

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)

DEPARTMENT OF MATHEMATICS

Replace
$$Z = \log(ax + b)^{n-1} \frac{d^n y}{dx^n} + k$$
, $(ax + b)^{n-1} \frac{d^{n-1} y}{dx^{n-1}} + \cdots + k_n y$

Replace $Z = \log(ax + b)$
 $(ax + b) \frac{dy}{dx} = a \cdot b'$
 $(ax + b)^2 \frac{d^2y}{dx^2} = a^2 \cdot b'(b' - 1) \cdot y$
 $(ax + b)^3 \frac{d^3y}{dx^3} = a^3 \cdot b'(b' - 1) \cdot (b' - 2) \cdot y \quad \text{and so on.}$

Problems:

1 Transform the equation to constant coefficients equation

 $(2x + 3)^2 y'' - (2x + 3)y' + 2y = 6x$

Soln:

Put $Z = \log(2x + 3)$
 $e^Z = 2x + 3$
 $e^Z = 2x + 3$



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DEPATMENT OF MATHEMATICS

Given evaction will be,

$$2^{2} D'(D'-1)y - 2D'y + 2y = b \left(\frac{e^{2}-3}{2}\right)$$
 $4(D^{2}-b)y - 2D'y + 2y = 3(e^{2}-3)$
 $4(D^{2}-b)y - 2D' + 2 = 3(e^{2}-b)$
 $4(D^{2}-b)y - 2D' + 2 = 3(e^{2}-b) + 2$
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