



# **SNS COLLEGE OF TECHNOLOGY**

## **An Autonomous Institution**

### **Coimbatore-35**



Accredited by NBA - AICTE and Accredited by NAAC - UGC with 'A+' Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

## **DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING**

### **19ECB212 – DIGITAL SIGNAL PROCESSING**

**II YEAR/ IV SEMESTER**

### **UNIT 1 – DISCRETE FOURIER TRANSFORM**

**TOPIC – Circular Convolution**



## EMPATHY



1

- Convolution of Periodic signal using Linear convolution is repetitive

2

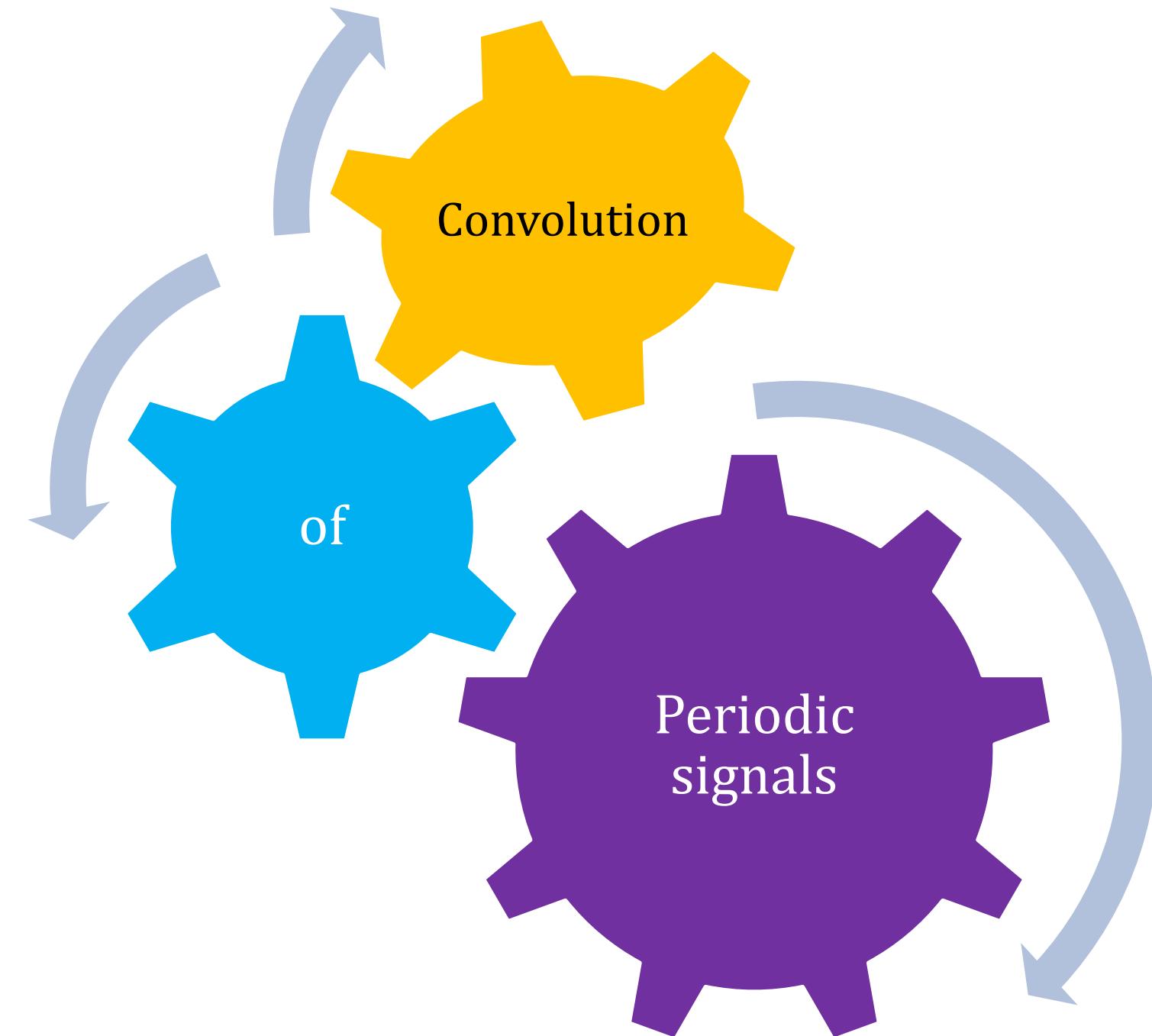
- Convolution takes lot of time

3

- Utilization of DFT for Convolution

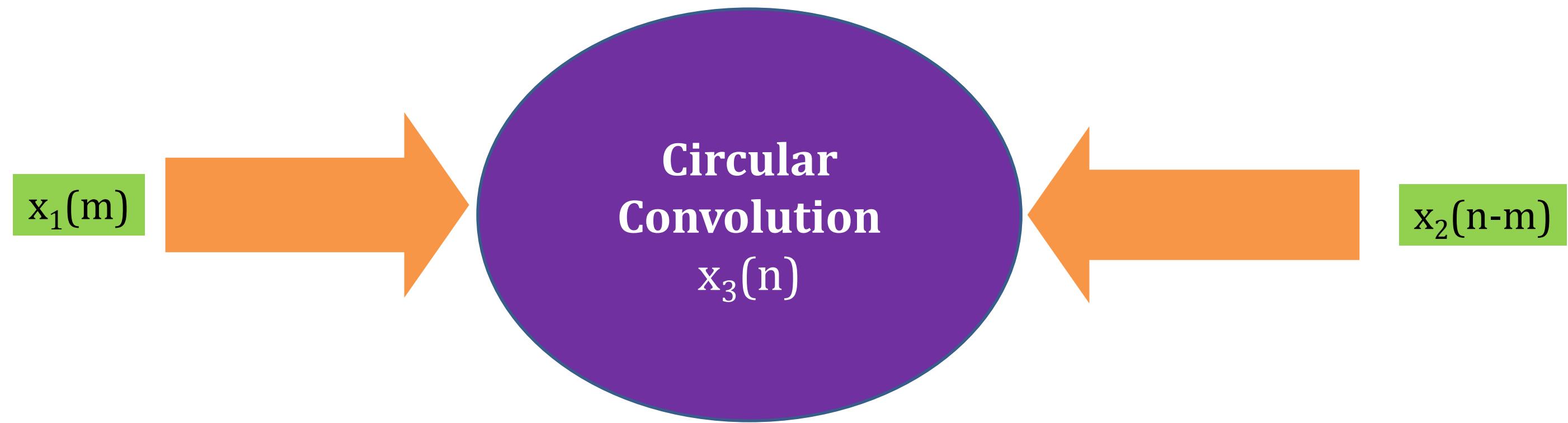


## DEFINE



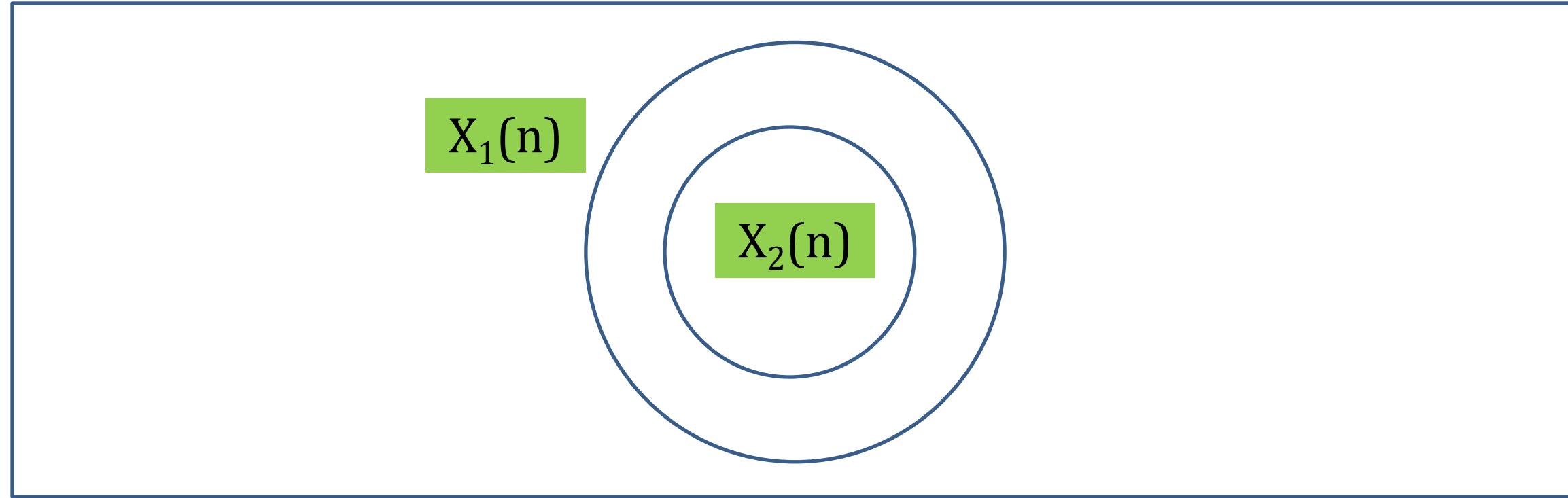


## METHOD





## NEED FOR CONVOLUTION



- To find the output of a system with input and impulse response of the system linear convolution is used
- Circular Convolution can be applied for periodic signals and to obtain linear Convolution through Circular padding of zeros are done



