

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)

DEPARTMENT OF MATHEMATICS

$$= \underbrace{Sin 3t}_{3} \underbrace{\left[\frac{e^{t}}{10}\left(-\cos 3t + 3\sin 3t\right) - \frac{1}{10}\left(-i\right)\right]}_{3}$$

$$= \underbrace{\left[\frac{e^{t}}{3}\right]}_{3} \underbrace{\left[\frac{e^{t}}{10}\left(-\sin 3t - 3\cos 3t\right) - \frac{1}{10}\left(-i\right)\right]}_{10}$$

$$= \underbrace{\left[\frac{e^{t}}{30}\right]}_{3} \underbrace{\left[\sin 3t + \cos^{2} 3t\right]}_{3} + \underbrace{\left[\frac{1}{30}\right]}_{3} \underbrace{\left(\sin 3t + 3\cos 3t\right)}_{3}$$

$$= \underbrace{\frac{e^{t}}{10}}_{10} + \underbrace{\frac{1}{30}}_{3} \underbrace{\left(\sin 3t + 3\cos 3t\right)}_{3}$$
Applications of Laplace transforms to

Differential equations:

If $L[f(t)] = F(s)$ then
$$L[g'(t)] = s^{2}L(y) - g(0)$$

$$L[g''(t)] = s^{2}L(y) - g(0)$$

$$L[g''(t)] = s^{2}L(y) - g(0)$$
Of Solve the differential equations using LT
$$\underbrace{g'' + 4g' + 4g}_{1} = e^{-t}$$
For each sides,
$$L(g'' + 4g' + 4g) = L(e^{t})$$

$$L(g'') + 4L(g') + 4L(g) = \underbrace{I}_{S+1}$$

$$\underbrace{\left[s^{2}L(y) - sg(0) - g'(0)\right]}_{S+1} + \underbrace{\left[s^{2}L(y) - g(0)\right]}_{S+1}$$



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DEPARTMENT OF MATHEMATICS

(2) Solve using
$$1 + \frac{d^2y}{dt^2} + b \frac{dy}{dt} + 9y = 3e^{-3t}$$
, $y(0) = 1$, $y'(0) = -2$

$$\frac{soln:}{y'' + 6y' + 9y} = 2e^{-3t}$$

$$1 (y'' + 6y' + 9y) = 2(e^{-3t})$$

$$1 (y'' + 6y' + 9y = 2e^{-3t}$$

$$1 (y'' + 6y' + 9y$$