SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore – 641 035

DEPARTMENT OF MATHEMATICS CROSS CORRELATION



Cross correlation:

A cross correlation of a two Random

Processes X(4) & Y(t) is defended by,

$$R_{xy}(\tau) = E[x(t) \ y(t+\tau)]$$

$$R_{yx}(\tau) = E[y(t) \cdot x(t+\tau)]$$

1. If x(t) and y(t) are was process, then $R_{xy}(-\tau) = R_{yx}(\tau)$

PLOOF:

WHT
$$R_{xy}(\tau) = E[x(t) \cdot y(t+\tau)]$$

Now, $R_{xy}(-\tau) = E[x(t) \cdot y(t-\tau)]$
Take $t-\tau=t_1 \Rightarrow t=t_1+\tau$
 $R_{xy}(-\tau) = E[x(t_1+\tau) \cdot y(t_1)]$
 $= E[y(t_1) \cdot x(t_1+\tau)]$
 $R_{xy}(-\tau) = R_{yx}(\tau)$

R. If X(t) and Y(t) are uses placess, then $R_{XX}(\tau) \leq \int R_{XX}(0) R_{YY}(0)$

Peoof:

$$R_{xy}(\tau) = E[x|t) y|t+\tau U$$

By schwartz graquality peoperty, $\left[E(xy)\right]^{2} \leq E(x^{2}) \cdot E(y^{2})$

$$E[x(t)|y(t+t)]^{2} \leq E[x^{2}(t)] \cdot E[y^{2}(t+t)]$$

$$[R_{xy}(t)]^{2} \leq E[x^{2}(t)] \cdot E[y^{2}(t+t)]$$

$$\vdots \quad E[y^{2}(t+t)] = E[y^{2}(t)]$$

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$$[R_{xy}(\tau)]^{2} \leq E[x^{2}(t)] \cdot E[y^{2}(t)]$$
By Prep. (1), $\Rightarrow E[x^{2}(t)] = R_{xx}(0)$

$$E[y^{2}(t)] = R_{yy}(0)$$

$$\vdots \left[R_{xy}(\tau)\right]^{2} \leq R_{xx}(0) \cdot R_{yy}(0)$$

$$R_{xy}(\tau) \leq \int_{R_{xx}} R_{xx}(0) \cdot R_{yy}(0)$$

F. Consider two R.P. $x(t) = 3 \cos(\omega t + \theta)$ and $y(t) = 2 \cos(\omega t + \phi)$, where $\phi = \theta - \frac{\pi}{2}$ and θ is cusiformly distributed. Mardom variable over $(0, 2\pi)$. Verify that $|R_{xy}(t)| \leq \sqrt{R_{xx}(0)} \cdot R_{yy}(0)$. Soln.

PDF
$$f(\theta) = \begin{cases} \frac{1}{2\pi}, & 0 \le \theta \le 2\pi \\ 0, & \text{otherwise} \end{cases}$$

Then
$$P_{XX}[t,t+T) = E[X(t)X(t+T)]$$

$$= E[9(\omega L(\omega t+\omega T+\Theta)]$$

$$= \frac{9}{2} E[2(\omega L(\omega t+\omega T+\Theta) \cdot C\alpha L(\omega t+\Theta)]$$

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$$= \frac{9}{2} C\alpha L(\omega t+\frac{9}{4\pi}) C\alpha L(2(\omega t+\omega T+\Theta)) d\theta$$

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and and proved that it is become and any

The start of the s

$$R_{xx}(\tau) = \frac{9}{2} \cos \omega \tau$$

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$$Y(t) = \mathfrak{D}(cc)(\omega t + \varphi)$$

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$$= \mathfrak{D$$

Let x(t) & y(t) & defined by x(t) = A cos w + B sin wt and y(t) = B cos w t - A sin w t where w is a constant and A, B are independent in vs. both baving zero mean problance of man the cross correlation of x(t) & y(t).

Are x(t) & y(t) forntly wss process?