## CIRCULAR CONVOLUTION



- The circular convolution of two periodic discrete time sequences

$X_1(n)$  and  $X_2(n)$  with periodicity of  $N$  sample is defined as

$$y(n) = x(n) * h(n) = \sum_{k=0}^{N-1} x(k)h(n-k) \quad x_3(n) = \sum_{m=0}^{N-1} x_1(m)x_2[((n-m))_N]$$

- If  $x(n)$  and  $h(n)$  two finite duration signals with length  $M$  and  $P$  respectively then the length of  $y(n) = x(n) * h(n)$  is  $\mathbf{N=M+P-1}$  samples



## CIRCULAR CONVOLUTION



- If  $x(n)$  and  $h(n)$  two periodic signals with period  $N$  then the length of  $y(n) = x(n) \circledast h(n)$  is also  $N$
- The convolution of two periodic signal is also periodic and is circular convolution.

$$y(n) = x(n) \circledast h(n)$$

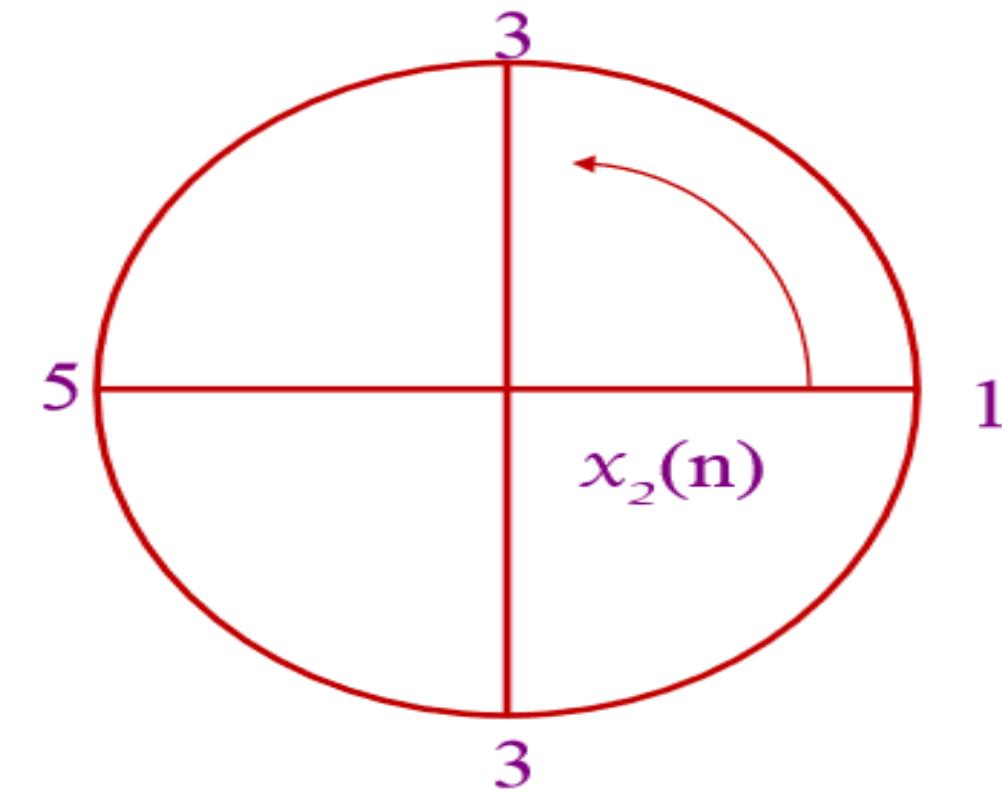
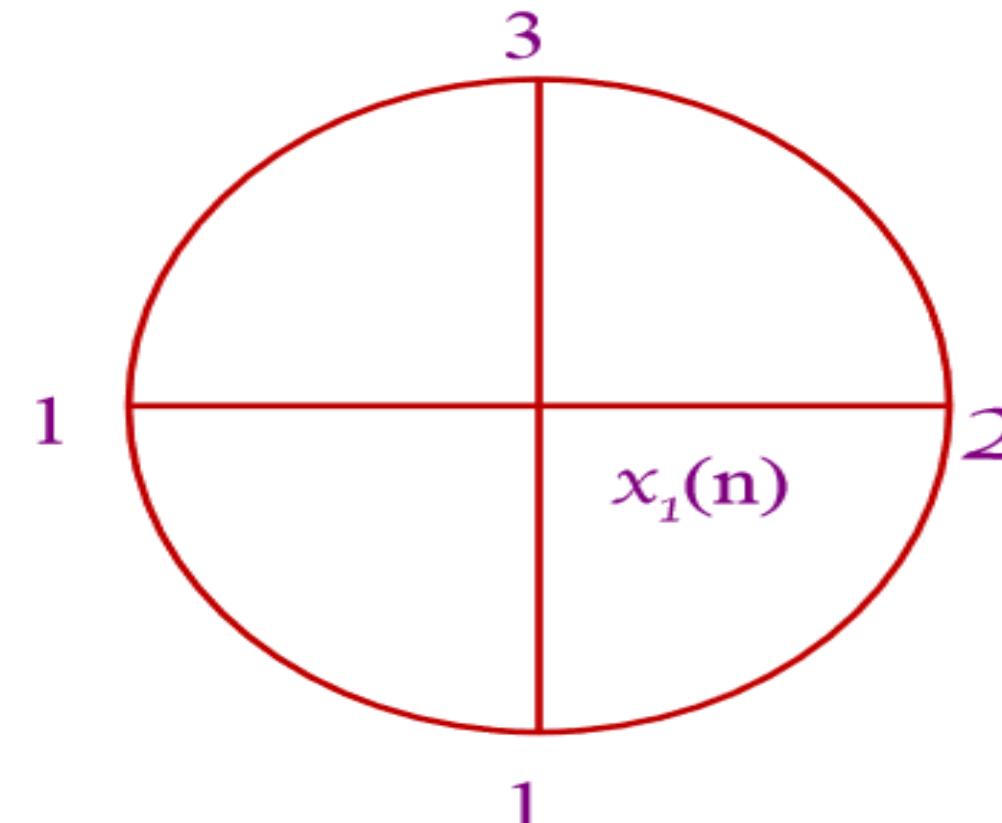
- Linear Convolution can be obtained by circular convolution by changing the length of both signals  $x(n)$  and  $h(n)$  to  $N$  by zero padding



