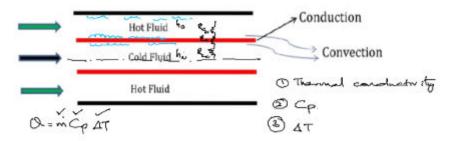




DEPARTMENT OF MECHANICAL ENGINEERING, 19MEB302/ Heat and Mass Transfer — UNIT III - PHASE CHANGE HEAT TRANSFER AND HEAT EXCHANGERS

Topic - Types of Heat Exchangers- Heat Exchanger Analysis- LMTD Method

Heat exchangers are the devices that facilitate heat transfer between two (or) more fluids. at different temperatures, while keeping them from mixing (or without mixing. Heat transfer in heat exchanger involves convection in each fluid and conduction through the wall separating the fluids.



Example: Shell and tobe theat exchanger.

Boilers.

Cooling towers

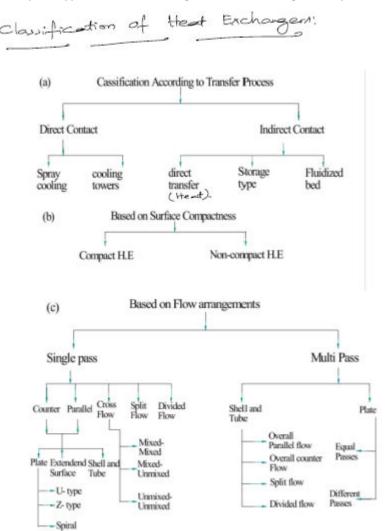
Cor radiators etc.,





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the transfer analysis of heat exchangers

To design 60 predict the performance,
the fluid temperatures, overall heat transfer
Coefficient and surface area parameters are
to be evaluated. They are modelled as.
Steady-flow devices. The wethods wed for
analysis are:

I LMTD approach (Log mean Temp difference)

1) LMTD approach (Log mean Temp difference) known -> Temperatures, Mass flow rates, overall heat transfer coefficient.

Calculate the size of the heat exchanger D', L', ey E-NTU approach! (Number of Transfer units).

Known - Either inlet (or) outlet temperatures, size.

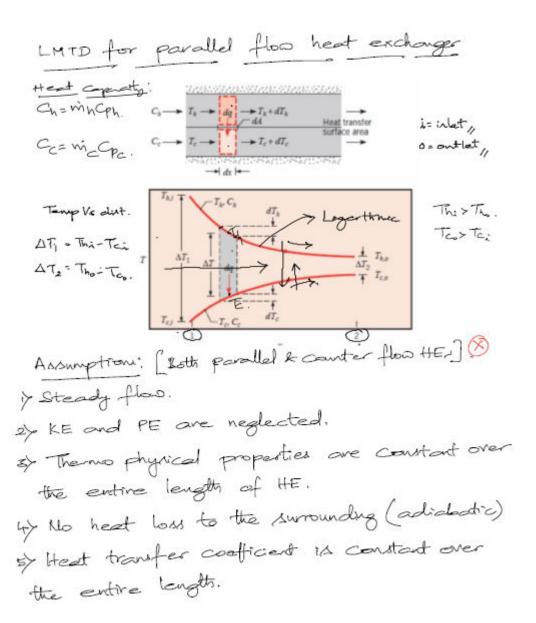
Type and size of heat exchanger.

Calculate the missing temperatures, Load on the heat exchanger.





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$\begin{tabular}{ll} \textbf{DEPARTMENT OF MECHANICAL ENGINEERING, } 19 MEB 302/ \ Heat and Mass Transfer - \textbf{UNIT III - PHASE CHANGE HEAT TRANSFER AND HEAT} \\ \end{tabular}$

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Let, As Surface ared in me. mania = Mass flow note in 18%. ATOTh-To = Local temperature difference 4/n not and cold fluids in 'd (60 K. U= Overall heat transfer coefficients. Applying the energy balance: (not & coldflied) Q= mg Ge (Teo-Tei) = mn Gpn (Thi-Tho) -> 0 Heat capacities are. Ca=miaGec and Ch=miaGeh. →@ Rate of heat transfer dá from the hot to the cold fluid through an elemental area da in given by: da=v.dadT -> 3 [Q=UAAT]. Also, da should be equal to the heat given up by the last fluid (or gared by the cold fluid flooring through an elemental area day is. da=m_GcdTc=-mnGndTn -> 19 [-ve sign due to heat lost by the hot fluid] (





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Respiring the above experience

$$dT_{c} = \frac{dQ}{\dot{w}_{c}} \quad \text{and} \quad dT_{h} = \frac{dQ}{\dot{w}_{h}} \quad \varphi_{h}$$

If, $\Delta T_{l} = T_{h} - T_{c}$ and $\Delta T_{e} = T_{h} - T_{c}$, then.

$$dT_{h} - dT_{c} = -\frac{dQ}{\dot{w}_{h}} \quad \varphi_{h} - \frac{dQ}{\dot{w}_{c}} \quad \varphi_{c}.$$

$$d(T_{h} - T_{c}) = -dQ \left[\frac{1}{\dot{w}_{h}} + \frac{1}{\dot{w}_{c}} \right] \rightarrow G$$

Substitute (a) M(b), we get.

$$d(T_{h} - T_{c}) = -UdAdT \left[\frac{1}{\dot{w}_{h}} + \frac{1}{\dot{w}_{c}} \right] - \frac{1}{\dot{w}_{c}}$$

Integrating between inleft and entitet.

