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$$= \int_{s}^{\infty} \int_$$





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$$= \left[\log S - \log (S^{2}+1)^{1/2}\right]_{S}^{\infty}$$

$$= \left[\log \frac{S}{\sqrt{S^{2}+1}}\right]_{S}^{\infty}$$

$$= \left[\log \frac{1}{\sqrt{1+\frac{1}{S^{2}}}}\right]_{S}^{\infty}$$

$$= \log 1 - \log \frac{S}{\sqrt{S^{2}+1}}$$

$$= \log \left[\frac{S}{\sqrt{S^{2}+1}}\right]$$

$$= \log \left[\frac{\sqrt{S^{2}+1}}{S}\right]$$

$$= \log \left(\frac{\sqrt{S^{2}+1}}{S^{2}+1}\right) dS$$

$$= \left[\log (S^{2}+3) - \log (S^{2}+4)\right]_{S}^{\infty}$$

$$= \left[\log \left(\frac{S^{2}+3}{S^{2}+1}\right)\right]_{S}^{\infty} = \log \left(\frac{S^{2}+4}{S^{2}+3}\right)$$





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Find L
$$\left[\frac{1-\cos at}{t}\right] = \int_{S}^{\infty} L \left(1-\cos at\right) ds$$

$$= \int_{S}^{\infty} \left[\frac{1}{s} - \frac{s}{s^{2}+a^{2}}\right] ds$$

$$= \left[\log s - \frac{1}{2}\log(s^{2}+a^{2})\right]_{S}^{\infty}$$

$$= \left[\log \left(\frac{s}{\sqrt{s^{2}+a^{2}}}\right)\right]_{S}^{\infty}$$

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$$= \frac{s}{s} L \left[\cos at - \cos bt\right] ds$$

$$= \int_{S}^{\infty} \left[\frac{a}{s^{2}+a^{2}} - \frac{b}{s^{2}+b^{2}}\right] ds$$

$$= \frac{1}{a} \left[\log\left(s^{2}+a^{2}\right) - \log\left(s^{2}+b^{2}\right)\right]_{S}^{\infty}$$

$$= \frac{1}{a} \left[\log\left(s^{2}+a^{2}\right) - \log\left(s^{2}+a^{2}\right)\right]_{S}^{\infty}$$





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DEPARTMENT OF MATHEMATICS

(5) Find the Laplace transform of
$$e^{\pm}\int_{s}^{t} \pm \cos t \, dt$$

$$\frac{|soln|}{|soln|} = \left[\frac{1}{s} \left(\int_{s}^{t} \pm \cos t \, dt \right) \right]_{s \to s+1}$$

$$= \left[\frac{1}{s} \left(\frac{1}{s} + \left(\cos t \right) \right) \right]_{s \to s+1}$$

$$= \left[\frac{1}{s} \left(\frac{1}{s} + \left(\cos t \right) \right) \right]_{s \to s+1}$$

$$= \left[\frac{1}{s} \left(\frac{1}{s} + \left(\cos t \right) \right) \right]_{s \to s+1}$$

$$= \left[\frac{1}{s} \left(\frac{s}{s^{2}+1} \right) \right]_{s \to s+1}$$

$$= \left[\frac{1}{s} \left(\frac{s^{2}+1-as^{2}}{(s^{2}+1)^{2}} \right) \right]_{s \to s+1}$$

$$= \left[\frac{1}{s} \left(\frac{1-s^{2}}{(s^{2}+1)^{2}} \right) \right]_{s \to s+1}$$

$$= \left[\frac{s^{2}-1}{s \left(s^{2}+1 \right)^{2}} \right]_{s \to s+1}$$

$$= \frac{(s+1)^{3}-1}{(s+1)(s^{3}+as+a)^{2}}$$
(6) Evaluate using Laplace transform
$$\int_{s}^{s} \pm e^{-at} \sin 3t \, dt$$





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(3) Find the Laplace transform of
$$e^{\pm}\int_{0}^{\infty} E \cos t \, dt$$

Soln:

$$L\left[e^{\pm}\int_{0}^{\infty} E \cos t \, dt\right] = \left[L\left(\int_{0}^{\infty} E \cos t \, dt\right)\right]_{S \to S+1}$$

$$= \left[\frac{1}{5}L(E \cos t)\right]_{S \to S+1}$$

$$= \left[\frac{1}{5}\left(\frac{-d}{ds}L(\cos t)\right)\right]_{S \to S+1}$$

$$= \left[\frac{-1}{5}\left(\frac{d}{ds}\left(\frac{S}{S^{2}+1}\right)\right]_{S \to S+1}$$

$$= \left[\frac{-1}{5}\left(\frac{S^{2}+1-2S^{2}}{(S^{2}+1)^{2}}\right)\right]_{S \to S+1}$$

$$= \left[\frac{-1}{5}\left(\frac{1-S^{2}}{(S^{2}+1)^{2}}\right)\right]_{S \to S+1}$$

$$= \left[\frac{S^{2}-1}{S(S^{2}+1)^{2}}\right]_{S \to S+1}$$

$$= \frac{(S+1)^{2}-1}{(S+1)(S^{2}+2S+2)^{2}}$$

(1) Evaluate using Laplace transform
$$\int_{0}^{\infty} E^{-2t} \sin 3t \, dt$$