

SNS COLLEGE OF TECHNOLOGY (An Autonomous Institution) Coimbatore – 641 035 DEPARTMENT OF MATHEMATICS LINEAR SYSTEMS WITH RANDOM INPUTS



6]. If x(t) is the input Voltage to a Circuit and y(t) is the output Voltage. [x(t)] is a Stationway 1.p. with $u_x=0$ and $R_{xx}(T)=e^{-2(|T|)}$. Find the mean u_y and power spectrum by $y(\omega)$ of the output is the system transfer function is 9 fven by $H(\omega)=\frac{1}{\omega+2i}$.

Green $u_{x}=0$, $R_{xx}(t)=e^{2(t)}$ WHAT $Y(t)=\int_{-\infty}^{\infty}b(u) x(t-u) du$ $E[Y(t)]=E[\int_{-\infty}^{\infty}b(u) x(t-u) du]$



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SIB

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$$H_{y} = 0 \qquad \therefore M_{x} = 0$$

$$\lim_{S_{xx}} (\omega) = \int_{S_{xx}} F_{xx}(\tau) e^{-i\omega\tau} d\tau$$

$$= \int_{\infty}^{\infty} e^{-RTT} (\cos \omega \tau d\tau - i \int_{\infty}^{\infty} e^{-RTT} (\cos \omega \tau - i \int_{\infty}^{\infty} e^{-RTT$$



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(1)
$$\Rightarrow$$
 $S_{yy}(\omega) = \left(\frac{4}{4+i\omega^2}\right)\left(\frac{1}{\omega^2+4}\right)^2$
$$= \frac{4}{\left(\omega^2+4\right)^2}$$

Soln.

Gaven b(t) = 2et, tro

$$H(w) = \int_{-\infty}^{\infty} b(t) e^{-i\omega t} dt$$

$$= \int_{-\infty}^{\infty} e^{-t} e^{-i\omega t} dt$$

$$= 2 \int_{0}^{\infty} e^{-(1+i\omega)t} dt$$

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$$= \frac{-8}{1+i\omega} (o_{-1})$$

$$H(\omega) = \frac{2}{1+i\omega}$$

$$|H(\omega)|^2 = \frac{4}{1+\omega^2}$$



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Input of PSD:

$$S_{XX}(\omega) = \int_{-\infty}^{\infty} R_{XX}(\tau) e^{-i\omega\tau} d\tau$$

$$= \int_{-\infty}^{\infty} e^{2i\tau} (\cos \omega \tau - i s n \omega \tau) d\tau$$

$$= 2 \int_{-\infty}^{\infty} e^{2i\tau} (\cos \omega \tau) d\tau - i(0)$$

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$$=$$

Output of PSD:

$$Syy(\omega) = S_{xx}(\omega) * |H(\omega)|^{9}$$

$$= \frac{4}{4+\omega^{9}} \frac{4}{1+\omega^{9}}$$

$$= \frac{16}{(1+\omega^{9})(4+\omega^{9})}$$

&J. A WSS bosse Process N(t) has an auto correlation function $P_{NN}(\tau) = Pe^{-3|\tau|}$ where P le a constant. Find le power spectrum. Caven RNN(T) = Pe Soln .:

Signal
$$R_{NN}(T) = Pe^{-3|T|} e^{-i\omega T} dT$$



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$$= P \int_{-\infty}^{\infty} e^{-3|T|} \left(\cos \omega \tau - i 890 \omega \tau \right) d\tau$$

$$= P 2 \int_{0}^{\infty} e^{-3T} \cos \omega \tau d\tau - i(0)$$

$$= 2P \frac{3^{2}}{3^{2} + \omega^{2}}$$

$$= \frac{6P}{91.02}$$