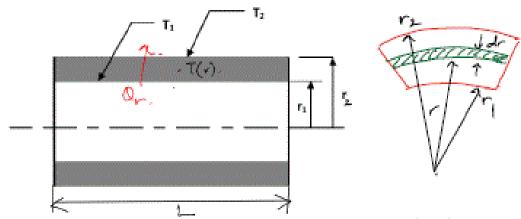




### **DEPARTMENT OF MECHANICAL ENGINEERING**

16ME306/ Heat and Mass Transfer – **UNIT I - CONDUCTION**Topic - Cylinders, Spherical systems

One dimensional conduction equation for cylinder.



In cylindrical coordinates, the conduction early state with no heat generation;

For k= constant, above equations can be;  $\frac{d}{dr}\left(r,\frac{dT}{dr}\right)=0 \longrightarrow 0$ 

Integrating once, we get  $r.\frac{dT}{dr} = C_1$ 

dT · C1 -> 2

Further integration gives;

T(r) = C Inr+C2 -> (3) [ Temp distribution].

Bounday @r=r, T(r)=T, Condition @r=r2, T(r)=T2.





#### **DEPARTMENT OF MECHANICAL ENGINEERING**

16ME306/ Heat and Mass Transfer — **UNIT I - CONDUCTION**Topic - Cylinders, Spherical systems

substituting there BCs in eqn @, we get. Ti= Cilnn+C2 -> (9) T20 C, In. 7, +C2 -> 6 Solve for constants C, &C2. 3-0, (t2-T,)= C, (ln r2-ln r,) L',  $C_1 = \frac{(T_2 - T_1)}{|v(\frac{r_1}{r_1})|} \rightarrow 0$ Substitute G' in equation ( we get. Ti = (Ta-Ti) Inr,+C2 -: C2 = T, - (T2-T1) lnr, -> (7) Substitute for G25 in equation 3, reget  $T(r) = \frac{\left(T_{2} - T_{1}\right) \ln r + T_{1} - \left(T_{2} - T_{1}\right) \ln r}{\ln \left(\frac{r_{2}}{r_{1}}\right)} \ln r + T_{1} - \frac{\left(T_{2} - T_{1}\right) \ln r}{\ln \left(\frac{r_{2}}{r_{1}}\right)} \ln r}$   $\frac{T(r) - T_{1}}{T_{2} - T_{1}} = \frac{\ln \left(\frac{r_{2}}{r_{1}}\right)}{\ln \left(\frac{r_{2}}{r_{1}}\right)} \rightarrow 8$ 

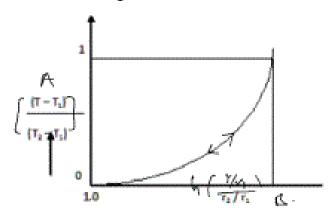




#### **DEPARTMENT OF MECHANICAL ENGINEERING**

16ME306/ Heat and Mass Transfer – UNIT I - CONDUCTION Topic - Cylinders, Spherical systems

The above equation gives the temperature distribution along the radius of the cylinder;



Expression for the rate of heat transfer.

Ar, = 2007, ( =784, (

Arz = 225/1=70

Qr=-K.27 L. (T2-T1).

Q = 2xk( (T,-T2)





#### **DEPARTMENT OF MECHANICAL ENGINEERING**

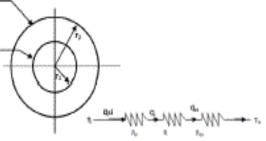
16ME306/ Heat and Mass Transfer – UNIT I - CONDUCTION Topic - Cylinders, Spherical systems

Sphere subjected to convective boundary condition

Surface in contact with fluid at T<sub>c</sub> and surface heat transfer

coefficient he

Surface in contact with fluid at T, and surface heat transfer coefficient h

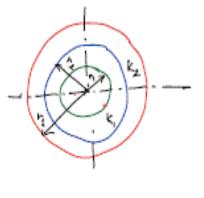


$$R_{co} = \frac{1}{h_o A_z} = \frac{1}{h_o \cdot 4\pi r_z^2}$$

$$R_{total} = R_{ci} + R + R_{co}$$

$$(T_i - T_i)$$

Composite sphere: Cover: No convection Ect. Thermal resistance circuit:



$$R_{1} = \frac{(r_{1} - r_{2})}{4\pi k_{1}}$$

$$R_{2} = \frac{(r_{2} - r_{3})}{4\pi k_{2}}$$

$$R_{3} = \frac{(r_{1} - r_{3})}{4\pi k_{2}}$$

$$R_{4} = \frac{T_{1} - T_{3}}{R_{4} + R_{2}}$$

$$R_{5} = \frac{T_{1} - T_{3}}{R_{4} + R_{2}}$$