entits ΔT_{2}

$$d(T_{h} - T_{c}) = -UdA \left[\frac{1}{\dot{w}_{h}} + \frac{1}{\dot{w}_{c}} \right]$$

$$d(T_{h} - T_{c}) = -UA \left[\frac{1}{\dot{w}_{h}} + \frac{1}{\dot{w}_{c}} \right]$$

Substituting for $\dot{w}_{h} + \dot{w}_{c} - T_{c}$

$$d(T_{h} - T_{c}) = -UA \left[\frac{1}{\dot{w}_{h}} + \frac{1}{\dot{w}_{c}} \right]$$

Substituting for $\dot{w}_{h} + \dot{w}_{c} - T_{c}$

$$d(T_{h} - T_{c}) = -UA \left[\frac{1}{\dot{w}_{h}} + \frac{1}{\dot{w}_{c}} \right]$$

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$$d(T_{h} - T_{c}) =$$





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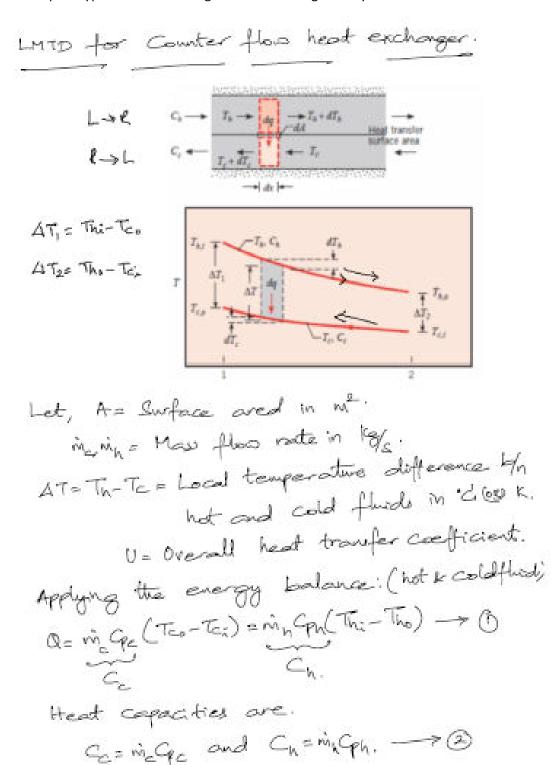
$$\begin{split} & \ln\left(\frac{Th_0-Tc_0}{Th_1-Tc_1}\right) = -\frac{UA}{Q} \left[\frac{Th_1-Th_0+Tc_0-Tc_1}{Th_1-Tc_1}\right] \\ & \text{Recoveraging the term.} \\ & \ln\left(\frac{Th_0-Tc_0}{Th_1-Tc_1}\right) = -\frac{UA}{Q} \left[\frac{Th_1-Tc_1}{Th_1-Tc_1}-\frac{Th_1-Tc_1}{Th_1-Tc_1}\right] \\ & \ln\left(\frac{Th_0-Tc_0}{Th_1-Tc_1}\right) = \frac{UA}{Q} \left[\frac{Th_0-Tc_0}{Th_1-Tc_1}-\frac{Th_1-Tc_1}{Tc_1}\right] \\ & -\frac{UA}{Q} \left[\frac{Th_0-Tc_0}{Th_1-Tc_1}-\frac{Tc_1}{Tc_1}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_2}{AT_1}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_2}{Q}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_2}{AT_1}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_2}{AT_1}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_2}{Q}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_1-Q}{Q}\right] \\ & = \frac{UA}{Q} \left[\frac{AT_1-AT_1-Q}{$$





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Topic - Types of Heat Exchangers- Heat Exchanger Analysis- LMTD Method

Rate of head transfer do from the hot to the cold fluid through an elemental area dá in given by: da=u.dadT -> @ [Q=UAAT]. Also, da should be equal to the heat given up by the not fluid (00 gaved by the cold fluid flooring through an elemental area da, is. Q da=- magadTc=-mnGpndTn → @ I -ve sign due to heat lost for hot fluid. -ve sign. due to apposite direction for cold fluid Recoriting the above equations dTc = -da and dTh = da -> 5 If, AT, = Thi-To and ATe= Tho-To:, than. ath-atc = - do + do minger





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Substitute (1) M (2), we get.

$$d(Th-Tc) = -UdAdT \left[\frac{1}{m_{N}Gp_{N}} - \frac{1}{m_{C}Gp_{C}} \right].$$

Integrating bothour inlet and outlet.

out = aT_{E} out
$$d(Th-Tc) = -UdA \left[\frac{1}{m_{N}Gp_{N}} - \frac{1}{m_{C}Gp_{C}} \right].$$

inlet = aT_{E} out
$$ln\left(\frac{Th_{0}-Tc_{E}}{Th_{E}-Tc_{O}} \right) = -UA \left[\frac{1}{m_{N}Gp_{N}} - \frac{1}{m_{C}Gp_{C}} \right].$$

Substituting for minGp_{N} to minGp_{C} from (D), we get
$$ln\left(\frac{Th_{0}-Tc_{E}}{Th_{E}-Tc_{O}} \right) = -UA \left[\frac{Th_{E}-Th_{O}}{Q} - \frac{Tc_{O}-Tc_{E}}{Q} \right].$$

Recovering the term.
$$ln\left(\frac{Th_{0}-Tc_{E}}{Th_{E}-Tc_{O}} \right) = -\frac{UA}{Q} \left[\frac{Th_{E}-T_{O}}{Th_{E}-Tc_{O}} - \frac{Tc_{O}+Tc_{E}}{Q} \right].$$





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Topic - Types of Heat Exchangers- Heat Exchanger Analysis- LMTD Method **References:**

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Other web sources