

SNS COLLEGE OF TECHNOLOGY



An Autonomous Institution Coimbatore-35

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

23ECT203 - DIGITAL SIGNAL PROCESSING

II YEAR/ IV SEMESTER

UNIT 1 - DISCRETE FOURIER TRANSFORM

TOPIC - LINEAR CONVOLUTION



LINEAR CONVOLUTION



- The convolution sum relates the input, output and unit sample response of the discrete time systems
- Linear convolution is a very powerful technique used for the analysis of Linear Time Invariant systems
- x(n) can be expressed as sum of weighted impulses

$$y(n) = x(n) * h(n)$$



LINEAR CONVOLUTION



• The behavior of the LTI system is completely characterized by the unit sample response h(n)

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$$

• It is the linear convolution of x(n) and h(n) gives y(n) Inverse Z

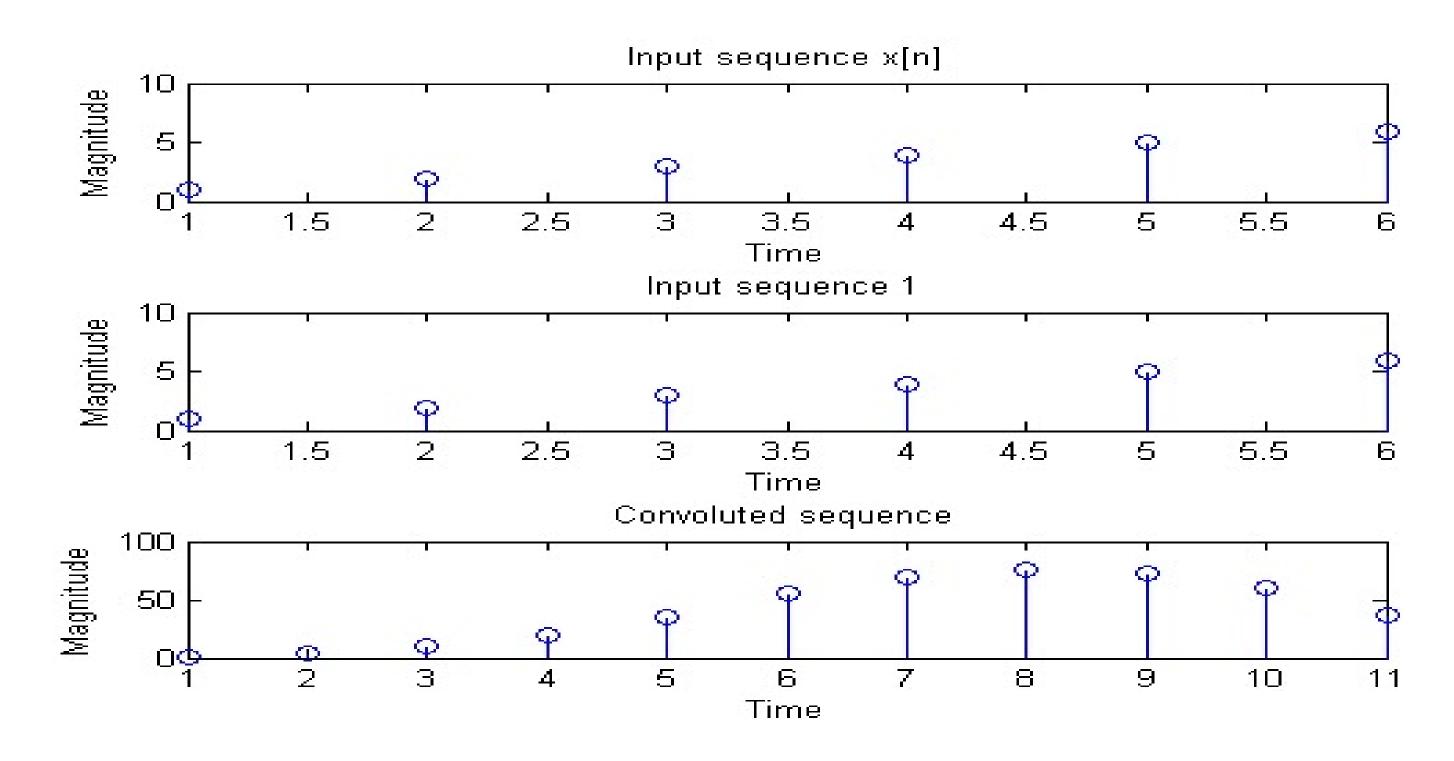
Transform:

$$\mathbf{x}(\mathbf{n}) \longrightarrow \mathbf{LTIDT} \longrightarrow \mathbf{y}(\mathbf{n})$$



REPRESENTATION OF CONVOLUTION

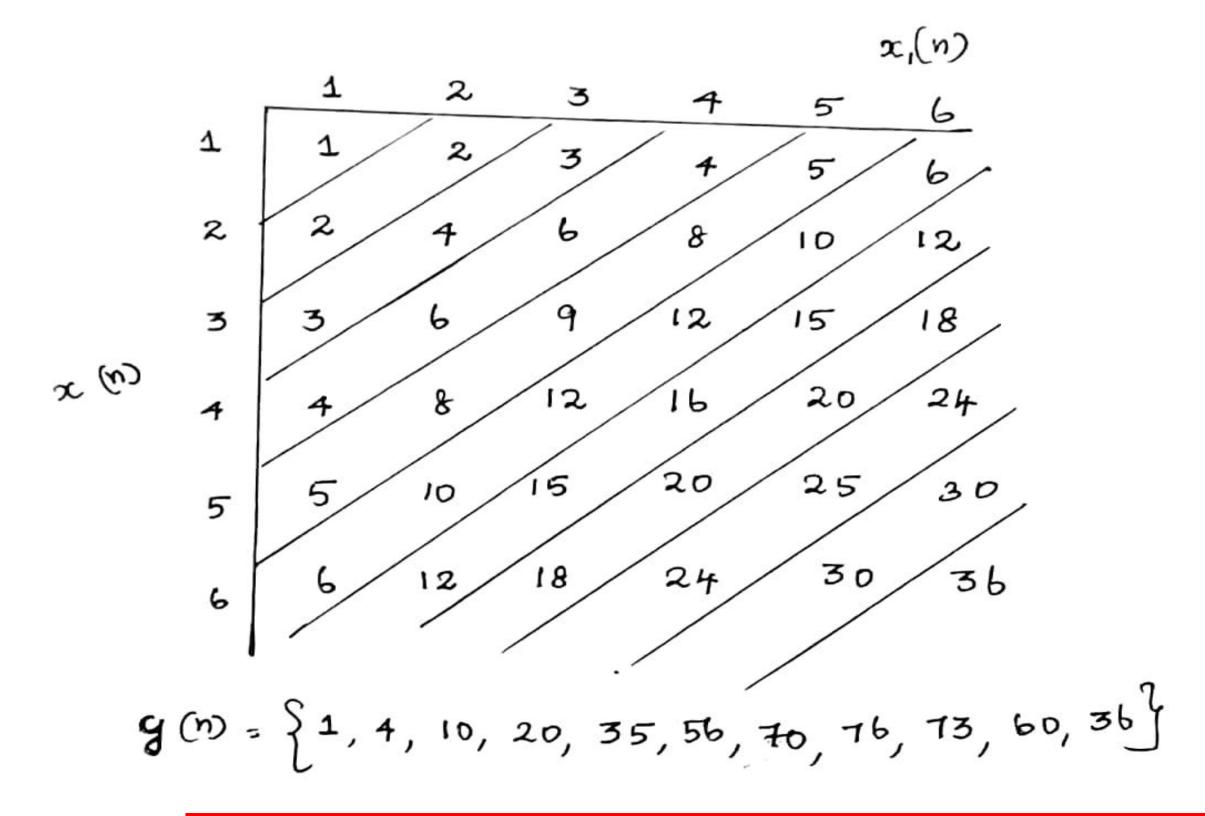






REPRESENTATION OF CONVOLUTION







LINE AR CONVOLUTION



Four methods available to compute convolution sum:

- 1. Definition Method
- 2. Graphical Method
- 3. Tabulation Method
- 4. Multiplication Method



CONVOLUTION SUM



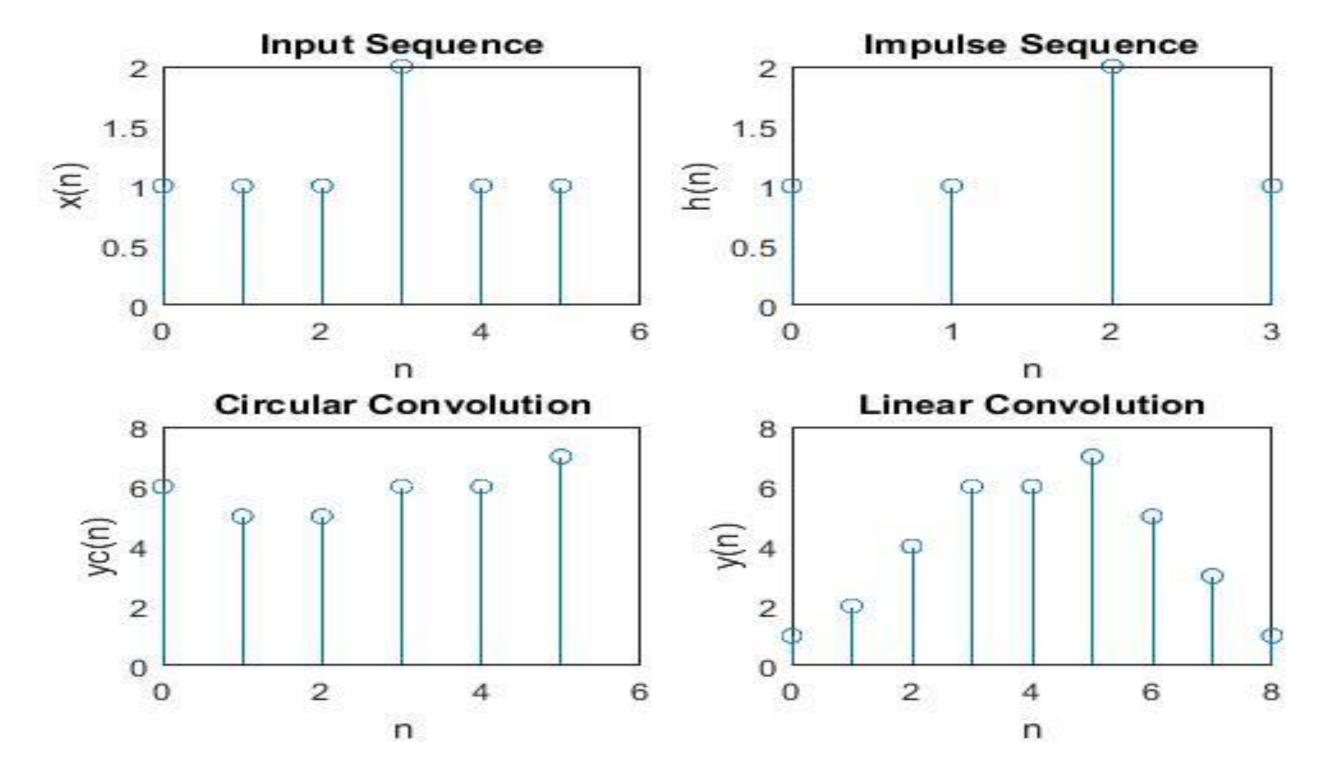
Four steps involved in computing convolution sum:

- 1. Folding
- 2. Shifting
- 3. Multiplication
- 4. Summation
- Let M be the total no. of samples of x(n) and N be the total no. of samples of
- h(n) then the total no. of samples in y(n) be M+N-1



CONVOLUTION SUM







CONVOLUTION SUM





PROPERTIES OF CONVOLUTION SUM



- It can be classified into
- 1. Commutative Property
- 2. Associative Property
- 3. Distributive Property