## CIRCULAR CONVOLUTION



- Compute the circular convolution using time domain approach for the following sequence:  $X_1(n) = \{2,3,1,1\}$  and  $X_2(n) = \{1,3,5,3\}$



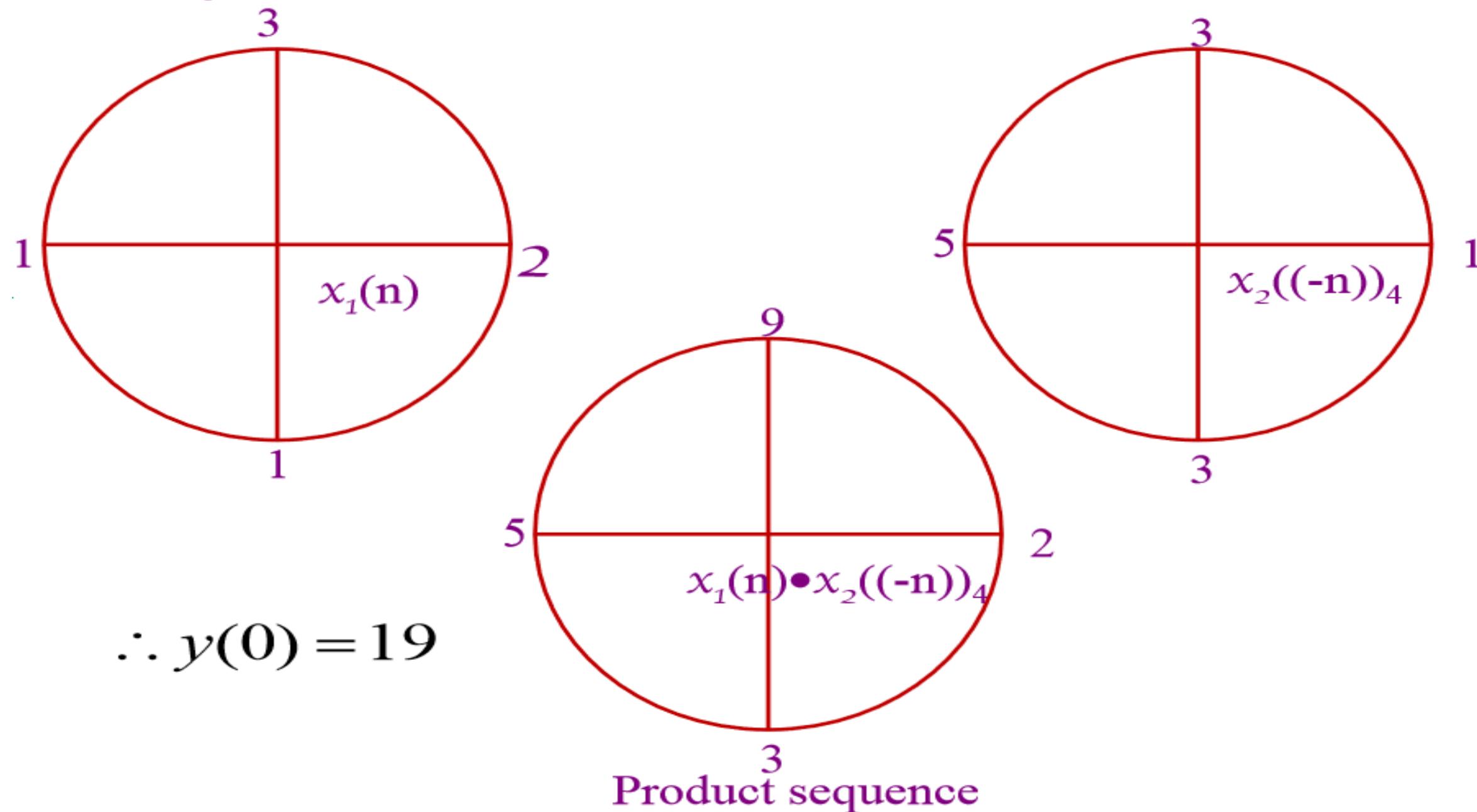
$$y(n) = \sum_{k=0}^{N-1} x_1(k) \cdot x_2(n-k) = \sum_{k=0}^3 x_1(k) \cdot x_2(n-k)$$



