



Random Variable: Random voollable is a real valued function that applying a numerical value to each possible experiment. outcome of an Eq: an experiment, tossing a com twice. considen The Sample space is B= SHH, HT, TH, TT such that let x be the gandom variable x (No. of heads) X(5)= =5 2, 1, 1, 0 X(S) ( CODI S= THH, HIT, TH, T 1 4 2 5 Random Variable: Of Types pisciete Random variable Variable Random Contenuous Note: P(x r 2) = 1 - P(x < 2) X L 22) Scanned with CamScanner

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# 23MAT203-PROBABILITY AND RANDOM PROCESSES

# SNSCT/MATHEMATICS

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## SNSCOLLEGEOFTECHNOLOGY (An Autonomous Institution) Coimbatore – 641 035 DEPARTMENTOFMATHEMATICS UNIT-1(PROBABILITY ANDRANDOM VARIABLES)



Disciete	Contenuous
* A Random varilable x is said to be discuste if it assumes estimate a is said to be discuste if it assumes estimate it countably 90,47,07,14. Eq: No. of Students present * purbability NOBS Function $P(x)$ * Let x be discuste mandom varilable then purbability mass function satisfies the following conditions. * $P(x_1) \ge 0$ * $\sum_{i=1}^{i=1} P(x_i) = 1$ * To find constant, $\sum_{i=1}^{i=1} P(x_i) = 1$ * To find constant, $\sum_{i=1}^{i=1} P(x_i) = 1$ * To find constant, is $given, then find PMF$ $P(x_0 = F(x_0) - F(x_{1-1})$ * To find mean: $E(x) = \sum_{i=1}^{i=1} x_i P(x_i) := E(x_0^2) = \sum_{i=1}^{i=1} x_i^2 P(x_i)$	<ul> <li>* A Rabdom Varlable × 98 Baid to be controlous of lt takes only an Interival Values.</li> <li>Eg: Age, Weight</li> <li>* Protability density function f(x)</li> <li>* Let x be continuous random variable.</li> <li>Probability density function Satisfies the following conditions</li> <li>* f(x) ≥ 0</li> <li>* f(x) dx = 1</li> <li>* TO FIND cumulative distributive function f(x)</li> <li>* Cumulative distribution is given, then find f(x) = f(x) dx.</li> <li>* To find mean: E(x) = f(x) dx : E(x<sup>2</sup>)=f(x)</li> </ul>



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J. A gaudons variable × bas the following perhability function **x** 0 1 2 3 4 5 6 7 P(x) 0  $K 2K 2K 3K K^2 2K^2 7K^2 + K$ 1). Frod K i). P(x<6), P(x 26), P(02x<5) ili). Distributive as amailative function iv). P(1/22×25/2/×+1) V). Find the smallest value of z such that  $P(x \le z) > \frac{1}{2}$ . Soln. D. Fand K: The many large and a company  $\sum_{i=0}^{n} P(x_i) = 1$ 0+ K+ 2K+ 2K+ 3K+ K2+ 2K2+ 7K2+K  $k = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ -9± 181-2(10)(-1) 2(10)  $= -9 \pm \sqrt{81+40}$  $= -\frac{-9\pm 11}{20} = -1, \pm 10$ K = -1, 10 - 10 Here K = 0.1 ("K=-138 not Possible) Scanned with CamScanner

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••• A LANDON MAN 3 4 5 6 2 7 0 X 0.3 0.01 0.02 0.17 0.2 0.2 0.1 0 P(x) 1 4 1 1 1 T ii).  $P(x \ge b) = P(x = b) + P(x = 1) + P(x = a) + P(x$ P(x=4) + P(x=5) = 0+0.1+0.2+0.2+0.3+0.01 p(x < b) = 0.81 $P(x \geq 6) = 1 - P(x \geq 6)$ =1-0.81 = 0.19 P(0 < x < 5) = P(x = i) + P(x = a) + P(x = 3) + P(x = 4)= 0.1 + 0.2 + 0.2 + 0.3= 0.8 iii) Distributive on cumulative function:  $F(x) = P(x \leq x)$ 0 1 2 3 4 5 6 7. X P(x) 0 0.1 0.2 0.2 0.3 0.01 0.02 0.17 F(x) 0 0.1 0.3 0.5 0.8 0.81 0.83 in) P(版 < × < 标2 / x>1) P(A|B) = P(ADB)<u>≺×∠気 N ×≻リ</u> : P(] x x 1 1/2 / x 71) =-P(x >1)  $= \frac{P(0.5/XX2.5.7.X)}{P(XY1)} \stackrel{(}{\leftarrow} \frac{}{0.5}$ 0.5  $= \frac{P[1 \times x \times 2.5]}{1 - P(x \le 1)}$ Scanned with CamScanner

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 $= \frac{P(x=2)}{1 - [P(x=0) + P(x=1)]}$ =  $\frac{0 \cdot 2}{1 - [0 + 0 \cdot 1]}$ = 0.260. c = Eco. 0. 2 0.9 = 0. 222. (22314 - - (223)  $P(x \leq \pi) > V_2$ V). The values are 4, 5, 6, 7The smallest value is 4. 2J. A random voreable x as the probabolity iii). Distribution function. Boln. i). Fond a:  $\sum_{i=0}^{h} p(x_i) = 1$  $\Rightarrow \frac{8}{5} p(x_i) = 1$ a+3a+5a+7a+9a+11a+13a+ 15a+17a=) 81a=1 => a= 1/81=0.012 Scanned with CamScanner

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$\therefore \ \ \mathbf{a} = 0 \cdot 0 \cdot 2  (\mathbf{a} = 0 \cdot 0 \cdot 2 \cdot 0 \cdot 1 \cdot 1 \cdot 0 \cdot 1 \cdot $										
X	0	1	2 3	3 4	5	6	7		8	
pGx	0.012	0.036 0	. 060 0.0	84 0.)	08 0.1	32 0.1	56 0	-180	0.204	
<u>71)</u>	P(X	< 3)		-	Š. O	E.				
$P(x \ge 3) = P(x = 0) + P(x = 1) + P(x = a)$										
= 0.012 + 0.036 + 0.060 = 0.108										
$P(x \ge 3) = 1 - P(x \ge 3) = 0 = 0$										
= 1-0.108										
		= 0	). 892		100	1 12	= >	) <b>.  </b>	·/].	
P(0 < x < b) = P(x = 1) + P(x = 2) + P(x = 3) + P(x = 4) + P(x = 5)										
= 0.036+0:060+0.084+0.108+0.132										
=0.420 - C 20100 - 500 1000 - 1										
iii). Destrebutton function: $F(x) = P(x \le x)$										
$F(x) = P(x \leq x)$ making A US										
x	0	i I	the second		4			And in the second second reactions	8	
Pa	0.012	0.036	0.060	0.084	0:108	0.132	0.156	0.180	0.204	

0.192 0.300 0.108 0.432 0.588 0.768 0.972

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0.012

F(2)

0.048