Commutative:

$$y(n) = x(n) * h(n) = h(n) * x(n)$$

$$x(n)$$
 $h(n)$ $y(n)$

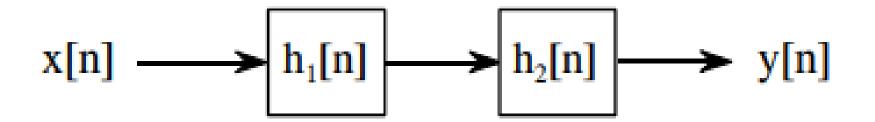
$$h(n)$$
 $x(n)$ $y(n)$

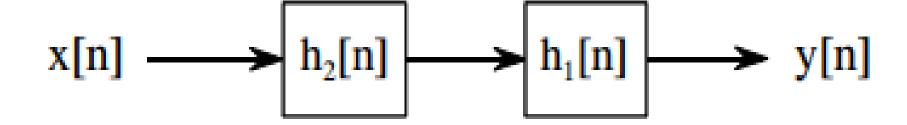


ASSOCIATIVE PROPERTY



$$[x(n) * h_1(n)] * h_2(n) = x(n) * [h_1(n) * h_2(n)]$$





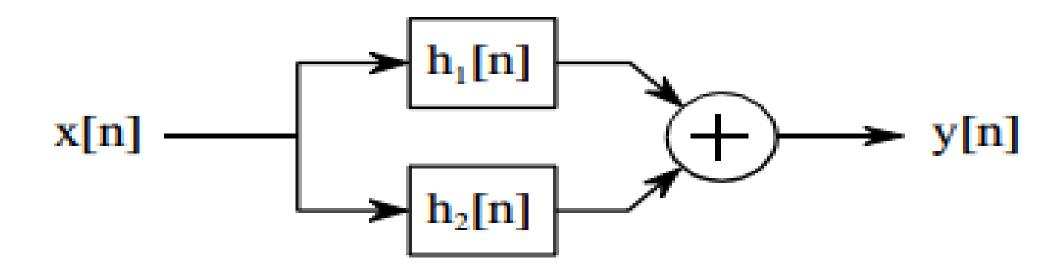
$$x[n] \longrightarrow h_1[n] * h_2[n] \longrightarrow y[n]$$



