



# SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)

Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai

Accredited by NAAC-UGC with 'A++' Grade (Cycle III) &

Accredited by NBA (B.E - CSE, EEE, ECE, Mech & B.Tech.IT)

COIMBATORE-641 035, TAMIL NADU



## DEPARTMENT OF MATHEMATICS

⑩ To find  $L(\cosh at)$ :

$$\begin{aligned}
 L(\cosh at) &= L\left\{\frac{1}{2}\left[e^{at} + e^{-at}\right]\right\} \\
 &= \frac{1}{2}L(e^{at}) + \frac{1}{2}L(e^{-at}) \\
 &= \frac{1}{2}\left\{\frac{1}{s-a} + \frac{1}{s+a}\right\} \\
 &= \frac{1}{2} \cdot \frac{2s}{s^2 - a^2}
 \end{aligned}$$

$$L(\cosh at) = \frac{s}{s^2 - a^2} \text{ for } s^2 > a^2$$

PROBLEMS:

① Find  $L(t^8)$

$$L(t^n) = \frac{n!}{s^{n+1}}$$

$$L(t^8) = \frac{8!}{s^{8+1}} = \frac{46320}{s^9}$$

② Find  $L(t+1)^2$

$$L[(t+1)^2] = L(t^2 + 2t + 1)$$

$$\begin{aligned}
 &= L(t^2) + 2L(t) + L(1) \\
 &= \frac{2!}{s^3} + \frac{2}{s^2} + \frac{1}{s}
 \end{aligned}$$

③ Find  $L\left(\frac{1}{\sqrt{t}}\right)$

$$\begin{aligned}
 L\left(\frac{1}{\sqrt{t}}\right) &= L(t^{-1/2}) \\
 &= \frac{\Gamma(-1/2 + 1)}{s^{-1/2 + 1}} = \frac{\Gamma(1/2)}{s^{1/2}} = \frac{\sqrt{\pi}}{\sqrt{s}}
 \end{aligned}$$



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4)  $L(\sqrt{t})$

$$L(\sqrt{t}) = L(t^{1/2})$$

$$\Gamma_{n+1} = n \Gamma_n \quad \& \quad \Gamma_{1/2} = \sqrt{\pi}$$

$$= \frac{\Gamma_{1/2+1}}{s^{1/2+1}} = \frac{1/2 \Gamma_{1/2}}{s \sqrt{s}} = \frac{1/2 \cdot \sqrt{\pi}}{s^{3/2}}$$

$$= \frac{\sqrt{\pi}}{2 s^{3/2}}$$

5)  $L(t^{5/2})$

$$L(t^{5/2}) = \frac{\Gamma_{5/2+1}}{s^{5/2+1}} = \frac{5/2 \Gamma_{5/2}}{s^{7/2}}$$

$$= \frac{(5/2 \cdot 3/2 \cdot 1/2) \Gamma_{1/2}}{s^{7/2}} = \frac{15 \sqrt{\pi}}{8 s^{7/2}}$$

6)  $L(e^{5t})$

$$L(e^{at}) = \frac{1}{s-a}$$

$$L(e^{5t}) = \frac{1}{s-5}$$

7)  $L(e^t)$

$$L(e^t) = \frac{1}{s-1}$$

8)  $L(e^{-7t})$

$$L(e^{-7t}) = \frac{1}{s+7}$$

9)  $L(e^{-t})$

$$L(e^{-t}) = \frac{1}{s+1}$$



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10) Find  $\mathcal{L}(\sin 5t)$

$$\mathcal{L}(\sin at) = \frac{a}{s^2 + a^2}$$

$$\mathcal{L}(\sin 5t) = \frac{5}{s^2 + 5^2} = \frac{5}{s^2 + 25}$$

11) Find  $\mathcal{L}(\cos bt)$

$$\mathcal{L}(\cos at) = \frac{s}{s^2 + a^2}$$

$$\mathcal{L}(\cos bt) = \frac{s}{s^2 + b^2} = \frac{s}{s^2 + 36}$$

✓ 12) Find  $\mathcal{L}(\sin^2 2t)$

$$\sin^2 t = \frac{1 - \cos 2t}{2}$$

$$\mathcal{L}(\sin^2 2t) = \mathcal{L}\left[\frac{1 - \cos 2(2t)}{2}\right]$$

$$= \frac{1}{2} \mathcal{L}(1 - \cos 4t)$$

$$= \frac{1}{2} [\mathcal{L}(1) - \mathcal{L}(\cos 4t)]$$

$$= \frac{1}{2} \left[ \frac{1}{s} - \frac{s}{s^2 + 16} \right]$$

✓ 13) Find  $\mathcal{L}(\cos^2 3t)$

$$\cos^2 t = \frac{1 + \cos 2t}{2}$$

$$\mathcal{L}(\cos^2 3t) = \mathcal{L}\left[\frac{1 + \cos 2(3t)}{2}\right]$$

$$= \frac{1}{2} \mathcal{L}(1 + \cos 6t)$$

$$= \frac{1}{2} [\mathcal{L}(1) + \mathcal{L}(\cos 6t)]$$

$$= \frac{1}{2} \left[ \frac{1}{s} + \frac{s}{s^2 + 36} \right]$$



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(14) Find  $L(\cos^3 2t)$

$$\cos^3 \theta = \frac{1}{4} (\cos 3\theta + 3 \cos \theta)$$

$$L[\cos^3 2t] = \frac{1}{4} L[\cos 3(2t) + 3 \cos(2t)]$$

$$= \frac{1}{4} \{ L(\cos 6t) + 3 L(\cos 2t) \}$$

$$= \frac{1}{4} \left\{ \frac{s}{s^2+36} + 3 \frac{s}{s^2+4} \right\}$$

$$= \frac{1}{4} \left\{ \frac{s}{s^2+36} + \frac{3s}{s^2+4} \right\}$$

(15) Find  $L(\sin^3 3t)$

$$\sin^3 \theta = \frac{3 \sin \theta - \sin 3\theta}{4}$$

$$L(\sin^3 3t) = \frac{1}{4} L[3 \sin 3t - \sin 9t]$$

$$= \frac{1}{4} \{ 3 L(\sin 3t) - L(\sin 9t) \}$$

$$= \frac{1}{4} \left\{ 3 \left( \frac{3}{s^2+9} \right) - \frac{9}{s^2+81} \right\}$$

$$= \frac{9}{4} \left\{ \frac{1}{s^2+9} - \frac{1}{s^2+81} \right\}$$

(16) Find  $L(\sin 2t \cos 3t)$

$$\sin A \cos B = \frac{\sin(A+B) + \sin(A-B)}{2}$$

$$L(\sin 2t \cos 3t) = \frac{1}{2} L[\sin(2t+3t) + \sin(2t-3t)]$$





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## DEPARTMENT OF MATHEMATICS

$$\begin{aligned} &= \frac{1}{2} \{L(\sin 5t) + L(\sin(-t))\} \\ &= \frac{1}{2} \{L(\sin 5t) - L(\sin t)\} \\ &= \frac{1}{2} \left\{ \frac{5}{s^2 + 25} - \frac{1}{s^2 + 1} \right\} \end{aligned}$$