



(An Autonomous Institution) Coimbatore 35

### **DEPARTMENT OF MATHEMATICS**

UNIT-I TESTING OF HYPOTHESIS

TEST OF SIGNIFICENCE OF SMALL BAMPLES!

STUDENTS t- TEST :

JEST JOR SINGLE MEAN

Null thypothesis . Ho: \u = \u0.

Test statutic, t =  $\frac{\bar{n} - \mu}{S/\sqrt{n-1}}$  if 8D is given.

E = 1 - H & SD & not given.

Fo find s:  $S^2 = \underbrace{S(n-\overline{n})^2}$ 

Degrees & Freedom: v=n-1

NOTE: Confedence Limit: It to 8

1) A sandom sample of to boys had the following Ig's. 70, 120, 110, 101, 88, 83, 95, 98, 107, 100. Do these data support the assumption of a population mean sig's of 100? Find a reservable lange to which most of the mean Ig's value of sample to boys ..

Soln: given: n=10, µ=100

T = 70+120+110+101 +88+88+95+98+107+100 10

= 97.2





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To find s: 
$$g^2 = \frac{\sum (n-\bar{n})^2}{n-1}$$

N: 70 120 110 101 88 83 95 98 107 100

ग-र्रे : -27.२ व.२.६ १२.६ ३.४ -१.२ -१.२ -२.२ ०.८ १.४ २.४

(n- 7) 2: 739.84 519.84 163.84 14.44 84.64 201.64 4.84 0.64 96.04 7.84

$$S^{2} = \frac{\sum (n-\pi)^{2}}{n-1} = \frac{1833.6}{10-1}$$

Step 1: Formulating Ho and Hi! Ho: µ = 100

HI: H + 100 (Two tailed test)

stip 2: Los. at d = 5% = 0.05.

Step 3: Test Statutic, t = M-M 8/Vn





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au t tab: 2.262 (tw)

Step 5: conclusion: E=0.62 < 2.262 = tx

: Ho is accepted at 5% Los.

(e) the population mean Ig's is too.

Confidence limit:

$$\mu = \bar{\chi} + E_{\chi} \frac{3}{\sqrt{n-1}}$$

$$= 972 \pm 2.262 \times \frac{14.27}{\sqrt{10-1}}$$

$$= 97.2 \pm 10.759$$

$$= 107.95, 86.45:$$

3) the weight of 10 peoples of a locality are jourd to be 70, 67, 62, 68, 61, 68, 70, 64, 64, 66 leg it is lesonable to believe that The average weights of people locality epleates than 64 kg. test at 51/2 Los.

90tn: Given: n=10, H=64

死 = 70+67+62+68+61+68+70+64+64+66 10 30 MERCETT NO 1000

5 = 66





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70 find S:  

$$3^{2} = \underbrace{\leq (n-\overline{n})^{2}}_{n-1}$$
71: 76 67 62 68 61 68 76 64 64 66  
71-\overline{n}: 4 1 -4 2 -5 2 4 -2 -2 0  
(71-\overline{n}): 16 1 16 4 25 4 16 4 4 0  

$$\underbrace{\leq (n-\overline{n})^{2}}_{n-1} = 90$$

$$\therefore S^{2} = \underbrace{\leq (n-\overline{n})^{2}}_{n-1} = 90$$

$$S = 3.16$$

Step 1: Formulating to and Hi:

Ho: 
$$\mu = 64$$
 $H_1: \mu \geq 64$  (one tailed test - right)

Step 2: Los at  $\alpha = 5$ ?

Step 3: Test statistic,  $t = \frac{\pi}{2} - \mu$ 
 $\frac{3\sqrt{10}}{3.16\sqrt{10}}$ 
 $= \frac{66-64}{3.16\sqrt{10}}$ 

Step 4:  $t_{ab}$  for degree 9 freedom,  $v = n-1$ 
 $= 10-1$ 
 $= 9$ 

as  $t_{bab}$ :  $t_{ab} = 1.833$  (at two tailed at 10%)





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Step 5: Conelwinon: \( \text{t} = 2.02 > \frac{1.833}{0.9165} = \text{tx} \)

i. Ho & rejected at 5 1/ Los

a) The avg. weight a people locality is executed than 64, kg.





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## JEST FOR DIFFERENCE OF MEAN!

Mull hypothesis; Ho: 
$$H_1 = H_2$$

Test statistics,  $E = \frac{\overline{x_1} - \overline{x_2}}{s \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$ 

where  $s^2 = \frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2 - 2}$  (or)  $s^2 = \underbrace{\sum (x_1 - \overline{x_1})^2 + \sum (m_1 - \overline{x_1})^2}_{n_1 + n_2 - 2}$ 

Deglee of Freedom;  $v = n_1 + n_2 - 2$ .

If n a test examination yiven to two youns of students. the masks obtained were as Jollows:

Group I: 18 20 36 50 49 36 34 49 41

Group I: 29 28 26 35 30 44 46

Enamine whether The significance of difference between the average marks secured by the students of the above two exouns.





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35(n) 
$$2^{10}$$
  $2^{10}$   $2^{1$ 





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Step 1: Formulating Ho and Hi

Ho: H1= H2

H1: H, & H2 (tow tailed test)

stips: Los at a = 5%.

gtip 3: Test statestic, t = x1-x2 SV1+1

10.42 1 + 7

= 0.5 413

Step4: Exal for degrees of freedom, v= n,+n2-2

(ii) that = (tx) = 2.145

step 5: Conclusion: E=0.5413 < 2.145=to.
... Ho is accepted at 5% Los.

: there is no significant difference in the ang.

marks of the two groups of students.





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2) A samples of two types of Electric bulbs were tested for length of life and the following data were obtained. Samples size mean 80. 1 8 1134 35 1134 1 1054 at 57.

Sample 1:  $n_1 = 8$ ,  $\overline{n_1} = 1134$ ,  $g_1 = 35$ 

Sample 9 . no = 4 , 7 = 1024 , So = 40 .

step 1: Formulating Ho and HI. Ho: H1 = H2

HI: HI # H2 (two failed test)

step 2: Los at a=5%.

step 3: Test statistic, t= x1-x2 SV1+1

Now 5= n, s, 2+n282 = 8 (35)2+ 7 (40)2 = 1615.38 8 = 40.19 mile stand





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