DISTRIBUTIVE PROPERTY



$$x(n) * h_1(n) + x(n) * h_2(n) = x(n) * [h_1(n) + h_2(n)]$$

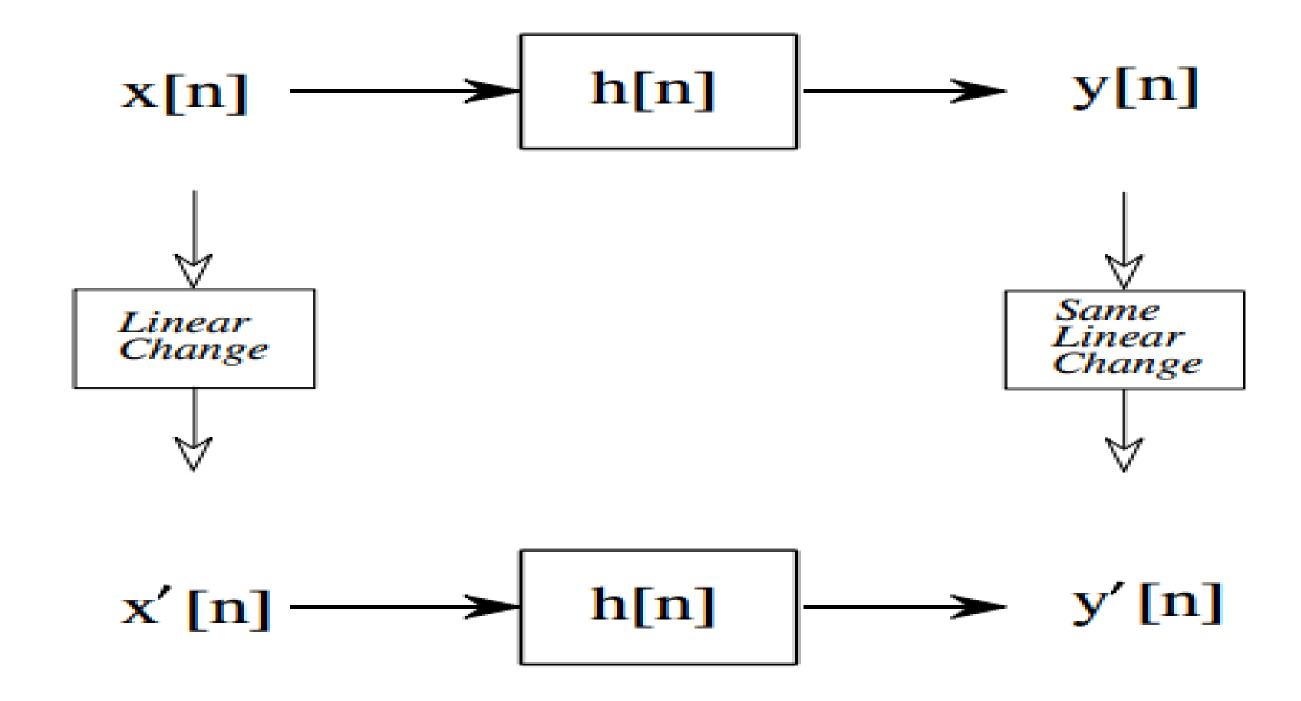


$$x[n] \longrightarrow h_1[n] + h_2[n] \longrightarrow y[n]$$



INPUT & OUTPUT TRANSFERENCE

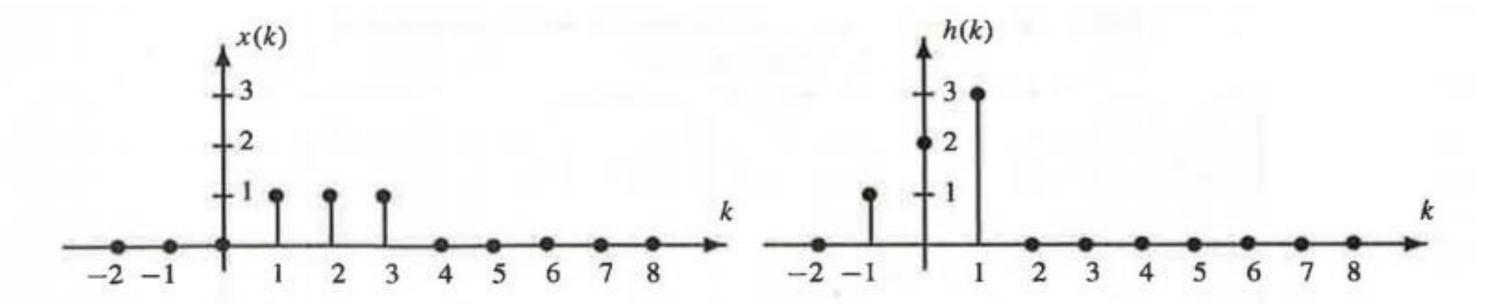


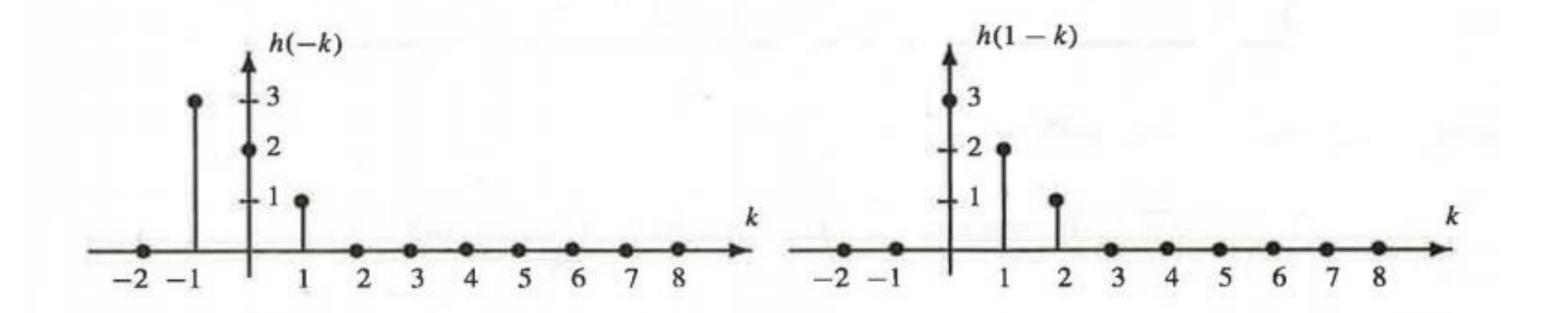




GRAPHICAL REPRESENTATION



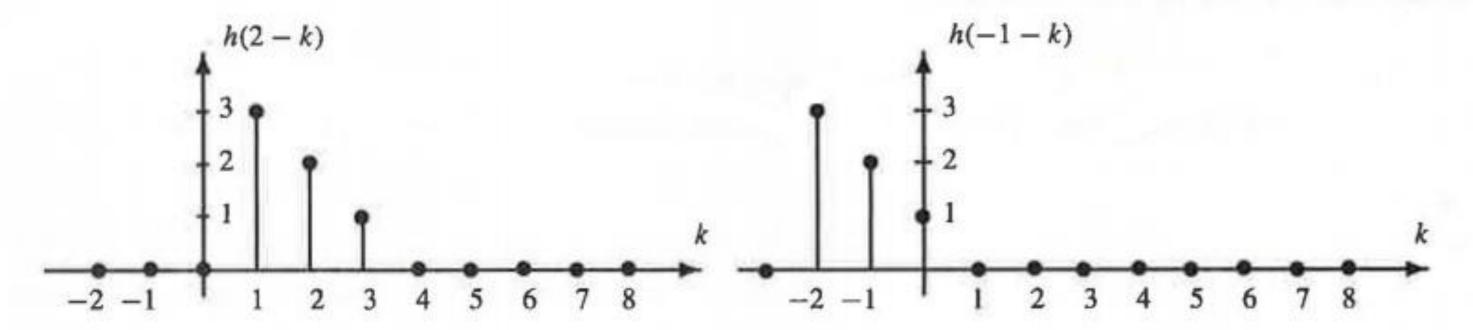


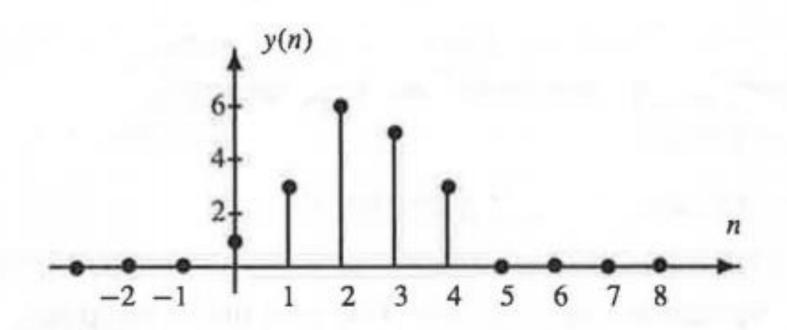




