



DEPARTMENT OF MECHANICAL ENGINEERING

19MEB302/ Heat and Mass Transfer – UNIT I - CONDUCTION Topic - One Dimensional Steady State Heat Conduction through Plane Wall

Conduction heat transfer:

Objectives of conduction analysis:

1) Primary objective is to determine the temperature field T(a) in a body (ie how temperature varies with position within the body

2) T(20) depends on boundary condition, initial condition, material properties (P, K, Cp), and geometry.

> Why we need temperature T(x). as Compute heat flux at any point (ung Forme by compute thermal strenes, expansion, deflection due to temp etc,

of Davign products in application such as. insulation thickness, chip temperatue calculations (electronics), Heat treatment al netali.

Boundary and Initial condition:

is Heat equation is second order in spatial coordinate. Hence, 280, needed for each coordinate

* ID problem: 2RC m x-direction.

2) Heat equation is first order in time. Hence IIC is needed.





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One-dimensional steady state heat conduction without heat generation: q"=0, 2 =0. $\frac{3}{2}\left(k,\frac{37}{27}\right)=0. \rightarrow . k,\frac{d^{\frac{1}{7}}}{12}=0. \rightarrow 0$ £ =0. Integrating the equation once. To $\frac{dT}{dt} \cdot C_1 \rightarrow 2$ Integrating the equation again. T= C,x+C2 -> 3 To determine the constants C, & C2, apply the boundary conditions. ie @x=0, T=T, > T,=C,0+C2 > C2=T,>0 & @ x=L, T=Te -> Tz=C,L+C2 T2=GL+T, ": C2=T, .. G= (T2-T1) → 3 becomes, $T = (T_2 - T_1) \times + T_1 \rightarrow T - T_1 = \frac{1}{L} \rightarrow 6$: 3 becomes,

Temperature distribution across the place wall.





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Rate of heat transfer through the plane wall: $Q := -KA \cdot dT \longrightarrow \widehat{T}$ [Fourier conduction equation] $Q := -K \cdot A \cdot \frac{dT}{dx} \longrightarrow \widehat{T} \cdot \widehat{T} \cdot$

Q = (Ti-Tz) -> ®

[La]

[KA]

Thornal resistance concept was Ohn's law: V=I.R. -> I= V -> 3. V, -> V.

Comparing equations @ and @, we have.

Q=I; (T,-T2)=V and L=R.

.. Thermal resistance for the plane would.

RH= LA > (10) [W/MKK Nt = W. K. = K]

Thermal resistance circuit for plane wall.

To the Te unit to GE W.

Thermal relistance for convection from newtools los of cooling Q=hA(Ts-Tm) -> Q=(Ts-Tm)

- RIE - HAS





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Plane wall with convective boundary conditions:

The differential equation is:

Integrating twice, T(x) = C, x+ Cz.

Bounday conditions are.

Heat flux across the wall is given by

Thermal resistance concept for convection!



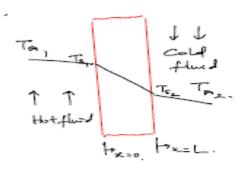


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Applying thermal resistance concept for the place wall with convection boundary conditions.



V ha V ka V ha.

Heat transfer rate may be determined by considering each element of the resistance network. as.

$$q = \frac{T_{0_1} - T_{S_1}}{h_1 A} = \frac{T_{S_1} - T_{S_2}}{h_2 A} = \frac{T_{S_2} - T_{0_2}}{h_2 A} \longrightarrow 0$$

since resistances are in series,

$$R_{total} = \leq R_{th} = \frac{1}{h_{i,A}} + \frac{L}{kA} + \frac{1}{h_{i,A}} \longrightarrow 2$$

$$= \frac{T_{0i,-}T_{2i}}{9i} + \frac{T_{2,-}T_{0i,2}}{9i} + \frac{T_{2,-}T_{0i,2}}{9i}$$