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DEPARTMENT OF MATHEMATICS

UNIT - I

DESIGN OF EXPERIMENTS

Experiment: A collection of data or measurements of some features of an object.

Treatments: Various objects of Comparison in a Comparative experiment are called theatments.

Experimental unit: The Smallest division of the experimental material to which we apply the Greatments.

Blocks: The whole experimental units are divided into subgroups called blocks.

Experimental error: It is the error occurred due to random causes or chance causes or non-assignable factors which are beyond own control.

Basic principles of experimental design

- 1. Randomisation
- 2. Replication
- 3. Local control

Basic Designs of experiment

- 1. Completely Randomised Design (C.R.D or one-way classification)
- 2. Randomised Block Design (R.B.D or Two-way classification)
- 3. Latin Square Design (L. S. D or Three way classification)

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Analysis of Variance (ANOVA)

The analysis of variance is a widely used technique developed by Prof. R.A. Fisher.

tumber of populations (more than two) are equal.

Assumptions:

- 1. Each sample taken is a standom sample
- 2. Each one is independent of the other sample.
- 3. Populations from which samples are taken are normal.
- 4. Variances of the populations are equal.

Completely Randomised Design (One-way Classification):
This is a one factor experiment.

Procedure:

Step 1:

Null hypothesis: Ho: There is no significante difference between columns and errors.

Alternative hypothesis: H.: There is a significant difference between columns and errors.

Step 2:

- * Find N, number of given observation
- * Find T, total number of observation
- # Find correction factor $C.F = \frac{T^2}{N}$

Step 3: Find :

* Moran sum of squares of treatments $SST = \sum x_1^2 + \sum x_2^2 + \sum x_3^2 + \cdots - C.F$



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* Sum of Squares of columns

$$SSC = \frac{(\Sigma x_1)^2 + (\Sigma x_2)^2 + (\Sigma x_3)^2}{c_1} + \dots - C.F$$

Stop 4: ANOVA Table:

Source of Variation	Degree of freedom	Sum of Squares	Mean Sum of Squares	Variance ratio	Table Value
Between Columns	C-1	SSC	$MSC = \frac{SSC}{C-1}$	MSE (or)	Fx (c-1, N-c)
Between	N-c	SSE	$MSE = \frac{SSE}{N-C}$	MSE MSC	E(N-C,C-1)

Step 5: Decision :

If Sinae $|F| < F_{\alpha}$, we accept the hypothesis $|F| > F_{\alpha}$, we deject the hypothesis.

Problem :

(1) A sandom sample is selected from each of these makes of ropes and their breaking strength are measured with the following results. Test whether the breaking strength of the ropes differ significantly.

T II III

70 100 60

72 108 57

75 112 84

80 113 87

83 120 73



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Solution :

Step 12 Null hypothesis : Ho : There is no significant difference between Column and errors.

difference between column and everors

Step 2:

$$T = 1576$$

 $C \cdot F = T^2/N = \frac{1576^2}{18} = 137987.55$

Step 3:

₩,	×3	x,2	7,2	x,2
100	60	4900	10000	3600
110	65	5184	12100	4225
108	57	5625	11664	3249
112	84	6400	12544	7056
113	8 7	6889	12.769	7569
120	73		14400	5329
107	and an		11449	
770	426	28 998	84926	31028
	100 110 108 112 113 120	100 60 110 65 108 57 112 84 113 87 120 73	100 60 4900 110 65 5184 108 57 5625 112 84 6400 113 87 6889 120 73	100 60 4900 10000 110 65 5184 12100 108 57 5625 11664 112 84 6400 12544 113 87 6889 12769 120 73 14400 11449

$$SST = 28998 + 84926 + 31028 - 137987.55$$

$$= 6964.45$$

$$SSC = \frac{(Sx_1)^2 + (Sx_2)^2 + (Sx_3)^2 - C.F}{c_1 - c_2 - c_3}$$

$$= \frac{(380)^2 + (770)^2 + (426)^2 - 137987.55}{5}$$



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SSE = SST - SSC = 6964.45 - 58 38.49

Stop 4 : ANOVA Lable :

Source of Variation	Degree of freedom	Sum of Squares	Mean sum of servares	Variance Vatio	Table Value
Between	C-1 = 3-1 = 2	5838.44	MSC = SSC C-1 = 2919.22	= 38.88	F2 (2,15,
Between	N-c=18-3	SSE =	MSE = SSE N-C = 75.067		

Steps: Decision:

Since F>Fa, we reject the hypothesis

There is a significant difference between Columns
and errors