GRAPHICAL REPRESENTATION









MULTIPLICATION METHOD

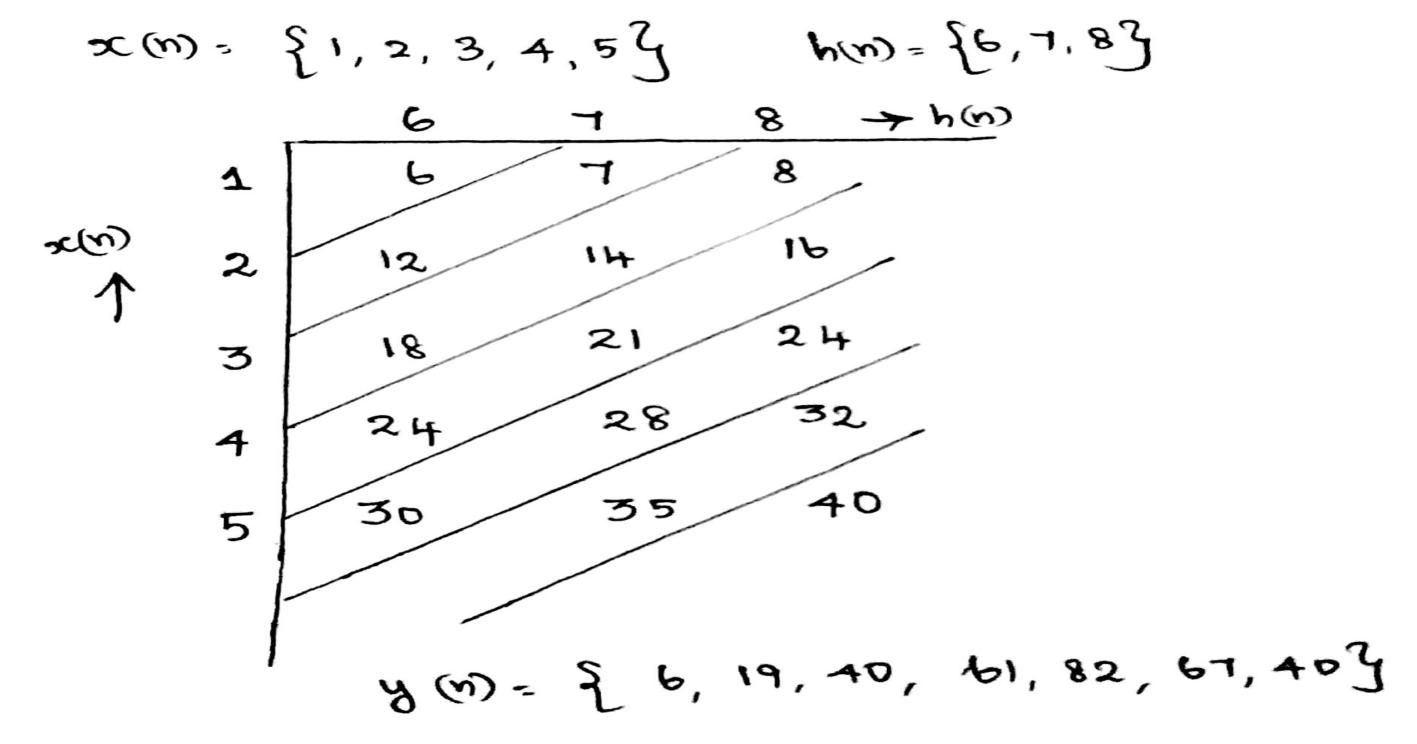


Find	the	tulormo	iwn S	um of	the soy	uence :-
x(m) = {1,2,3,4,5} h(m) = {6,7,8}						
		1	2	3	4	5
				6	٦	8
		8	16	24	32	40
	ヿ	14	21	28	35	
6	12	18	24	30		
6	19	40	61	82	67	40



TABULATION METHOD







DEFINITION METHOD



$$x(m) = \{1,2,3,4,5\}$$
 $h(m) = \{6,7,8\}$
 $x(m) = 1, x(m) = 2, x(m) = 3, x(m) = 4, x(m) = 5$
 $h(m) = 6, h(m) = 7, h(m) = 8$
 $M = 5$
 $N = 3$
 $y(m) = H + N - 1 \Rightarrow 5 + 3 - 1 \Rightarrow T$
 $y(m) = 7$
 $y(m$



ASSESSMENT



- 1. Define convolution sum.
- 2. Total no. of samples in y(n) will be -----
- 3. List the methods involved to compute convolution sum.
- 4. y(n) = x(n) * h(n) = h(n) * x(n) is defined as ----- property
- 5. Mention the steps involved to compute linear convolution.
- 6. List the properties of convolution sum.





THANK YOU