

(An Autonomous Institution) Coimbatore - 641 035 DEPARTMENT OF MATHEMATICS UNIT- II (STANDARD DISTRIBUTIONS) NORMAL DISTRIBUTION



Normal Distiglibution!

If x is a continuous gardon Variage which follows normal destribution,

$$f(x) = \frac{1}{6\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-u}{6}\right)^{2}}$$

Note:

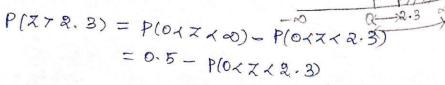
$$M_X(t) = e^{tu + \frac{t^2 \sigma^2}{2}}$$

Properties/charactersctics of Normal Distribute

- + The curve is bein shaped and symmetric about the olygin.
  - + The curive has a single peak it. Unimodel.
  - + The mean of the normal destribution lies at the centre of the walve.
- \* In Normal destribution, mean, median & mode are cognisode.

Note:

Example:

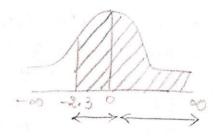




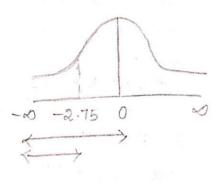
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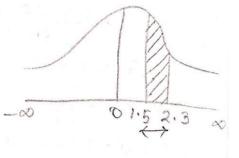
$$p(27-2.3) = P(2.34240)$$
  
+  $P(04240)$   
=  $P(04242.3) + 0.5$ 



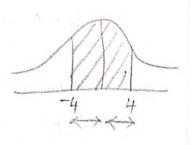
# J. P[24-2-75)



# 刊、P(1.5イスイス、3)



$$P(-A < Z < H)$$
  
=  $P(-H < Z < 0) + P(0 < Z < H)$   
=  $P(0 < Z < H) + P(0 < Z < H)$   
=  $P(0 < Z < H)$ 





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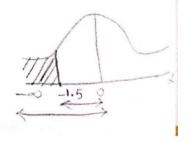
J. In a test on 2000 electric bulbs, it was found that the life of the particular make, was normal distributed with an average life of 2040 hours and S.D. of 60 hours. Estimate the number of bulbs like the burn for i). more than 2150 hours, ii). less that 1950 hours and iii). more than 1920 hours but less than 2160 hours but less soln:

Mean: 11 = 2040 hours

1). P(x \( \) 2150)

Let 
$$z = \frac{x - u}{\sigma}$$
  
=  $\frac{2150 - 2040}{60}$ 

$$\begin{array}{r}
 1950 - 2040 \\
 \hline
 60
 \end{array}$$



-00





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$$p(x \le 1950) = P(7 \le -1.5)$$

$$= P(-\infty < 2 < 0) - P(-1.5 < 2 < 0)$$

$$= P(0 < 2 < \infty) - P(0 < 2 < 1.5)$$

$$= 0.5 - 0.4332$$

$$= 0.067$$

$$= 0.067 \times 2000$$

$$= 134$$

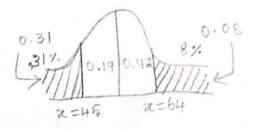
iii) More than 1920 hes and 10% than 2160 hrs.

P(1920 × × 22160)

Let 
$$X = 1920 \Rightarrow Z = \frac{1920 - 2040}{60} = -9$$
  
 $X = 2160 \Rightarrow Z = \frac{2160 - 9040}{60} = 2$ 

$$P(1920 \le x \le 2160) = P(-2 \le x \le 2)$$
 $= 2 \cdot P(0 \le x \le 2)$ 
 $= 2 \cdot [0.4772]$ 
 $= 0.954$ 
 $= 0.954 \times 2000$ 
 $= 1908$ 

5]. In a Normal destribution, 31% of the 9+ems are under 45 and 8% are over 64. find mean & S.D.





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when 2 = 45

13 (1)

Solveng (1) and (2),  

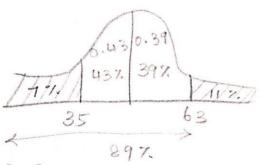
$$-1.96 = -19$$
 $6 = -19$ 

$$\mu = 45 + 0.56$$

$$= 45 + 0.5(10)$$

96 = 64  $1.41 = \frac{64 - 11}{6}$  1.416 = 64 - 11 1.416 = 64 1.416 = 641.416 = 64

3]. In a destrophetion exactly sosmal 7% of one frems are under 35 and 89% are under 63. What are the means Sp of destrophetion.





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When 
$$x = 35$$
 $x = \frac{x - u}{6}$ 
 $x = \frac{x - u}{6}$ 

6=10.33





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# AREA UNDER NORMAL CURVE TABLE OF AREAS

		TABLE OF AREAS										
$\downarrow Z \rightarrow$	0	(1)	/ 2	3	4	5	6	7	8	9		
.0	.0000	.0040	.0080	.0120	.0160	.0199	.0539	.0279	.0319	.0359		
.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753		
.2	.0793	.0832	.0871	.0910	.0480	.0987	.1026	.1064	.1103	.1141		
.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517		
.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879		
								× 1	100			
.5	.1915	.1950	1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224		
.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549		
.7	.2580	.2611	.2642	.2673	.2703	.2734	.2764	.2794	.2823	.2852		
.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133		
.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389		
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621		
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830		
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015		
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177		
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319		
-										1		
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441		
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545		
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4603	.4616	.4625	.4633		
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706		
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767		
					e**			10				
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817		
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857		
2.2	.4861	.4864	.4868	.4871	.4875	.4879	.4881	.4884	.4887	.4890		
2.3	.4893	.4896	.4898	.4901	.4904	.4995	.4900	.4911	.4913	.4916		
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936		
							1.0					
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4959	.4951	.4952		
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4952		
2.7	.4965	.4966	.4967	.4958	.4969	.4970	.4971	.4972	.4973	.4974		
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981		
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986		
	n C) year	A respect	e 1 1			100000000000000000000000000000000000000						
3.0	.4987	.4987	.4987	.4983	.4988	.4989	.4989	.4989	.4990	.4990		
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993		
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995		
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997		
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998		
								.1777	.4771			
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998		
3.6	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999		
3.7	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999		
3.8	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999		
3.9	.5000	.5000	.5000					20 miles 20 miles				
3.9	.5000	.5000		.5000	.5000	.5000	.5000	.5000	.5000	.5000		