

SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)

Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai

Accredited by NAAC-UGC with 'A++' Grade (Cycle III) &

Accredited by NBA (B.E - CSE, EEE, ECE, Mech & B.Tech.IT)

COIMBATORE-641 035, TAMIL NADU



Pipes and Cisterns

Problems on Pipes and Cisterns are based on the basic concept of time and work. Pipes are connected to a tank or cistern and are used to fill or empty the tank or cistern. In pipe and cistern, the work is done in form of filling or emptying a cistern/tank.

Inlet pipe : It fills a tank/cistern/reservoir.

Outlet pipe: It empties a tank/cistern/reservoir.

Important Points:

1. If a pipe can fill/empty a tank in 'm' h, then the part of tank filled /emptied in $1 h = \frac{1}{m}$.

For example, A pipe can fill the tank in 7 h, then the volume of tank filled in $1 h = \frac{1}{7}$.

2. If a pipe can fill/empty ' $\frac{1}{m}$ ' part of a tank in 1 h, then it can fill/empty the whole tank in 'm' h.

For example, If a pipe can fill $\frac{1}{5}$ part of a tank in 1 h, then it can fill the whole tank in 5 h.

3. Generally, time taken to fill a tank is taken positive (+ve) and time taken to empty a tank is taken negative (-ve).
4. If a pipe fills a tank in m h and an another pipe fills in n h. Then, part filled by both pipes in $1 h = \frac{1}{m} + \frac{1}{n}$.

Example : 1 An outlet pipe can empty a cistern in 5 h. In what time will the pipe empty $\frac{2}{5}$ part of the cistern?

Solution : Time taken to empty full cistern = 5 h

$$\text{Time taken to empty } \frac{2}{5} \text{ part of the cistern} = \frac{2}{5} \times 5 = 2 h$$

Example : 2 If a pipe can fill a tank in 2 h and another pipe can fill the same tank in 6 h, then what part of a tank will be filled by both the pipes in 1 h, if they are opened simultaneously?

Solution : In 1 h, part filled by 1st pipe = $\frac{1}{m} = \frac{1}{2}$

In 1 h, part filled by 2nd pipe = $\frac{1}{n} = \frac{1}{6}$.

In 1 h, part filled by both the pipes together = $\left(\frac{1}{m} + \frac{1}{n}\right) = \left(\frac{1}{2} + \frac{1}{6}\right) = \frac{3+1}{6} = \frac{4}{6} = \frac{2}{3}$ part

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Example : 3 If a pipe can fill a tank in 5 h and an another pipe can empty the tank in 10 h, then part fill by both pipes in 1 h, if both pipes are open simultaneously.

Solution: In 1 h, part filled by 1st pipe = $\frac{1}{m} = \frac{1}{5}$

In 1 h, part emptied by 2nd pipe = $\frac{1}{n} = \frac{1}{10}$

In 1 h, part filled by both pipes when open simultaneously = $\frac{1}{m} - \frac{1}{n}$

$$= \frac{1}{5} - \frac{1}{10} = \frac{2-1}{10} = \frac{1}{10} \text{ part} \quad [-\text{ve sign is used, as } 2^{\text{nd}} \text{ pipe empties the tank}]$$

Fast Track Techniques to solve the Questions

Technique :1

If a pipe can fill/empty a tank in ' m ' h and an another pipe can fill/empty the same tank in ' n ' h, then

- If both pipes either fills or empties the tank, then the time taken to fill or empty the tank when both pipes are opened is $t = \frac{mn}{m+n}$
- If first pipe fills the tank and second pipe empties the tank, then the time taken to fill the tank when both pipes are opened is $t = \frac{mn}{m-n} : m > n$
- If first pipe fills the tank and second pipe empties the tank, then the time taken to empty the tank when both pipes are opened is $t = \frac{mn}{n-m} : n > m$

Example : 4 Two pipes A and B can fill a tank in 18 h and 12 h, respectively. If both the pipes are opened simultaneously, how much time will be taken to fill the tank?

Solution: Time taken by both pipes to fill the tank = $\frac{mn}{m+n}$ where m and n are the time taken to fill the tank by individual pipes.

Here, $m = 18, n = 12$

$$\text{Time taken to fill the tank} = \frac{m \times n}{m+n} = \frac{18 \times 12}{18+12} = \frac{18 \times 12}{30} = \frac{3 \times 12}{5} = \frac{36}{5} = 7 \frac{1}{5} \text{ h}$$

Example : 5 A pipe can fill a tank in 5 h, while another pipe can empty it in 6 h. If both the pipes are opened simultaneously, how much time will be taken to fill the tank?

Solution : Here, $m = 5$ h and $n = 6$ h

$$\text{Time taken to fill the tank} = \frac{m \times n}{n-m} = \frac{5 \times 6}{6-5} = \frac{30}{1} = 30 \text{ h}$$

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Example : 6 A pipe can fill a tank in 10 h. Due to a leak in the bottom, it fills the tank in 20 h. If the tank is full, how much time will the leak take to empty it?