## CIRCULAR CONVOLUTION

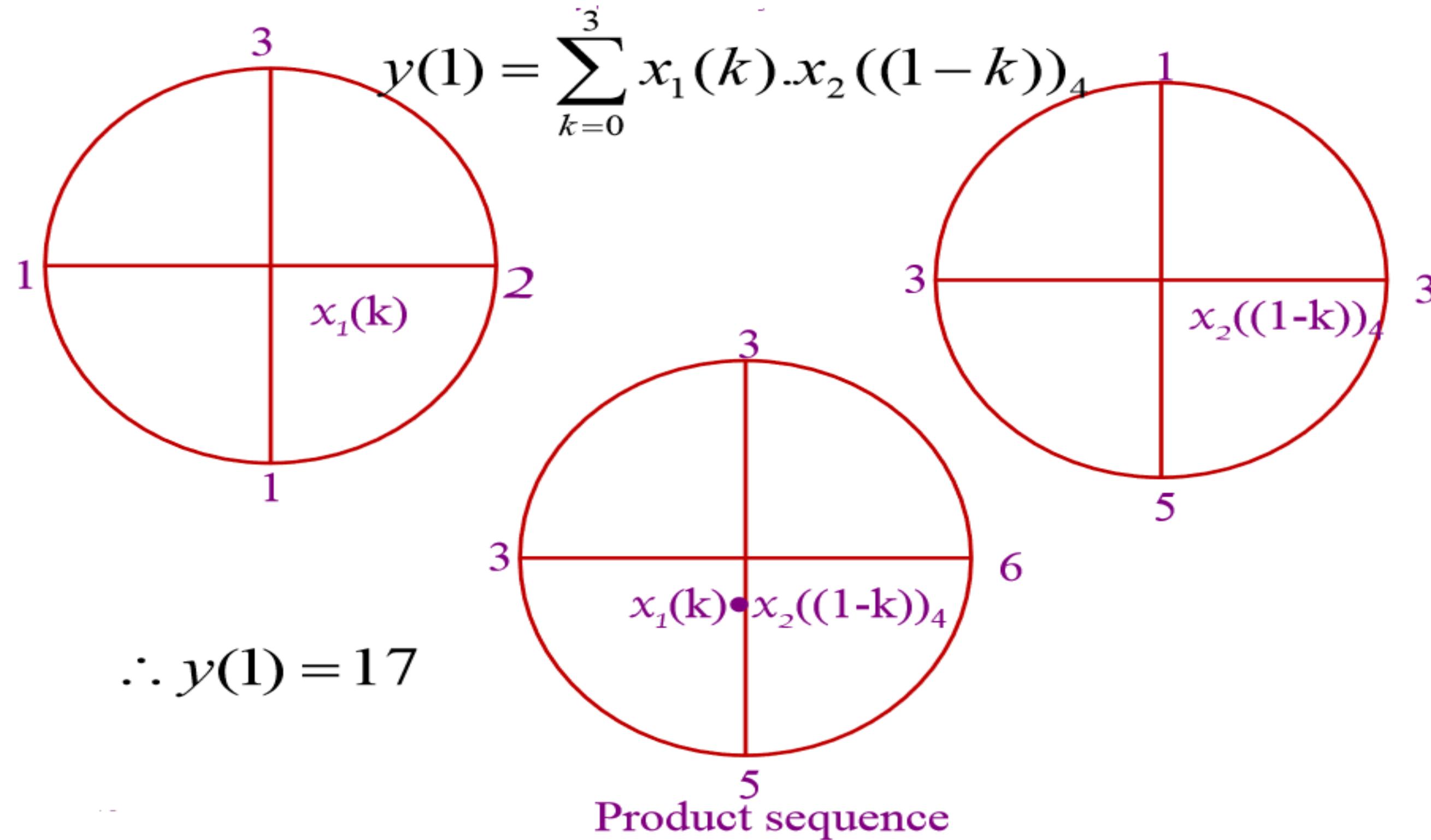


$$y(0) = \sum_{k=0}^3 x_1(k) \cdot x_2(-k)$$



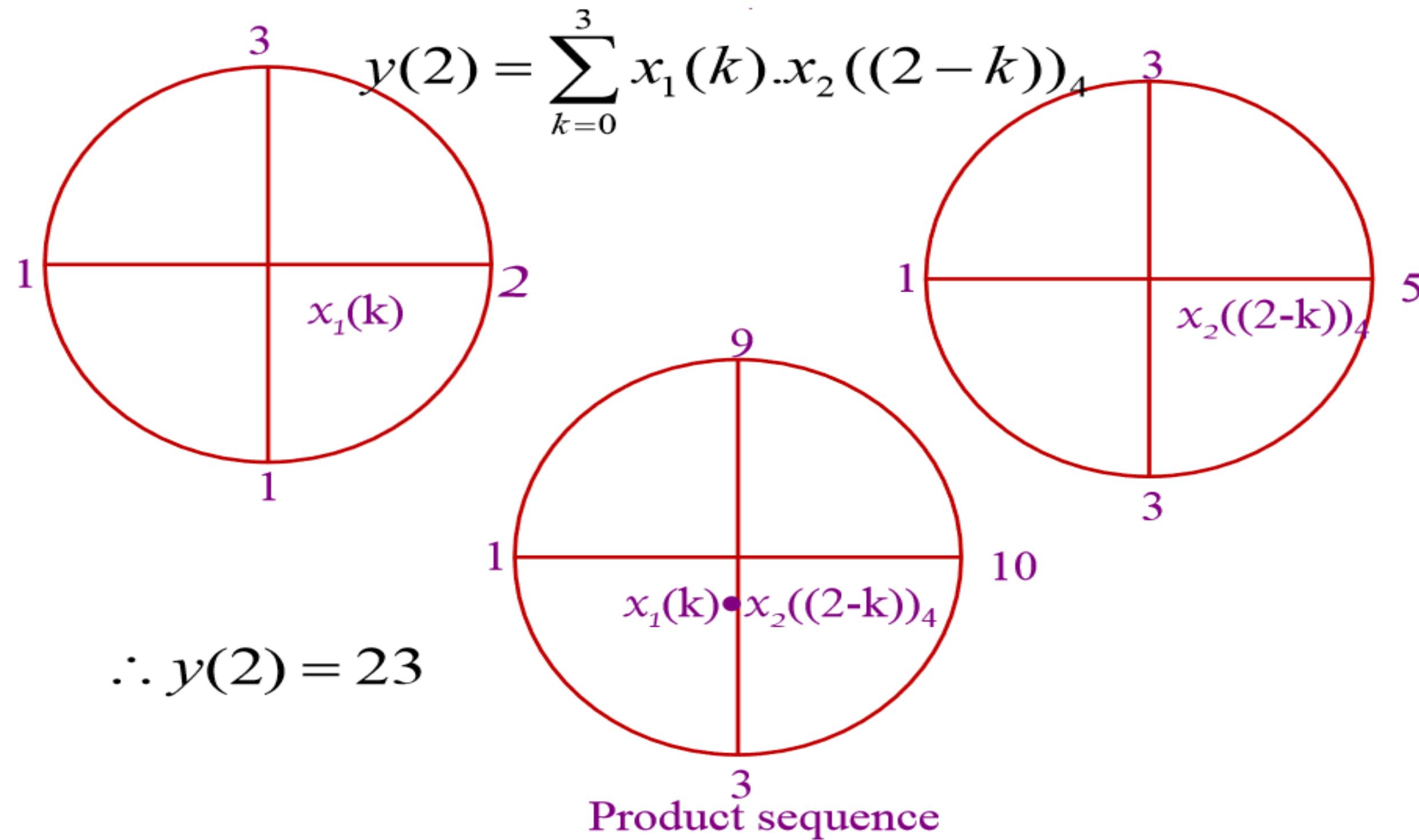


## CIRCULAR CONVOLUTION



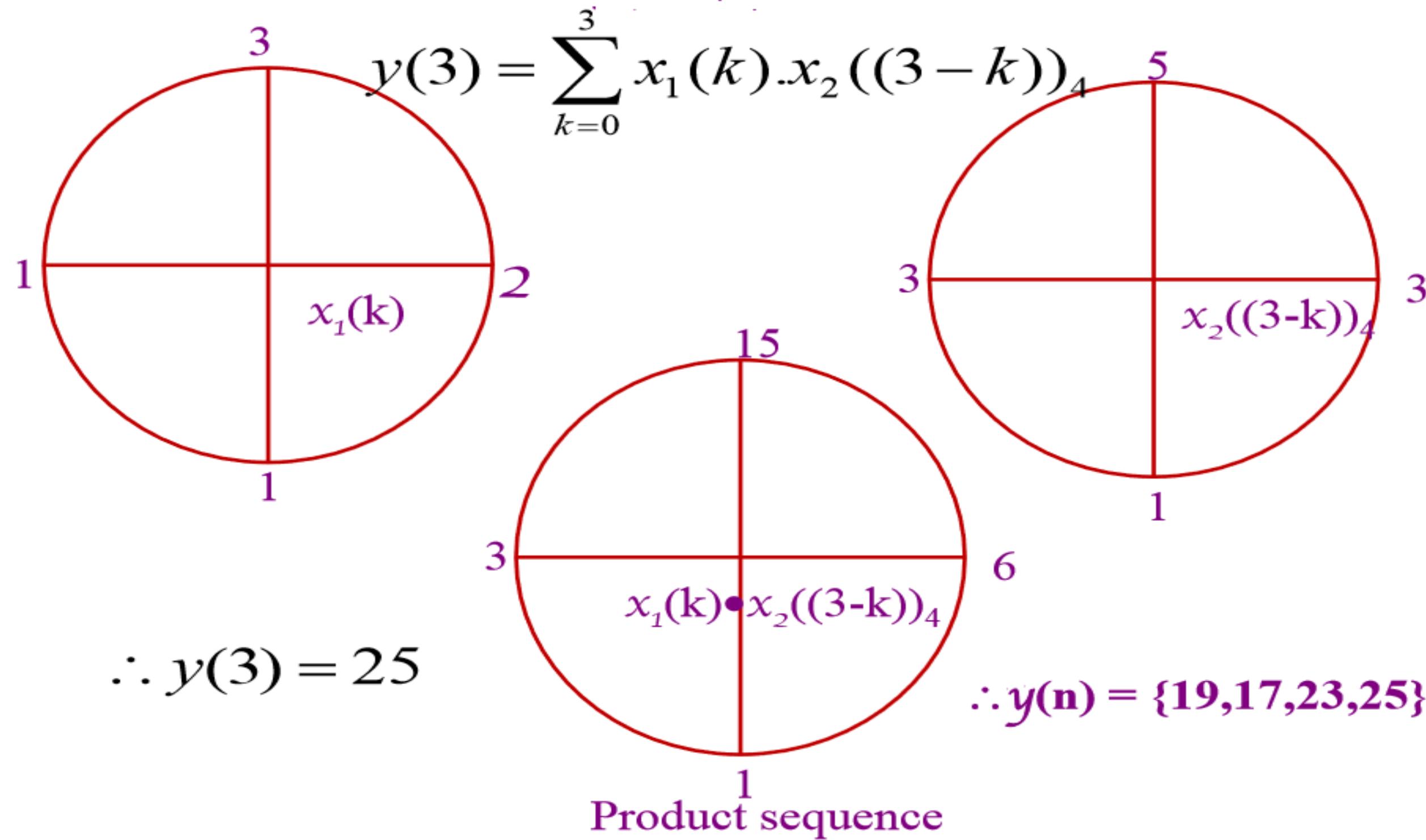


## CIRCULAR CONVOLUTION





## CIRCULAR CONVOLUTION





## CIRCULAR CONVOLUTION – MATRIX APPROACH



$$y[n] = \begin{bmatrix} h(0) & h(N-1) & .. & h(1) \\ h(1) & h(0) & .. & h(2) \\ \vdots & \vdots & .. & \vdots \\ h(N-1) & h(N-2) & .. & h(0) \end{bmatrix} \begin{bmatrix} x(0) \\ x(1) \\ \vdots \\ x(N-1) \end{bmatrix}$$

