



Linear Systems with landom inputs * input -output selationship to the time domain J. IF bits is the impulse response of the linear System & Y(t) is the output losponse of the System for the Poput x(t), then the output correlation function is given by, $R_{yy}(\tau) = b(-\tau) * b(\tau) * R_{xx}(\tau)$ The class correlation function between the Poput XIt, and the output Y(t) is given by, Rxy(T) = b(T) * Rxx(T) * Input-output relationship in the frequency domain J. IF b(t) is the work empulse response of the lanear system & gits is the response of the System for the input x(t), then $S_{y}(F) = |H(F)|^{2} S_{x}(F)$





2). The brows power density spectrum between
the Priput and output processes of a known
system &
$$9VD$$
. by
 $S_{XY}(f) = H(f)$. $S_X(f)$
 $w \rightarrow 2\pi f$
Mean and rocan-square value of the input:
The mean of the output of a lensear system
& given by $\overline{y} = H(0)\overline{x}$





J. Constitutes a literate System as shown below:

$$\frac{x(t)}{(t+1)\omega} \frac{y(t+1)}{y(t+1)}$$

$$x(t+1) is the imput and y(t+1) is the imput of the system. The imput consolution of x(t+1) is $R_{x,x}(t) = 3.$ S(t)
field the power spectral density auto consolution function and mean equare value of the purput y(t+1).
goln.
The input auto consolution is $9v_{21}$ by $R_{x,x}(t) = 3.$ S(t)
 $R_{x,x}(t) = 3.$ S(t)
 $S_{x,x}(\omega) = \int_{0}^{\infty} B_{x,x}(t) e^{-i\omega t} dt$
 $= \int_{0}^{\infty} 3.$ S(t) $e^{-i\omega t} dt$
 $R_{x,x}(\omega) = 3$ \therefore F[S(t)] = 1
and $H(\omega) = \frac{1}{6+j\omega}$
 $H(\omega) = \frac{1}{\sqrt{6^{2}+\omega^{2}}}$
 $H(\omega) = \frac{1}{\sqrt{6^{2}+\omega^{2}}}$
 $R_{y,y}(t) = \frac{1}{2\pi t} \int_{0}^{\infty} \frac{3}{36+\omega^{2}} e^{i\omega t} d\omega$$$

3





$$= \frac{3}{2\pi} \left[\frac{\pi}{6} e^{6\pi i \pi} \right] \qquad \text{wk}$$

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$$= \frac{1}{4} e^{-6\pi i \pi} e^{2\pi i \pi} e^{2\pi i \pi} \right] \qquad \text{wk}$$

$$= \frac{1}{4} e^{-6\pi i \pi} e^{2\pi i \pi} e$$

4





J Assume a nardom Process XHJ is given as
applet to a System with transfer function

$$H(f) = 1$$
, $-W < F < W$
Find the output correlation function and powers
of output process Assume the autosorrelation ob
input process $\Omega_{S} (\frac{\eta_{0}}{2} S(T))$.
Solo:
 $C(Sven R_{XX}(T) = \frac{\eta_{0}}{2} S(T)$
Taking Founded transform of $R_{XX}(T)$,
 $S_{X}(f) = \frac{\eta_{0}}{2} , -\infty < f < \infty$
 $f(S(T)] = 1$
 $S_{Y}(f) = 1 H(f) = S_{X}(f)$
 $= 1 (\frac{\eta_{0}}{2})$
 $= \frac{\eta_{0}}{2} , -W = f = W$

5





power of Y(t) = J Sylt , df $= a \int \frac{D}{a} dF$ $R_{yy}(\tau) = \int \frac{D_0}{2} e^{i2\pi f \tau} df$ $= \frac{n_0}{2} \int (\cos a\pi ft + isgn a\pi ft) df$ $= \frac{20}{2} \left[2 \int_{0.6}^{10} RTFT dF + i(0) \right]$ = 2 [SPD & TFT] = 20 W [SPO 2TWT - 0] Ryy (T) = bowSPD (ATTWI) = DOW [SPD (2TTWI)] 2TT I W Power of $Y(t) = B_{yy}(0) = D_0 \cdot V \cdot V$ = $D_0 \cdot W \cdot V \cdot V = D_0 \cdot V \cdot V \cdot V \cdot V = D_0 \cdot V \cdot V \cdot V \cdot V = D_0 \cdot V \cdot V \cdot V \cdot V = D_0 \cdot V \cdot V \cdot V \cdot V = D_0 \cdot V \cdot V \cdot V \cdot V = D_0 \cdot V = D_$