

Unit III – Database Design

Dependencies and Normal forms - Functional Dependencies, **Armstrong's axioms for FD's**, closure of a set of FD's, minimal covers-Non- loss decomposition-First,Second,Third Normal Forms, Dependency Preservation-Boyce/Codd Normal Form-Multivalued Dependencies and Fourth Normal Form- Join Dependencies and Fifth Normal Form





Types of Functional Dependencies

Dependencies in DBMS is a relation between two or more attributes.

- 1.Trivial functional dependency
- 2.Non-Trivial functional dependency
- 3.Multivalued functional dependency
- 4.Transitive functional dependency

Trivial functional dependency

- In **Trivial Functional Dependency**, a dependent is always a subset of the determinant.

If $X \rightarrow Y$ and Y is the subset of X , then it is called trivial functional dependency

- Example

roll_no	name	age
42	abc	17
43	pqr	18
44	xyz	18

$\{\text{roll_no}, \text{name}\} \rightarrow \text{name}$ is a trivial functional dependency, since the dependent **name** is a subset of determinant set $\{\text{roll_no}, \text{name}\}$

Similarly, $\text{roll_no} \rightarrow \text{roll_no}$ is also an example of trivial functional dependency.



Non Trivial functional dependency

- In **Non-trivial functional dependency**, the dependent is strictly not a subset of the determinant.

If $X \rightarrow Y$ and Y is not a subset of X , then it is called Non-trivial functional dependency.

Non Trivial functional dependency^{6/19}

- Example

roll_no	name	age
42	abc	17
43	pqr	18
44	xyz	18

roll_no → **name** is a non-trivial functional dependency, since the dependent **name** is **not** a subset of determinant **roll_no**

Similarly, **{roll_no, name}** → **age** is also a non-trivial functional dependency, since **age** is **not** a subset of **{roll_no, name}**

Multivalued functional dependency

- **Multivalued functional dependency**, entities of the dependent set are **not dependent on each other**.
- If $a \rightarrow \{b, c\}$ and there exists **no functional dependency** between **b and c**, then it is called a **multivalued functional dependency**.

- Example

roll_no	name	age
42	abc	17
43	pqr	18
44	xyz	18
45	abc	19

roll_no → {**name, age**} is a multivalued functional dependency, since the dependents **name** & **age** are **not dependent** on each other (i.e. **name** → **age** or **age** → **name** doesn't exist !)

Transitive Functional dependency

- In transitive functional dependency, dependent is indirectly dependent on determinant.
- If $a \rightarrow b$ & $b \rightarrow c$, then according to axiom of transitivity, $a \rightarrow c$. This is **a transitive functional dependency**

Transitive functional dependency ^{10/19}

Example

enrol_no	name	dept	building_no
42	abc	CO	4
43	pqr	EC	2
44	xyz	IT	1
45	abc	EC	2

enrol_no → **dept** and **dept** → **building_no**, Hence, according to the axiom of transitivity, **enrol_no** → **building_no** is a valid functional dependency. This is an indirect functional dependency, hence called Transitive functional dependency.

Armstrong's axioms for FD's

Primary

- ✓ Axiom of reflexivity
- ✓ Axiom of augmentation
- ✓ Axiom of transitivity

Secondary

- ✓ Union
- ✓ Composition
- ✓ Decomposition
- ✓ Pseudo Transitivity

Axiom of reflexivity

- if Y is a subset of X, then X determines Y.
- If $X \supseteq Y$ then $X \rightarrow Y$
- $X \rightarrow X$

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2

Axiom of Transitivity

- if X determines Y and Y determine Z, then X must also determine Z.

• **If $X \rightarrow Y$ and $Y \rightarrow Z$**

then $X \rightarrow Z$

Ram is sibling of Sham
Sham is sibling of Mohan



Ram is sibling of Mohan

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2

**Name \rightarrow Marks and Marks \rightarrow Dept then
name \rightarrow Marks**

Axiom of Augmentation

- The augmentation is also called as a partial dependency.
- In augmentation, if X determines Y, then XZ determines YZ for any Z.
- If $X \rightarrow Y$ then $XZ \rightarrow YZ$

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2

R.No \rightarrow Name then
R.No, Marks \rightarrow Name, marks

- if X determines Y and X determines Z, then X must also determine Y and Z.
- If $X \rightarrow Y$ and $X \rightarrow Z$ then $X \rightarrow YZ$

R.No \rightarrow Name and R.No \rightarrow Marks

R.No \rightarrow Name, marks

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2

Axiom of Decomposition / Splitting

- Decomposition rule is also known as **project rule**. It is the reverse of union rule.
- if X determines Y and Z, then X determines Y and X determines Z separately.
- If $X \rightarrow YZ$ Then $X \rightarrow Y$ then $X \rightarrow Z$

Name, Marks \rightarrow Dept, Course then

Name, Marks \rightarrow Dept and

Name, Marks \rightarrow Dept, Course

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2

Axiom of Pseudo Transitivity

- if X determines Y and YZ determines W, then XZ determines W.
- If $X \rightarrow Y$ and $YZ \rightarrow W$ then $XZ \rightarrow W$

**Roll No \rightarrow Name, and
Name, Marks \rightarrow Dept
Then
Roll No, Marks \rightarrow Dept**

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2



Axiom of Composition

- If $X \rightarrow Y$ and $A \rightarrow B$ then $XA \rightarrow YB$

Roll No \rightarrow Name, and

Marks \rightarrow Dept

Then

Roll No, Marks \rightarrow Name, Dept

R.No	Name	Marks	Dept	Course
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CE	C2
4	B	60	EE	C3
5	C	80	IT	C2



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Thank You!