

SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)



DEPARTMENT OF MATHEMATICS

Conditional probability:

The Conditional probability of an event B assuming that the event A has happened, is defined as,

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$
, provided $P(A) \neq 0$

Similarly

$$P(A|B) = \frac{P(A|B)}{P(B)}$$
, provided $P(B) \neq 0$

Theorem:

If A and B are independent, then prove that

1. A and B are independent

2. A and B are independent

3. A and B are independent.

Proof: Given A and B are independent => P(AnB) = P(A)P(

1.
$$P(\overline{A} \cap B) = P(\overline{A}) \cdot P(B)$$

Consider.

$$P(B) = P(A \cap B) + P(\overline{A} \cap B)$$

$$= P(B) \left[1 - P(A) \right]$$

.. A and B are independent.

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ANB



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Ans

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2.
$$P(A \cap \overline{B}) = P(A) \cdot P(\overline{B})$$

Consider,

= P(AnB) + P(AnB)

$$P(A \cap B) = P(A) - P(A \cap B)$$

$$= P(A) - P(A)P(B)$$

$$P(AnB) = P(A) P(B)$$

P(AnB) = P(A) P(B) . A and B are independent

3. P(AnB) = P(A).P(B)

Consider.

= I - P(AUB)

$$= 1 - [P(A) + P(B) - P(A \cap B)]$$

$$= 1 - \left[P(A) + P(B) - P(A) \cdot P(B) \right]$$

$$= 1 - P(A) - P(B) + P(A) \cdot P(B)$$

$$= P(\overline{A}) - P(B) [1 - P(A)]$$

$$= P(\overline{A}) - P(B) \cdot P(\overline{A})$$

$$P(\bar{A} \cap \bar{B}) = P(\bar{A}) P(\bar{B})$$

. A and B are independent.

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PROBLEMS:

(1) From a bag containing 5 white balls and 6 green ba 3 balls are drawn with replacement. What is the chance that (i) all are of same colour (ii) they are alternatively of different colours.

(i) P (all are of Same colour)

$$= \frac{5}{11} \times \frac{5}{11} \times \frac{5}{11} \times \frac{5}{11} \times \frac{6}{11} \times \frac{6}{11} \times \frac{6}{11}$$

$$=\frac{125}{1331}+\frac{216}{1331}$$

(ii) P (they are alternatively of different colours)

$$=\frac{5}{11}\times\frac{6}{11}\times\frac{5}{11}+\frac{6}{11}\times\frac{5}{11}\times\frac{6}{11}$$

$$= 150 + 180$$

$$1331 \quad 1331$$

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(3)

(2) If A and B are events with
$$P(A) = \frac{3}{8}$$
, $P(B) = \frac{1}{2}$ and $P(A \cap B) = \frac{1}{4}$, find $P(A^C \cap B^C)$.

Soln:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{3}{8} + \frac{1}{2} - \frac{1}{4} = \frac{5}{8}$$

$$P(A^{C} \cap B^{C}) = P[(A \cup B)^{C}]$$

$$= 1 - P(A \cup B)$$

$$= 1 - \frac{5}{8} = \frac{3}{8}$$

(3) If P(A) = 0.4, P(B) = 0.7, $P(A \cap B) = 0.3$, find $P(\overline{A} \cap \overline{B})$ & $P(\overline{A} \cup \overline{B})$.

Soln:

$$P(AUB) = P(A) + P(B) - P(ADB)$$

$$= 0.4 + 0.7 - 0.3$$

$$= 0.8$$

$$P(\overline{ADB}) = P(\overline{AUB})$$

$$= 1 - P(AUB)$$

$$= 1 - 0.8$$

$$= 0.2$$

$$P(\overline{AUB}) = P(\overline{ADB})$$

$$= 1 - P(ADB)$$

$$= 1 - P(ADB)$$

$$= 1 - P(ADB)$$

$$= 1 - O.3$$

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