Solution: Here, $m = 10$ and $n = 20$

According to the formula,

$$\text{Required time taken to empty the tank} = \frac{m \times n}{n - m} = \frac{10 \times 20}{20 - 10} = \frac{200}{10} = 20 \text{ h}$$

Technique : 2

If three pipes can fill a tank separately in m, n and p h, respectively, then part of tank filled in 1 h by all the three pipes is given by $\left(\frac{1}{m} + \frac{1}{n} + \frac{1}{p}\right)$ and total time taken to fill the tank is given by $\frac{mnp}{np+mp+mn} h$.

Note : If any one of the three pipes is used to empty the tank, then time taken by that particular pipe will be negative (-ve). Suppose, 3rd pipe is used to empty the tank. Then, the above formulae takes the form as $\left(\frac{1}{m} + \frac{1}{n} - \frac{1}{p}\right)$ and $\frac{mnp}{np+mp-mn} h$.

Example : 7 Three pipes m, n and p can fill a tank separately in 4, 5 and 10 h, respectively. Find the time taken by all the three pipes to fill the tank when the pipes are opened together.

Solution : Part filled by pipe m in 1 h = $\frac{1}{4}$

Part filled by pipe n in 1 h = $\frac{1}{5}$

Part filled by $(m + n + p)$ pipes in 1 h = $\frac{1}{4} + \frac{1}{5} + \frac{1}{10} = \frac{5+4+2}{20} = \frac{11}{20}$

Required time to fill the tank = $\frac{20}{11} h = 1 \frac{9}{11} h$.

Example : 8 Pipe A can fill a tank in 20 h while pipe B alone can fill it in 10 h and pipe C can empty the full tank in 30 h. If all the pipes are opened together, how much time will be needed to make the tank full?

Solution : Here, $m = 20, n = 10$ and $p=30$

$$\begin{aligned} \text{Required time to fill the tank} &= \frac{mnp}{np+mp-mn} = \frac{20 \times 10 \times 30}{10 \times 30 + 20 \times 30 - 20 \times 10} \\ &= \frac{6000}{300 + 600 - 200} = \frac{6000}{700} = \frac{60}{7} = 8 \frac{4}{7} h. \end{aligned}$$

Technique : 3

Two pipes A and B together can fill a tank in time t . If time taken by A alone is more than t by a and time taken by B alone is more than t by b , then $t = \sqrt{ab}$.

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Example : 9 Two pipes A and B are opened together to fill a tank. Both the pipes fill the tank in time t . If A separately takes 4 min more time than t to fill the tank and B takes 64 min more than t to fill the tank, find the value of t .

Solution : We know that, time taken by both pipes to fill the tank $(t) = \sqrt{ab}$

Here $a=4$ and $b= 64$

$$t = \sqrt{4 \times 64} = 2 \times 8 = 16 \text{ min}$$

Technique : 4

A full tank get emptied in ' a ' h due to presence of a leak in it. If a tap which fills it at a rate of ' b ' L/h, is opened, then it get emptied in ' c ' h.

Therefore, volume of tank = $\frac{abc}{c-a}$

Example : 10 A full tank get emptied in 6 min due to presence of an orifice in it. On opening a tap which can fill the tank at the rate of 8 L/min, the tank get emptied in 10 min. Find the capacity of tank.

Solution: Here, $a = 6, b = 8$ and $c = 10$

$$\text{Capacity of tank} = \frac{abc}{c-a} = \frac{6 \times 8 \times 10}{10-6} = 120 \text{ L.}$$

Technique : 5

If two taps A and B, which can fill a tank, such that efficiency of A is n times of B and takes t min less/more than B to fill the tank, then

- (i) Time taken to fill the tank by both pipes together = $\frac{nt}{n^2-1}$ min
- (ii) Time taken to fill the tank by faster tap = $\frac{t}{n-1}$ min
- (iii) Time taken to fill the tank by slower tap = $\frac{nt}{n-1}$ min

Example : 11 If tap A can fill a tank 3 times faster than tap B and takes 28 min less than tap B to fill the tank. If both the taps are opened simultaneously, then find the time taken to fill the tank.

Solution: Here, $n = 3$ and $t = 28$

According to the formula,

$$\text{So, time taken to fill the tank by both pipes together} = \frac{nt}{n^2-1} = \frac{28 \times 3}{(3)^2-1} = \frac{21}{2} \text{ min}$$

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Technique : 6

Two pipes A and B can fill a tank in x min and y min, respectively. If both the pipes are opened simultaneously, then the time after which pipe B should be closed so that the tank is full in t min, is $\left[y \left(1 - \frac{t}{x} \right) \right]$ min.

Example : 12 Two pipes A and B can fill a tank in 12 and 16 min, respectively. If both the pipes are opened simultaneously, after how much time should B be closed so that the tank is full in 9 min?

Solution: Here, $x = 12, y = 16$ and $t = 9$

Required time after which B should be closed = $y \left(1 - \frac{t}{x} \right) = 16 \left(1 - \frac{9}{12} \right) = 16 \times \frac{3}{4} = 12$ min.