



(An Autonomous Institution) Coimbatore - 641 035 **DEPARTMENTOFMATHEMATICS** UNIT-1(PROBABILITYANDRANDOMVARIABLES)



Total Probability:

The probability of A 90 the sample space In P(A) can be experessed interiors of conditional Probabelety. Suppose 'h' mutually exclusive event Bns we can prove that

$$P(A) = \sum_{i=1}^{N} P(A/B_n) - P(B_n)$$

Baye's Theorem:
1.04 A, Az, Az, ..., An be in matually exclusive and exhaustive event, with P(A;) \$ 0 and B be an Independent event BC . A; with P(B) to such

the second of th

 $P(A_{1}|B) = \frac{P(A_{1}) \cdot P(B|A_{1})}{P(A_{1}) \cdot P(B|A_{1})}$

J. In a Bolt Factory machine A, B, C nanufacture 25%, 35%, 40% of the total of their output. 5%, 4% and 2% are defective bolts. A bolt is drawn at a Handom flow the product and is found is to be defective. What are the purbability that it was manufactured by machine A, B, C. 30/n.:

Let A; be the purbability of manafacturing bolt.

10+ B be the pubability of defective Scanned with CamScanner



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NOW
$$P(A_1/B) = \frac{P(A_1) \cdot P(B/A_1)}{\sum_{i=1}^{n} P(A_i) \cdot P(B/A_1)}$$

P(A;)	P(B/A;)	P(A;) · P(B/A;)
P(A1)=25% = 0.25	ტ. 05	୦. ତାୟନ
P(Pa) = 0.35	0.04	0.014
P(A3) = 0.40	0.02	0.008
Top pa a little		The second second second

$$SP(A_i) \cdot P(B/A_i) = 0.0345$$

$$P(A_1|B) = \frac{0.0125}{0.0345} = 0.362$$

$$P(A_2/B) = \frac{0.014}{0.0345} = 0.405$$

$$P(A_3/B) = \frac{0.008}{0.0345} = 0.231$$

Let A; be the probabelisty of manufacturing bolt.

Let B be the defective boilt. Soln:

NOW,
$$P(A_i|B) = \underbrace{P(A_i) \cdot P(B|A_i)}_{E_i}$$

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P(A;)	P(B/A;)	PlA;). PlB/A;)
ವಿ ಸ	5	125
35	4	140
40	2	80

≤ P(A;). P(B/A;)= 345

$$P(A_1|B) = \frac{125}{345} = 0.362$$

$$P(A_{2}/B) = \frac{140}{345} = 0.406$$

$$P(A_3|B) = \frac{80}{345} = 0.232$$

3. The first bag centains 3w balls, 2R, 4B and second bag centains 4w, 3R, 5B, thank bag centains 3w, 4R, 2B. One bag s choosen at Handom and from Ct 3 balls are drawn. Out of these a balls are w, one 9s R ball. what are the probability that they have taken from 1st, 2nd, 3rd bag.

Let A; be the purbability of gelecting bags.

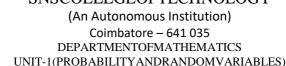
Let B be the purbability of taking balls that

are sev, IR.

P(A;)	P (B/ A;)	P(A;) · P(B/A;)
P(A)=1/3	$\frac{3c_{2}.ac_{1}}{20}=0.071$	0.024
P(A2) = 1/3	903 <u>HC2.301</u> = 0.082	0. 027
P(A3)= V3	$\frac{3c_3}{3c_3 \cdot 4c_1} = 0.143$	0.048
	903 S.P.(9:)	P(B/A;) = 0.099

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$$\frac{3c_{3}\cdot ac_{1}}{ac_{3}} = \frac{3x2x1x2x2x2x1}{2x1x9x2x7} = \frac{1}{14} = 0.071$$

$$\frac{7 + \frac{4 \cdot 3 \cdot 1}{3}}{12 \cdot 3} = \frac{4 \times 3 \times 3 \times 3 \times 2 \times 1}{2 \times 11 \times 10} = \frac{9}{110} = 0.082$$

$$\frac{3c_{8}\cdot 4c_{1}}{9c_{3}} = \frac{3x2x4x3x2x1}{2x1x9x8x7} = \frac{1}{7} = 0.143$$

Now,

$$P(A_1/B) = \frac{0.024}{0.099} = 0.247$$

$$P(A_2)B) = \frac{0.027}{0.099} = 0.272$$

$$P(A_3|B) = \frac{0.048}{0.099} = 0.484$$

AT The chances of 3 candidates A, B, c becomes a manager?

The purbability that Special bonus that will be introduced by them. It selected are 0.6,0.5,0.4 sespectively and the bonus schemes introduced. what is the purbability that is has become one manager?

Let B be the peobabolity of selecting a manager.

Let B be the peobabolity that the special bonus Introduce by 3 candidates.

$$P(A_i/B) = \frac{P(A_i) \cdot P(B|A_i)}{\sum_{i=1}^{B} P(A_i) \cdot P(B|A_i)}$$

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Tolong , and			
P(A;)	P(B/A;)	P(A;). P(B/A;)	
P(A1) = 3 = 0.25	0.6	0.150	
P(A2) = 5 = 0.41	0.5	0.205	
$P(A_3) = \frac{4}{12} = 0.3$	0.4	0.120	

$$P(A_2/B) = \frac{0.205}{0.475} = 0.432$$

5] Let 5 men out of 100 and 25 women out of 100 are colour blind. A colour blind a colour blind what is blind partially of his being male. (Assume that male and female are in equal proposition)

30ln.

Let M be the probability of male.

Let F be the probability of female.

Let c be the probability of colour blind person.

$$P(M) = \frac{1}{2} = 0.500$$

 $P(R) = \frac{1}{2} = 0.500$

$$P(C/M) = \frac{5}{100} = 0.050$$

$$P(C|F) = \frac{a5}{100} = 0.250$$

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DEPARTMENTOFMATHEMATICS

UNIT-1(PROBABILITY ANDRANDOMVARIABLES)



$$P(M/C) = \frac{P(M) \cdot P(C/M)}{\frac{2}{5} P(M) \cdot P(C/M)}$$

$$= \frac{\frac{1}{5} \times 0.05}{0.025 + 0.125}$$

$$\frac{0.025}{0.150}$$

$$P(M/c) = 0.167$$
 (or)

Let P(A;) be male or female.

Let P(B) be selecting a colour blind person at mandom.

P(A;)	P(B/A;)	P(A;) · P(B/A;)
M====0.5	\$/100 = 0.05	0.025
$F = \frac{1}{2} = 0.5$	25/100 = 0.250	0.125

$$P(M/B) = \frac{0.025}{0.150}$$

$$= 0.167$$

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