection point to R is d'' . The total distance from T to R is d . The angle of incidence is labeled E_{LOS} and the angle of reflection is labeled E_g . The diagram also shows dashed lines representing the virtual path and the horizontal distances.

$$\begin{aligned} \triangle abc \\ bc &= d'' \\ d'' &= \sqrt{(h_t + h_r)^2 + d^2} \\ \triangle a'b'c' \\ b'c' &= d' \\ d' &= \sqrt{(h_t - h_r)^2 + d^2} \end{aligned}$$



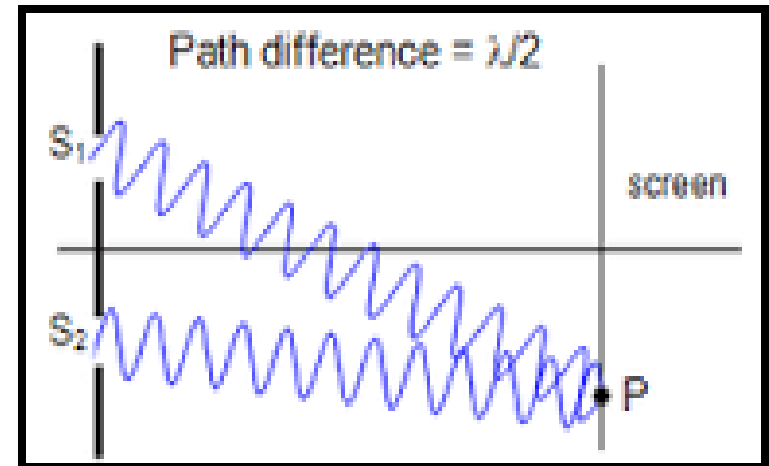
Method of images

Path difference Δ is

$$\Delta = d'' - d' = \sqrt{(h_t + h_r)^2 + d^2} - \sqrt{(h_t - h_r)^2 + d^2}$$

- When T-R Separation is very large compared to $h_t + h_r$ the equation can be simplified by using **Taylor's series approximation**

$$\Delta = d'' - d' \approx \frac{2h_t h_r}{d}$$



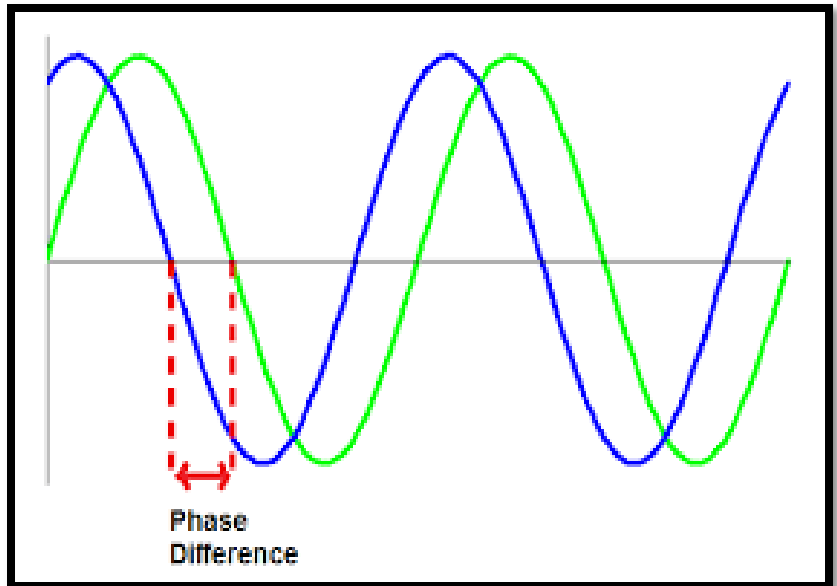


Method of images

- Once the path difference is known,
The **Phase Difference** between the two E Field Components and **Time Delay** between the arrival of the two components can be computed

$$\theta_{\Delta} = \frac{2\pi\Delta}{\lambda} = \frac{\Delta\omega_c}{c}$$

$$\tau_d = \frac{\Delta}{c} = \frac{\theta_{\Delta}}{2\pi f_c}$$





LOS Vs Reflected path

- When “d” becomes larger and larger the differences between the d' and d” becomes very small.
- In this case the amplitude levels of both LOS and Reflected Rays are virtually identical.

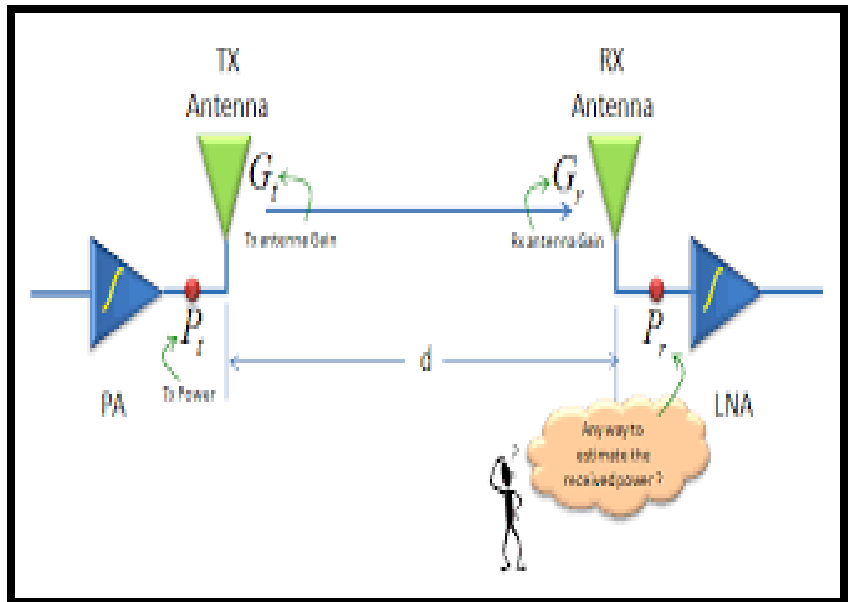
$$\left| \frac{E_0 d_0}{d} \right| \approx \left| \frac{E_0 d_0}{d'} \right| \approx \left| \frac{E_0 d_0}{d''} \right|$$



Received Power, Path Loss

- Received power at the distance d from the transmitter for the two ray model is given by:

$$P_r = P_t G_t G_r \frac{h_t^2 h_r^2}{d^4}$$



- The **Path Loss** is Defined as:

$$PL(\text{dB}) = 40\log d - (10\log G_t + 10\log G_r + 20\log h_t + 20\log h_r)$$



Assessment



1. What does path loss exponent indicates?

- a) Rate at which path loss decreases with distance
- b) Rate at which path loss increases with distance
- c) Rate at which path loss decreases with power density
- d) Rate at which path loss increases with power density

2. Difference between the direct path and the diffracted path is called _____

- a) Average loss
- b) Radio path loss
- c) Excess path loss
- d) Wavelength