e.g.  $h(n) = \{2,3,1,1\}$  and  $x(n) = \{1,3,5,3\}$

$$\therefore y[n] = \begin{bmatrix} 2 & 1 & 1 & 3 \\ 3 & 2 & 1 & 1 \\ 1 & 3 & 2 & 1 \\ 1 & 1 & 3 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 3 \\ 5 \\ 3 \end{bmatrix}$$

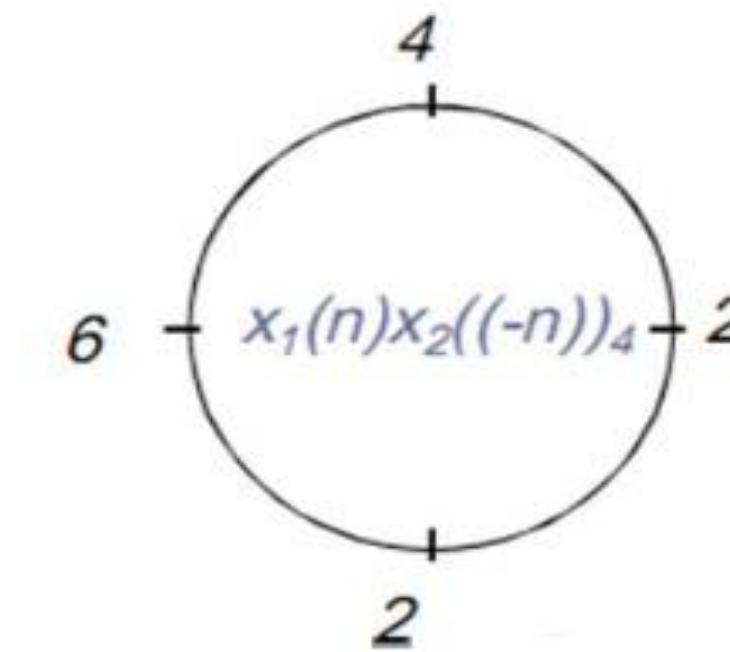
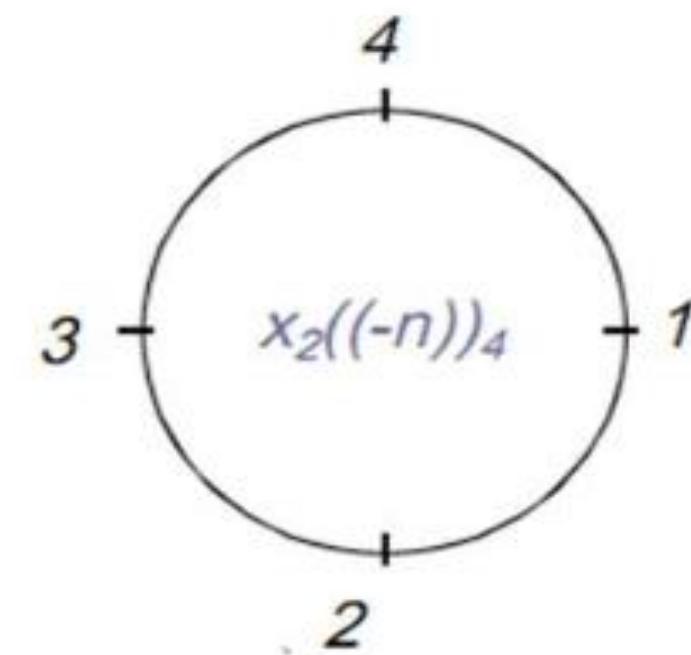
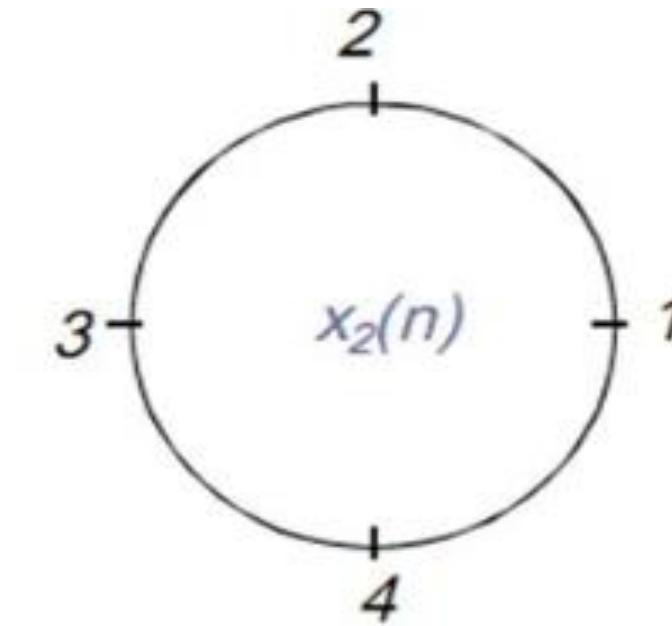
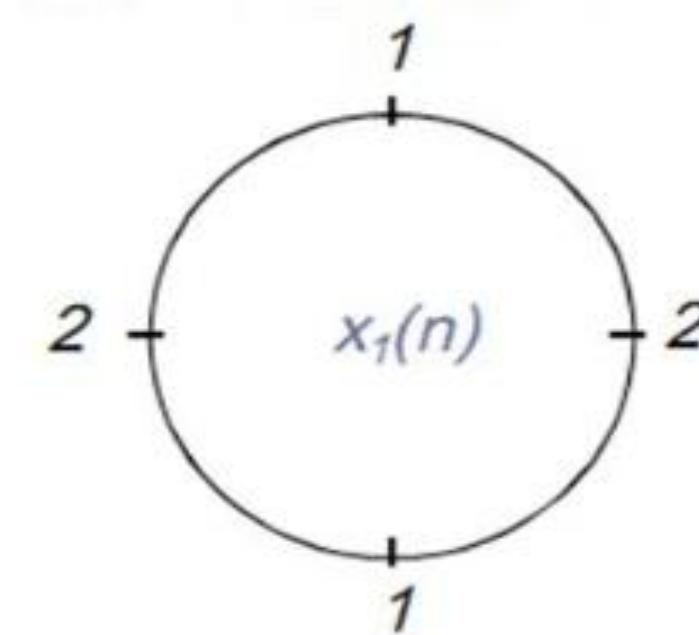
$$\therefore y[n] = \begin{bmatrix} 2+3+5+9 \\ 3+6+5+3 \\ 1+9+10+3 \\ 1+3+15+6 \end{bmatrix} = \begin{bmatrix} 19 \\ 17 \\ 23 \\ 25 \end{bmatrix}$$



## CIRCULAR CONVOLUTION

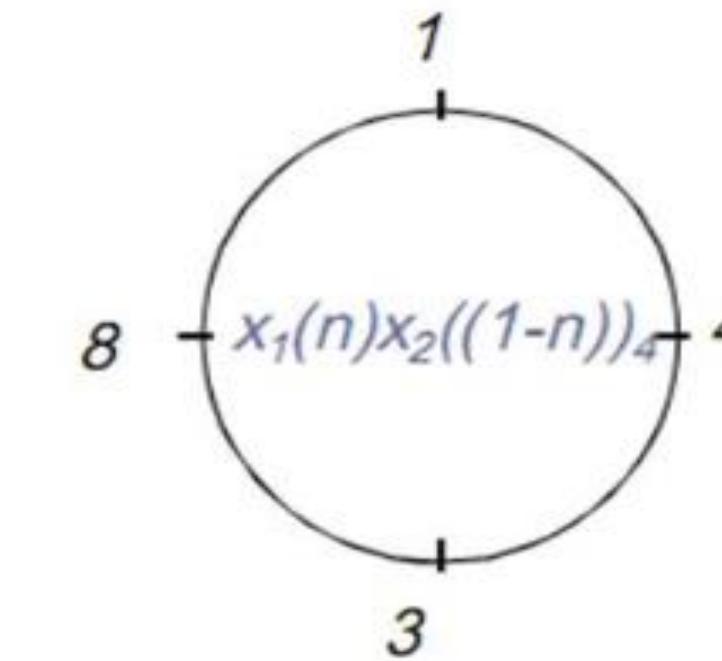
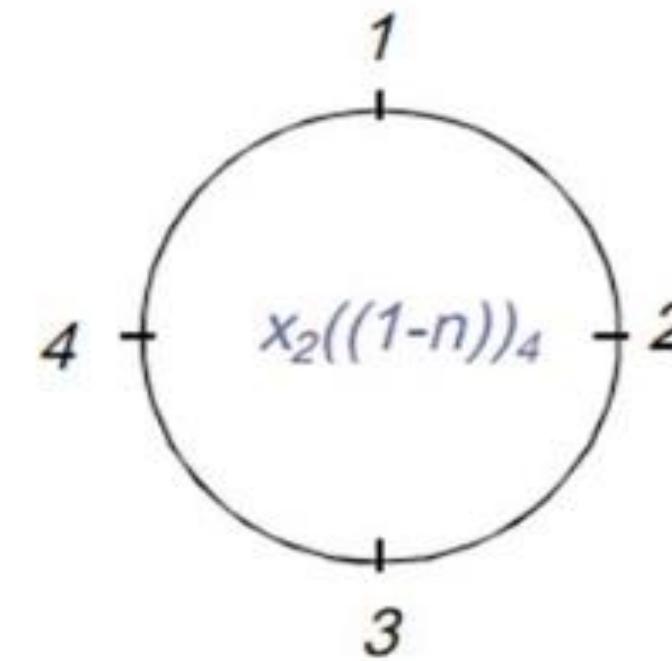
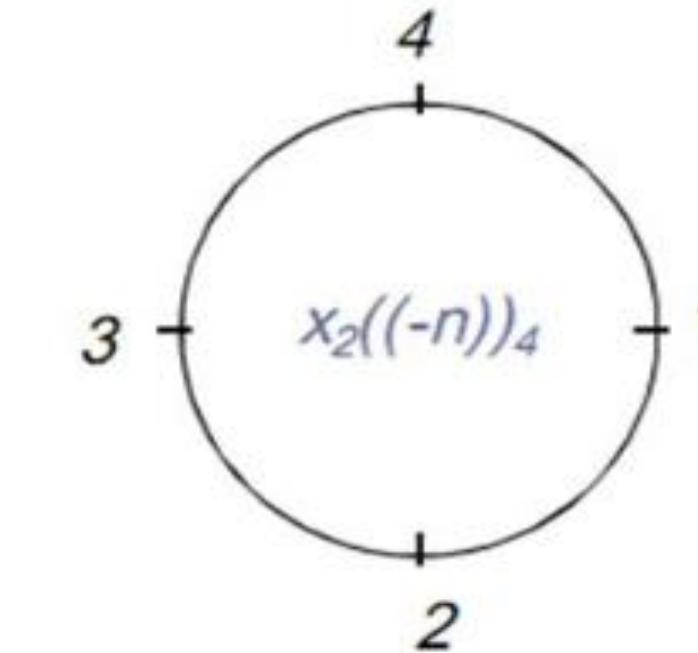
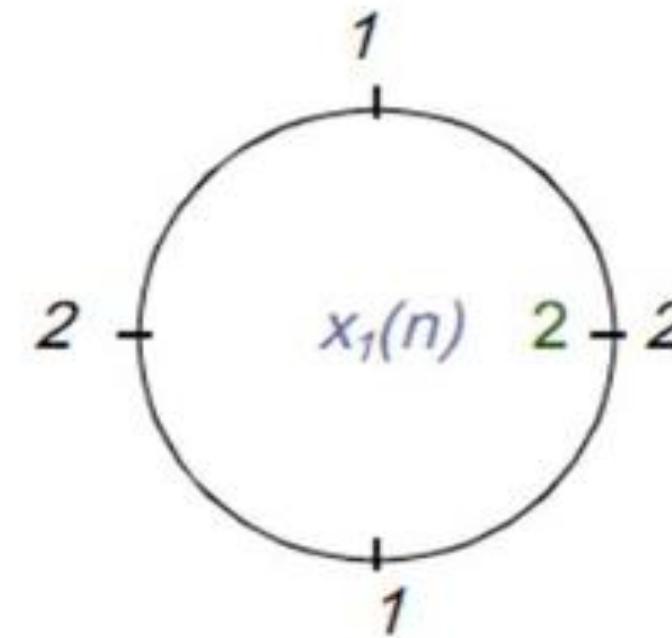


Perform circular convolution  $X_1(n) = \{2,1,2,1\}$  and  $X_2(n) = \{1,2,3,4\}$



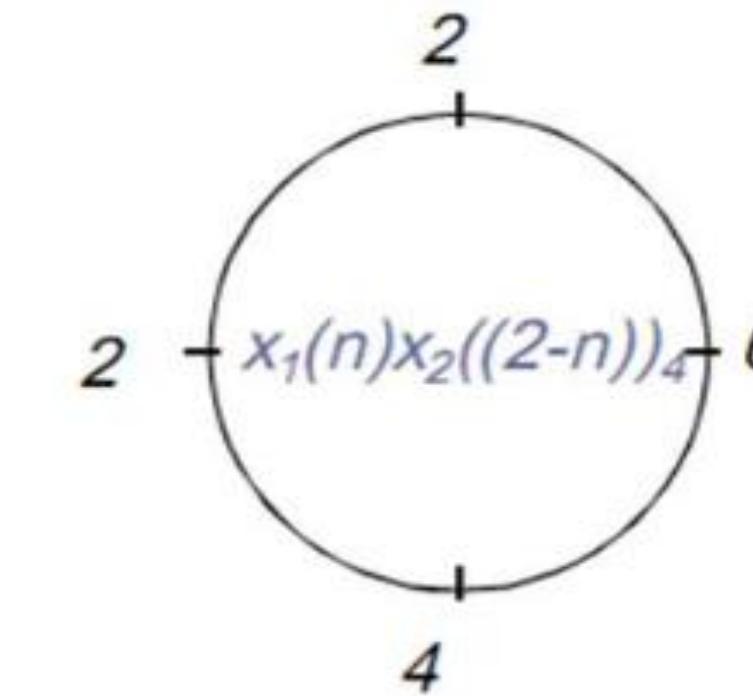
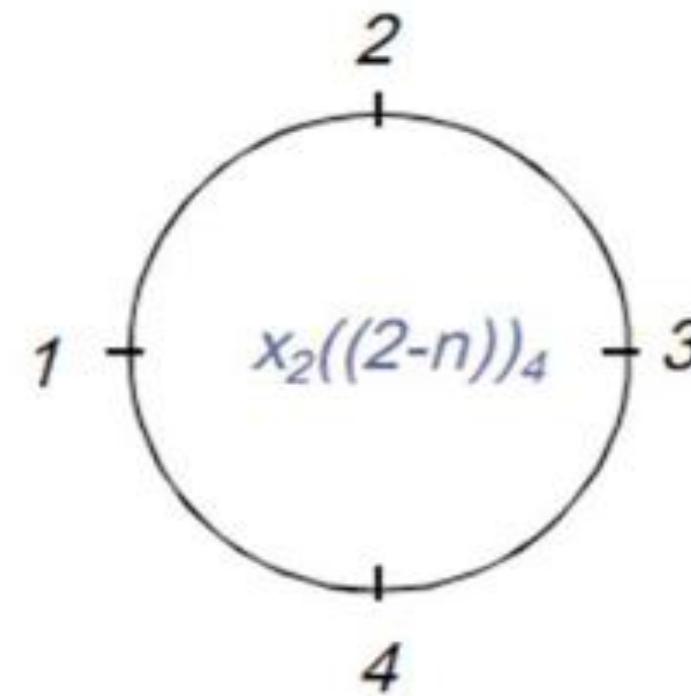
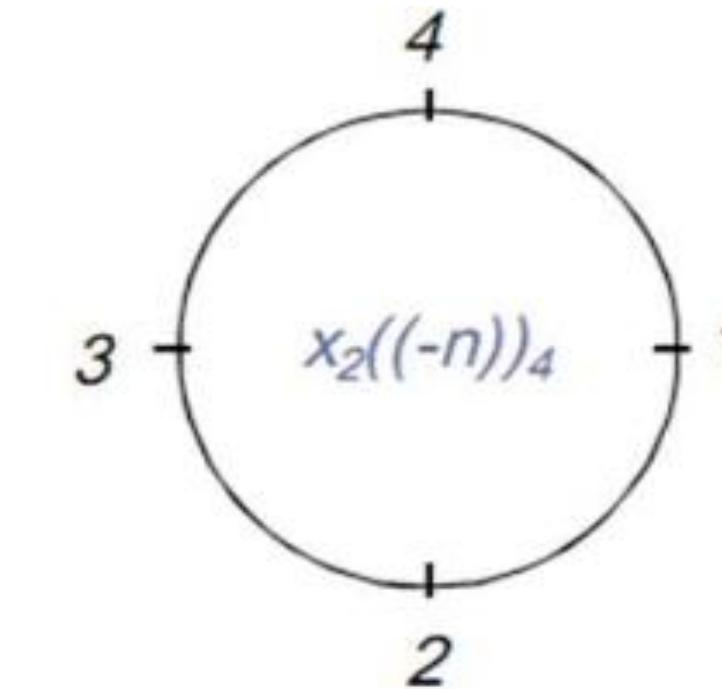
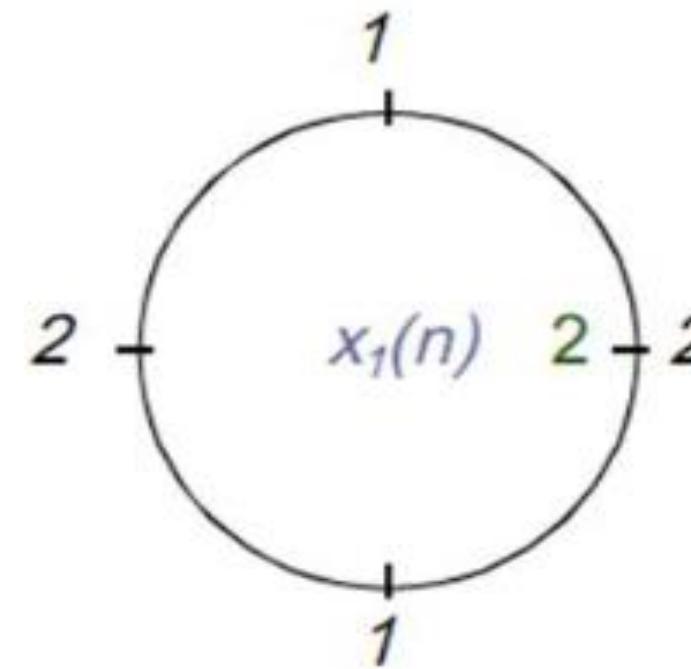


## CIRCULAR CONVOLUTION



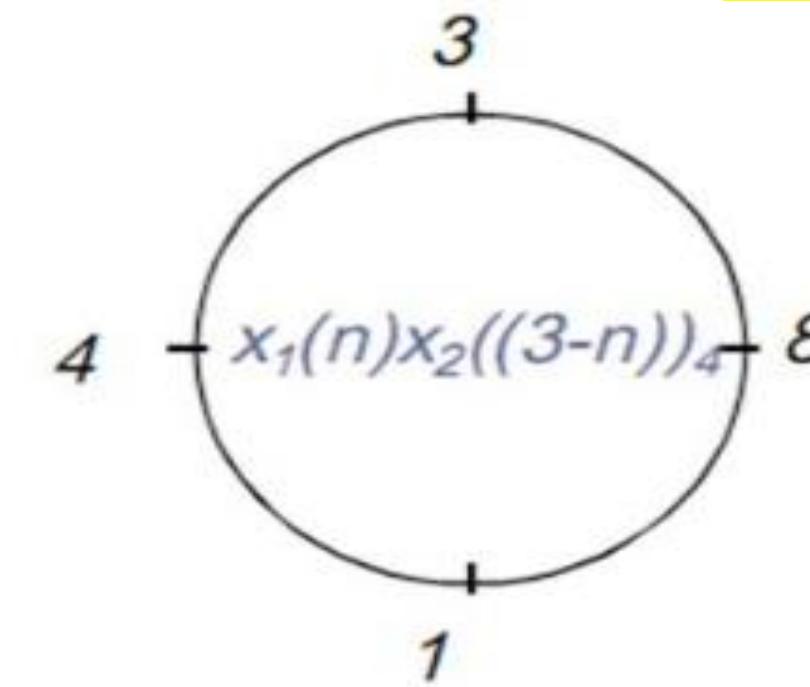
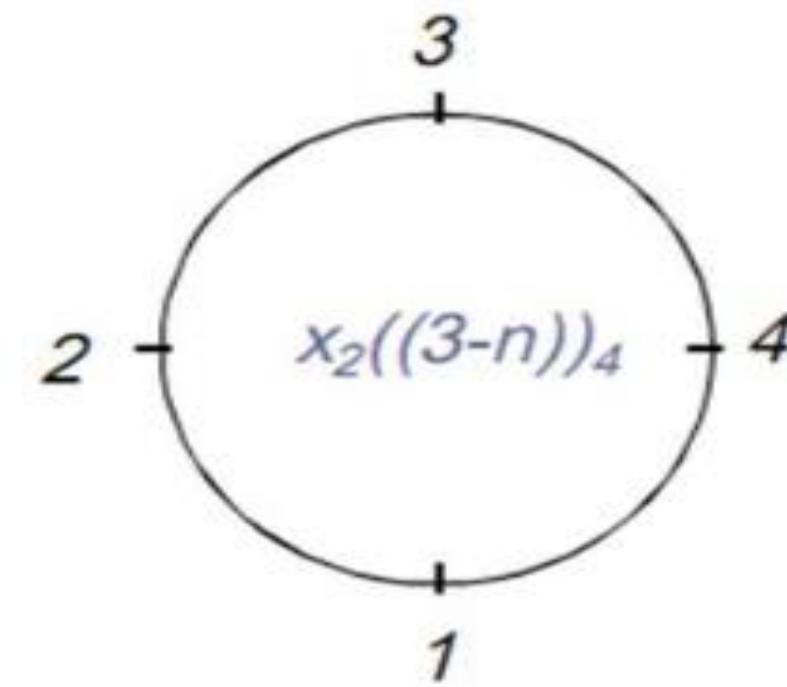
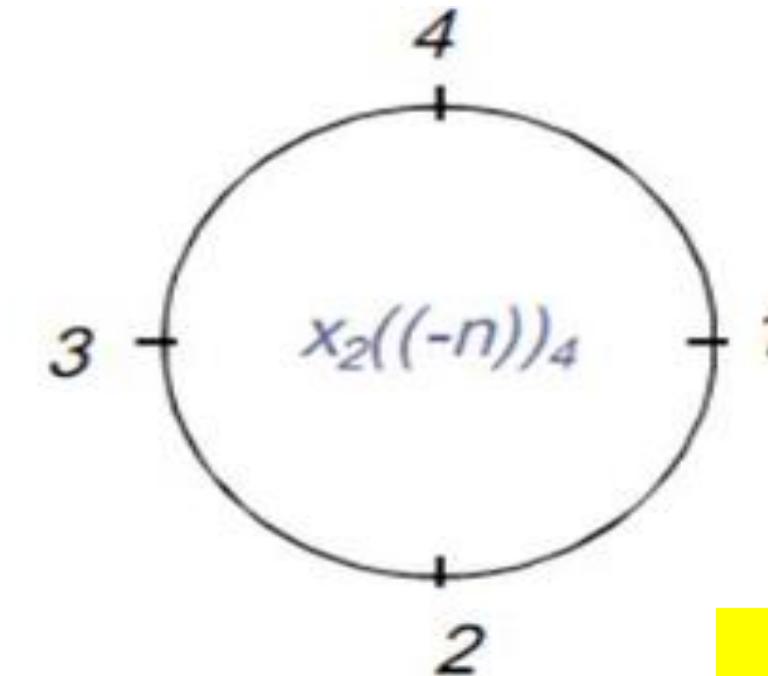
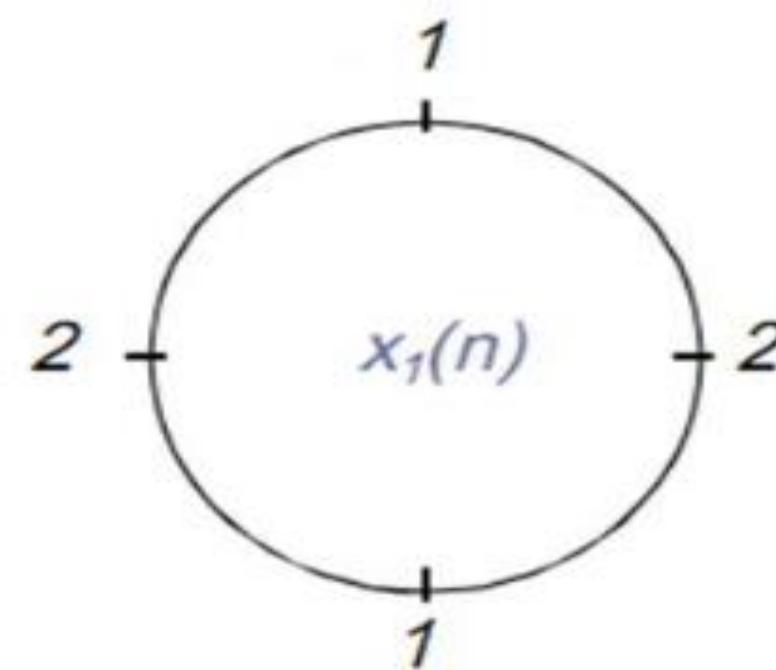


## CIRCULAR CONVOLUTION





## CIRCULAR CONVOLUTION



$$y(n) = \{14, 16, 14, 16\}$$

$$x_3(3) = 16$$



## DIFFERENCE B/W LINEAR & CIRCULAR CONVOLUTION



S.No.	Linear Convolution	Circular Convolution
1	In case of convolution two signal sequences input signal $x(n)$ and impulse response $h(n)$ given by the same system, circular convolution. output $y(n)$ is calculated	Multiplication of two DFT s is called as
2	Multiplication of two sequences in time domain is called as Linear convolution	Multiplication of two sequences in frequency domain is called as circular convolution.
3	Linear Convolution of two signals returns $N-1$ elements where $N$ is sum of elements in both sequences.	Circular convolution returns same number of elements that of two signals.
4	$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$	$x_3(n) = \sum_{m=0}^{N-1} x_1(m)x_2[((n-m))_N]$



# ASSESSMENT



1. Define Circular Convolution.
  
2. If  $x(n)$  and  $h(n)$  two finite duration signals with length  $M$  and  $P$  respectively then  
the length of  $y(n) = x(n) * h(n)$  is ----- samples
  
3. Mention some applications of Circular Convolution.
  
4. Determine circular convolution of  $X_1(n) = \{2,1,2,1\}$  and  $X_2(n) = \{1,2,3,4\}$
  
5. What is the difference between linear convolution and circular convolution.



# THANK YOU